CAPACITY FORCES IN SLIDE JOURNAL BEARING LUBRICATED OIL WITH MICROPOLAR STRUCTURE

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Abstract

Present paper shows the results of numerical solution Reynolds equation for laminar, steady oil flow in slide cylindrical bearing gap. Lubrication oil is fluid with micropolar structure. Properties of oil lubrication as of liquid with micropolar structure in comparison with Newtonian liquid, characterized are in respect of dynamic viscosity additionally dynamic couple viscosity and three dynamic rotation viscosity. Under regard of build structural element of liquid characterized is additionally microinertia coefficient. In modeling properties and structures of micropolar liquid one introduced dimensionless parameter with in terminal chance conversion micropolar liquid to Newtonian liquid. The results shown on diagrams of capacity forces in dimensionless form in dependence on coupling number N^2 and characteristic dimensionless length of micropolar fluid Λ_1. Presented calculations are limited to isothermal models of bearing with infinite length.

Keywords: micropolar lubrication, cylindrical journal bearing, capacity force

1. Introduction

Presented article take into consideration the laminar, steady flow in the crosswise cylindrical slide bearing gap. Non-Newtonian fluid with the micropolar structure is a lubricating factor. Materials engineering and tribology development helps to introduce oils with the compound structure (together with micropolar structure) as a lubricating factors. Exploitation requirements incline designers to use special oil refining additives, to change viscosity properties. As a experimental studies shows, most of the refining lubricating fluids, can be included as fluids of non-Newtonian properties with microstructure [4,5,7,8]. They belong to a class of fluids with symmetric stress tensor that we shall call polar fluids, and include, as a special case, the well known Navier-Stokes model. Physically, the micropolar fluids may represent fluids consisting rigid randomly orientated spherical particles suspended in a viscous medium, where the deformation of fluid particles is neglected [3,4]. Presented work dynamic viscosity of isotropic micropolar fluid is characterized by five viscosities: shearing viscosity η (known at the Newtonian fluids), micropolar coupling viscosity κ and by three rotational viscosities bounded with rotation around the coordinate axes. This kind of micropolar fluid viscosity characteristic is a result of essential compounds discussed in works [4,5]. Regarding of limited article capacity please read above works. In difference to classical oil with Newtonian properties, micropolar fluid is characterized by microinertia of the fluid part and by microrotation velocity field. This fact

determine the additional system of equation development describing micropolar fluid flow which is described by moment of momentum equation. In result of the above, the conjugation between fluid flow field and the microrotation velocity field. In presented flow, the influence of lubricating fluid inertia force and the external elementary body force field were omit [4,5,6].

2. Reynolds equation

Basic equation set defining isotropic micropolar fluid flow are describe following equations [2,4,5,6]: momentum equation, moment of momentum equation, energy equation, equation of flow continuity. Incompressible fluid flow is taken into consideration with constant density skipping the body force. We assume also, that dynamic viscosity coefficients which characterize micropolar fluid are constant. According to above velocity flow field is independent from temperature field and the momentum equation, moment of momentum equation and equation of flow continuity are part of closed system of motion equations. The constant viscosity of micropolar oil, independent from thermal and pressure condition in the bearing. Quantity of viscosity coefficient depend on shearing dynamic viscosity η, which is decisive viscosity in case of Newtonian fluids. Reference pressure p_0 is also described with this viscosity, in order to compare micropolar oils results with Newtonian oil results. In micropolar oils decisive impact has quantity of dynamic coupling viscosity κ [1,3]. In some works concerning bearing lubrication with micropolar oil, it's possible to find the sum of the viscosities as a micropolar dynamic viscosity efficiency. In presented article coupling viscosity was characterized with coupling number N^2, which is equal to zero for Newtonian oil:

$$N = \sqrt{\frac{\kappa}{\eta + \kappa}} \qquad\qquad 0 \leq N < 1 \qquad\qquad (1)$$

Quantity N^2 in case of micropolar fluid, define a dynamic viscosity of coupling share in the oil dynamic viscosity efficiency. From the coupling number N^2 we can determine both dynamic viscosity ratio, which is dimensionless micropolar coupling viscosity:

$$\kappa_1 = \frac{\kappa}{\eta} = \frac{N^2}{1 - N^2} \qquad \kappa_1 \geq 0 \qquad\qquad (2)$$

From the dynamic rotational viscosities at the laminar lubrication, individual viscosities are compared to viscosity γ, which is known as the most important and it ratio to shearing viscosity η is bounded to characteristic flow length Λ, which in case of Newtonian flow assume the zero quantity. Dimensionless quantity of micropolar length Λ_1 and micropolar length Λ are defined:

$$\Lambda = \sqrt{\frac{\gamma}{\eta}} \; ; \qquad \Lambda\Lambda_1 = \varepsilon \qquad\qquad (3)$$

Dimensionless micropolar length Λ_1 in case of Newtonian oil approach infinity. Momentum equation, moment of momentum equation and equation of flow continuity writing out in cylindrical coordinates φ; r; z are presented in article [2,3] where individual phases leading to Reynolds equation for laminar, stationary lubricating process in dimensionless form are mentioned. Reynolds equation for stationary flow of laminar micropolar fluid in the crosswise, cylindrical, slide bearing gap can be present [1,2,7] in dimensional form:

$$\frac{\partial}{\partial\varphi}\left(\frac{h^3}{\eta}\Phi(\Lambda, N, h)\frac{\partial p}{\partial\varphi}\right) + \frac{\partial}{\partial z}\left(\frac{h^3}{\eta}\Phi(\Lambda, N, h)\frac{\partial p}{\partial z}\right) = 6\frac{dh}{d\varphi} \qquad\qquad (4)$$

where: p – hydrodynamic pressure,
      h – gap height of bearing

$\Phi(\Lambda,N,h)$ function in form (5) when in case of the Newtonian fluid it has a value 1 and the Reynolds equation (4) change into a non-Newtonian fluid equation.

$$\Phi(\Lambda,N,h) = 1 + 12\frac{\Lambda^2}{h^2} - 6\frac{N\Lambda}{h}\coth\left(\frac{Nh}{2\Lambda}\right) \tag{5}$$

Reynolds equation (4) can be presented in dimensionless form [1,7] using the method of changing into this values:

$$\frac{\partial}{\partial\varphi}\left(\Phi_1(\Lambda_1,N,h_1)\frac{\partial p_1}{\partial\varphi}\right) + \frac{1}{L_1^2}\frac{\partial}{\partial z_1}\left(\Phi_1(\Lambda_1,N,h_1)\frac{\partial p_1}{\partial z_1}\right) = 6\frac{dh_1}{d\varphi} \tag{6}$$

for $0 \le \varphi \le \varphi_k;\ \ 0 \le r_1 \le h_1;\ \ -1 \le z_1 \le 1$

where: $\Phi_1 = h_1^3 + 12\frac{h_1}{\Lambda_1^2} - 6\frac{Nh_1^2}{\Lambda_1}\coth\left(\frac{h_1N\Lambda_1}{2}\right) \tag{7}$

Reference pressure p_o caused by journal rotation with the angular velocity ω was assumed in (8) taking into consideration dynamic viscosity of shearing η and the lubricating gap height h_1 at the wrapping angle φ was taken in relative eccentricity function λ :

$$p_0 = \frac{\omega\eta}{\psi^2}\ ;\qquad h_1(\varphi,\lambda) = 1 + \lambda\cos\varphi\ ;\qquad \psi = \frac{\varepsilon}{R} \tag{8}$$

where: ω – angular journal velocity,
      ψ – dimensionless radial clearance $(10^{-4} \le \psi \le 10^{-3})$,
      ε – radial clearance,
      R – radius of the journal,
      b – length of the journal

$$\psi = \frac{\varepsilon}{R};\qquad\qquad L_1 = \frac{b}{R} \tag{9}$$

Dimensionless values in equation (6) : hydrodynamic pressure p_1, radial coordinate r_1 , length coordinate of the journal z_1, longitudinal gap height h_1, bearing length L_1 are in form:

$$p = p_0p_1\ ;\ \ r = R(1+\psi r_1)\ ;$$
$$z = bz_1\ ;\ \ \ h = \varepsilon h_1\ ;\ \ b = L_1R \tag{10}$$

$\Phi_1(\Lambda_1,N,h_1)$ function in form (7) when in case of the Newtonian fluid it has a value h_1^3 .

3. Hydrodynamic pressure distribution

Below solutions (6) for infinity length bearing is presented. In this solution the Reynolds boundary conditions, applying to zeroing of pressure at the beginning ($\varphi=0$) and at the end ($\varphi=\varphi_k$) of the oil film and zeroing of the pressure derivative on the wrapping angle at the end of the film

where fulfill. The pressure distribution function in case of the micropolar lubrication $p_1(\varphi)$, of the Newtonian lubrication $p_{1N}(\varphi)$ has a form:

$$p_1(\varphi) = 6\int_0^\varphi \frac{h_1 - h_{1k}}{\Phi_1(\Lambda_1, N, h_1)} d\varphi \; ; \qquad p_{1N}(\varphi) = 6\int_0^\varphi \frac{h_1 - h_{1k}}{h_1^3} d\varphi \qquad (11)$$

where: $h_{1k} = h_1(\varphi_k)$ lubricating gap height at the end of the oil film.

In the boundary case of lubricating Newtonian fluid, pressure distribution function is a pressure $p_{1N}(\varphi)$. Example numerical calculation were made for the infinity length bearing with the relative eccentricity $\lambda = 0,6$.
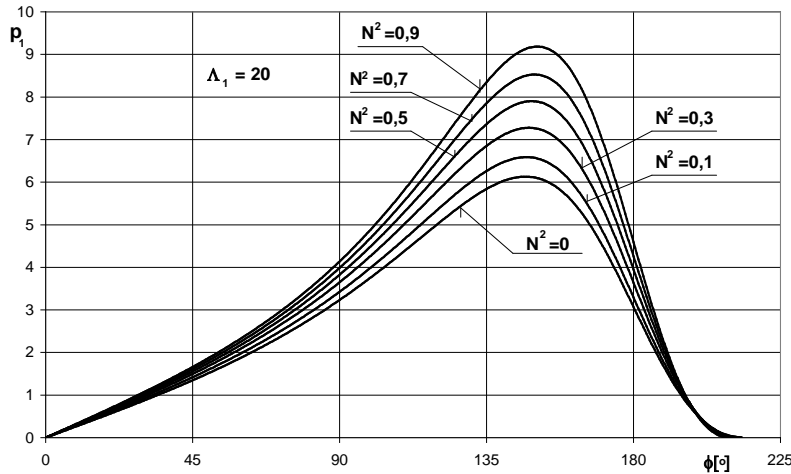

Fig.1 The dimensionless pressure distributions p_1 in direction φ in dependence on coupling number N^2 by micropolar ($N^2 > 0$) and Newtonian ($N^2 = 0$) lubrication for dimensionless eccentricity ratio $\lambda = 0,6$ and characteristic dimensionless length of micropolar fluid $\Lambda_1 = 20$

Analyzing the influence of coupling number N^2 and the influence of dimensionless micropolar length Λ_1 on hydrodynamic pressure distribution in the bearing liner circuital direction. At the Fig.1 pressure distribution for individual coupling numbers at constant micropolar length $\Lambda_1 = 20$. The pressure increase effect is caused by oil dynamic viscosity efficiency increase as a result of coupling viscosity κ. At $N^2 = 0,5$, coupling viscosity is equal to shearing viscosity. Pressure graph in the Fig.1 for micropolar oil lubrication ($N^2 > 0$) find themselves above the pressure graph at the
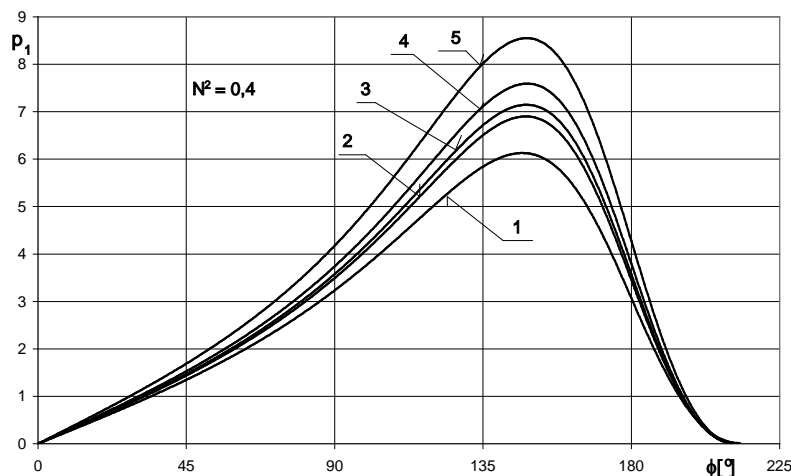

Fig.2 The dimensionless pressure distributions p_1 in direction φ in dependence on characteristic dimensionless length of micropolar fluid Λ_1: 1) Newtonian oil, 2) $\Lambda_1 = 40$, 3) $\Lambda_1 = 30$, 4) $\Lambda_1 = 20$, 5) $\Lambda_1 = 10$, for dimensionless eccentricity ratio $\lambda = 0,6$ and coupling number $N^2 = 0,4$

Newtonian oil lubrication ($N^2=0$). Pressure distribution is higher for higher coupling number. It is caused by oil viscosity dynamic efficiency. In the Fig.2 the course of dimensionless pressure p_1 for few micropolar length quantity Λ_1 is shown. Decrease of this parameter determine the increase of micropolar oil rotational dynamic viscosity. Pressure distribution are presented at the constant coupling number $N^2=0,4$. Rotational viscosity increase determine the pressure distribution increase and is caused, because both the oil flow and microratation velocities are coupled. Quantities of coupling number N^2 and dimensionless micropolar length where taken from works [1,2,3].

4. Capacity forces

Capacity force W for cylindrical slide journal bearing has following components W_x and W_y to be determined [2,5] in the local co-ordinate systems in Fig. 3.
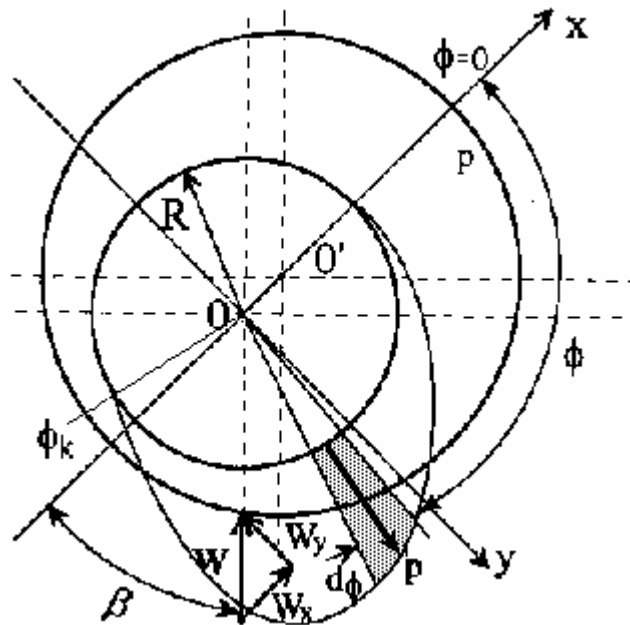

Fig. 3 Capacity force W and components W_x and W_y in the local co-ordinate system

Thus dimensionless components W_{1x} and W_{1y} of capacity forces W_1 are as follows [2]:

$$W_{1x} = \frac{W_x}{W_0} = -\int_0^{\varphi_k} p_1 \cos\varphi d\varphi, \qquad W_{1y} = \frac{W_y}{W_0} = -\int_0^{\varphi_k} p_1 \sin\varphi d\varphi , \qquad (12)$$

$$W_1 \equiv S_o = \sqrt{W_{1x}^2 + W_{1y}^2} = \frac{W}{W_0}$$

where: W_0 - characteristic value of capacity force $W_0 \equiv 2Rbp_0$,
   S_o – Sommerfeld Number for slide journal bearing.

Capacity force is situated in the co-ordinate φ angle φ_{W1}:

$$\varphi_w = \pi - \beta = \pi - \text{arctg}\left|\frac{W_{1y}}{W_{1x}}\right| \qquad (13)$$

Quantities capacity forces W_1 are presented in the Fig.4 in the coupling Number N^2 function for chosen micropolar length Λ_1. All lines are coming out from the maximal pressure point in case of Newtonian fluid flow. We observe maximal capacity force increase when the coupling number N^2 increases (coupling viscosity increases κ) and the micropolar length decreases Λ_1 (rotational viscosity increases γ) . Full range of coupling number change, that covers the range [0;1), apply to coupling viscosity κ change from small to very high quantities. In most of the works, the
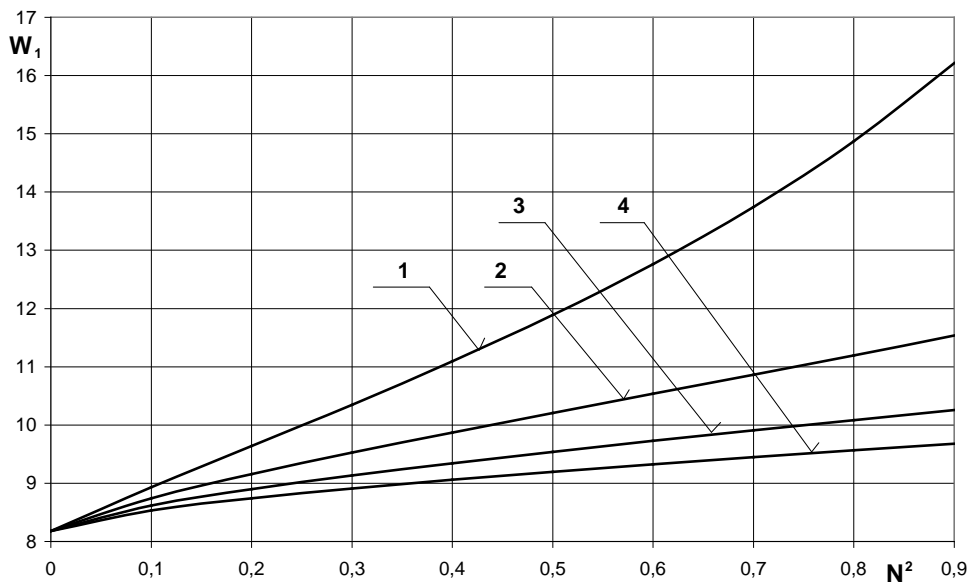

Fig.4 The dimensionless capacity force W_1 in dependence on coupling number N^2 for characteristic dimensionless length of micropolar fluid Λ_1:1) $\Lambda_1=10$, 2) $\Lambda_1=20$, 3) $\Lambda_1=30$, 4) $\Lambda_1=40$

hydrodynamic parameters of the bearing graphs are given in the function, which is Capacity forces courses presented in the Fig.4, can be more suitable for small quantities for parameter κ_1. In the
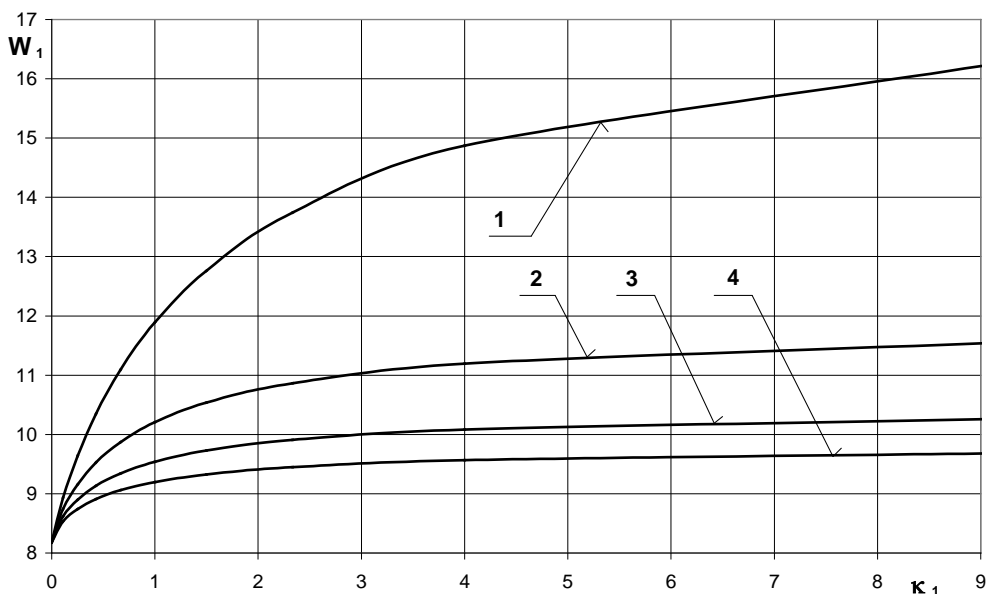

Fig.5 The dimensionless capacity force W_1 in dependence on dimensionless coupling viscosity κ_1 for characteristic dimensionless length of micropolar fluid Λ_1:1) $\Lambda_1=10$, 2) $\Lambda_1=20$, 3) $\Lambda_1=30$, 4) $\Lambda_1=40$

Fig.5 presented capacity forces W_1 courses in the dimensionless micropolar length function Λ_1 for a few coupling number N quantities. Broken line show the capacity force in case of Newtonian oil

lubrication. All lines approach asymptoticly to the broken line when the micropolar length increases (rotational viscosity decreases γ). Together with coupling number increase, maximal
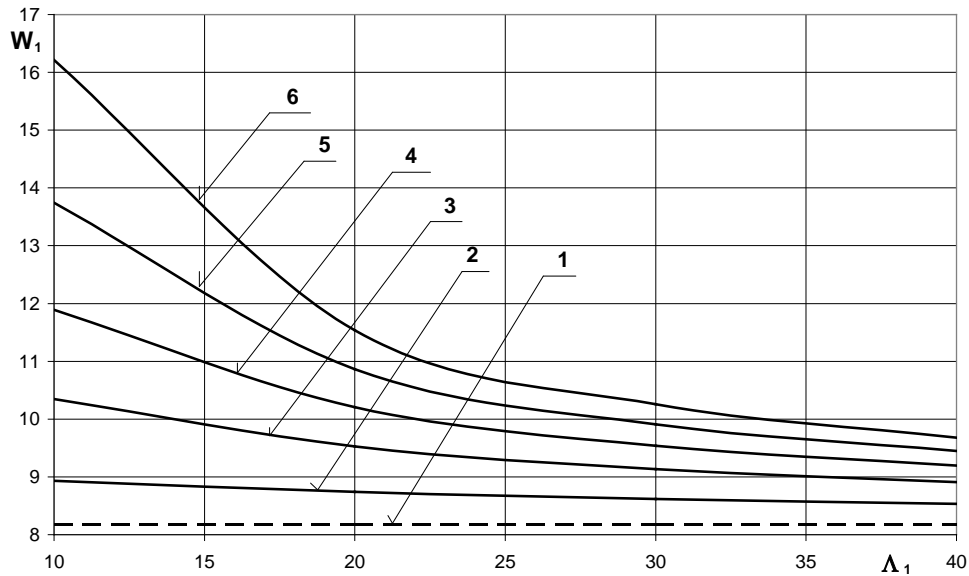

Fig.6 The dimensionless capacity force W_1 in dependence on characteristic dimensionless length of micropolar fluid Λ_1 for coupling number N^2 (---- Newtonian oil)

pressure increases (coupling viscosity increases). Angular coordinate φ_{W1} of capacity force position W_1 in thesquare function of coupling number N^2 for chosen micropolar length Λ_1 were show in the Fig.6. All lines come out from the capacity force position point in case of Newtonian
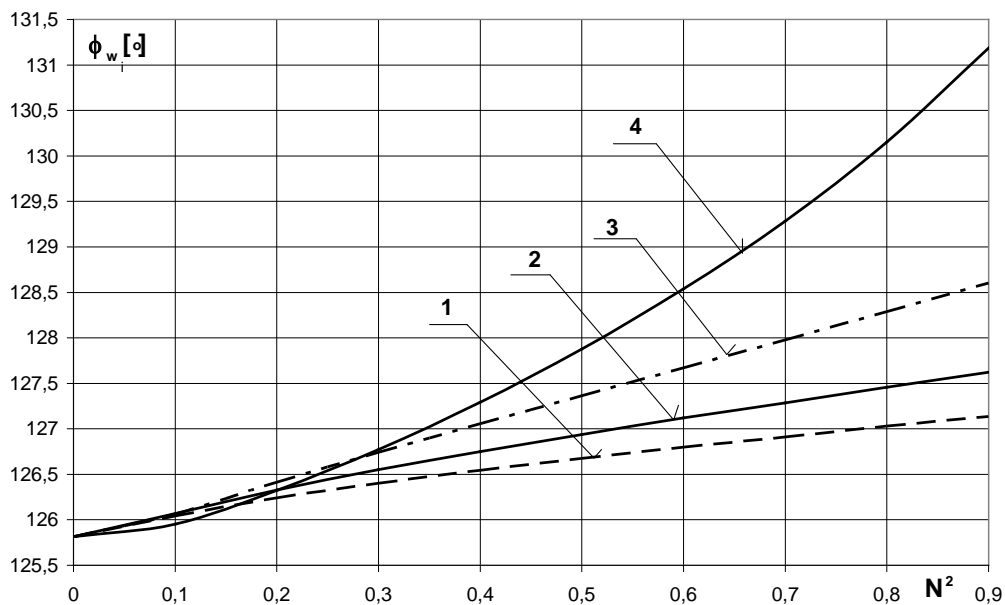

Fig.7 Angle φ_w situated capacity force W_1 in dependence on coupling number N^2 for characteristic dimensionless length of micropolar fluid Λ_1: 1) $\Lambda_1=10$, 2) $\Lambda_1=20$, 3) $\Lambda_1=30$, 4) $\Lambda_1=40$

fluid flow. Increase of capacity force position angle φ_W is observed while the coupling number increases N^2 (coupling viscosity increases κ) and the micropolar length decreases Λ_1 (rotational viscosity increases γ). Graphs in the Fig.6 are described with nonlinear scale of dimensionless coupling viscosity κ_1 change.

5. Conclusions

Presented example of the Reynolds equation solutions for steady laminar non-Newtonian lubricating oil flow with micropolar structure, enable the hydrodynamic pressure distribution introductory estimation as a basic exploitation parameter of slide bearing. Comparing Newtonian oil to oils with micropolar structure, can be used in order to increase hydrodynamic pressure and also to increase capacity load of bearing friction centre. Micropolar fluid usage has two sources of pressure increase in view of viscosity properties: increase of fluid efficient viscosity (coupling viscosity increase) and the rotational viscosity increase (characteristic length parameter Λ). Author realize that he made few simplified assumptions in the above bearing centre model and in the constant parameter characterizing oil viscosity properties. Despite this calculation example apply to bearing with infinity length, received results can be usable in estimation of pressure distribution and of capacity force at laminar, steady lubrication of cylindrical slide bearing with infinity length. Presented results can be usable as a comparison quantities in case of numerical model laminar, unsteady flow Non-Newtonian fluids in the lubricating gaps of crosswise cylindrical slide bearings.

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