

Adsorption of CO₂ by surface modified coal-based activated carbons: kinetic and thermodynamic analysis

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The effects of different surface modifiers on the CO₂ adsorption capacity of coal-based activated carbons were studied, and the diffusion behavior, adsorption kinetics and thermodynamic parameters of CO₂ in activated carbons were analyzed. The results show that compared with ethylene glycol, 1,2-propylenediamine and zinc chloride, potassium hydroxide and sodium hydroxide can greatly improve CO₂ adsorption capacity. The adsorption rate is faster, and the adsorption capacity is larger, with the maximum CO₂ adsorption capacity being 33.54 mL/g. Fick's law can well describe the diffusion behavior of CO₂ in activated carbon. The addition of a surface modifier can increase the diffusion coefficient. The diffusion of CO₂ in activated carbon falls into the category of crystal diffusion. The adsorption kinetics of CO₂ before and after surface modification follow the Bangham equation. During the adsorption process, $\delta H < 0$, $\delta G < 0$, $\delta S < 0$. Surface modification can reduce adsorption heat and promote adsorption, and the adsorption process is dominated by physisorption.

Keywords: Surface modification; CO₂ adsorption capacity; adsorption kinetics; thermodynamic parameters.

INTRODUCTION

Melting snow and glaciers contribute to continuous flow of water into the ocean. Since the start of the 20th century, the sea level has risen at a rate of 1.5–2 mm per year¹. In the past 100 years, the global average temperature has increased by 0.74 °C, making it about 1.1 °C higher than in the pre-industrial period². Global warming is mainly caused by the massive emissions of anthropogenic greenhouse gases such as CO₂, CH₄, and N₂O, of which the contribution rate of CO₂ is as high as 76%³. According to the data released by the Hawaii-based Mauna Loa Observatory in May 2020, CO₂ concentration hit a new high of 415.26 mg/L, the highest so far in human history⁴. Therefore, it is imperative to control the growing CO₂ concentration and reduce the rising global temperature.

In response to the multiple problems caused by CO₂, the 4th International Conference on Greenhouse Gas Control Technology held in 1998 proposed for the first time the use of separation, capture, and transportation, among other methods, to store CO₂⁵. Up to now, CO₂ capture and storage technology (carbon capture and storage, CCS) has become the most effective way to reduce CO₂ emissions in the short term. China's efforts to reduce carbon footprint are subject to economic and technological restraints. To achieve effective CO₂ emission reduction, we must start with CCS by employing existing CO₂ capture facilities⁶. At the core of CCS is CO₂ capture. So far, many CO₂ capture technologies have been developed such as absorption method, membrane separation method, and adsorption method, etc. The absorption method achieves CO₂ separation by taking advantage of the physical solubility of physical adsorbents or the chemical reaction of chemical absorbents. It features simple process flow and mature technology. However, physical absorption entails high operating costs, while chemical absorption causes severe corrosion to facilities⁷. Membrane separation method separates gas mixture by making use of selective permeability of composite membranes. A variety of driving forces are generated on both

sides of the composite membrane to separate or enrich the gas. Permeability and separation coefficient are key indicators of the functionality of composite membranes. Some membranes are not resistant to high temperature or corrosion. Membrane separation method suffers from the disadvantages of huge energy consumption, heavy investment, and immature industrial application⁸. The adsorption method mainly uses solid adsorbents, which can be regenerated by changing temperature and pressure conditions⁹. Adsorption via changing temperature is called temperature swing adsorption¹⁰, while adsorption via changing pressure is called pressure swing adsorption¹¹. Pressure swing adsorption using solid adsorbents has become the most widely used CO₂ capture technology. It has the advantages of good stability, adjustable pore size and less corrosiveness. The use of CO₂ as adsorbent is due to the global problems caused by the greenhouse effect, and is in line with the hot spot in China and the world, namely carbon neutralization.

Commonly used solid adsorbents include fibers¹², ceramic materials and metal oxides¹³, carbonaceous adsorbents¹⁴, molecular sieves¹⁵, etc. Among those solid adsorbents, activated carbon¹⁶ is widely used in industrial fields for adsorption separation, purification and catalysis due to its developed pore structure, large specific surface area, excellent adsorption performance and stable physical and chemical properties. In this study, surface modification of activated carbon was carried out, CO₂ adsorption capacity of activated carbons surface-modified with the optimum concentration was identified, and the adsorption rate was analyzed. Zinc chloride, potassium hydroxide and sodium hydroxide are common chemical reagents for surface modification. Comparing with the common surface modification reagents, the use of ethylene glycol and 1, 2-propylenediamine for surface modification is to explore the modification effect of these two chemical reagents on coal-based activated carbons. The adsorption process and adsorption mechanism of activated carbons before and after surface modification were discussed using the diffusion coefficient, kinetic models and thermodynamic parameters.

This work takes CO₂ as adsorbent and activated carbons as adsorbent. The purpose of this study lies in the application of five chemical reagents on the surface of coal-based activated carbons and carbon dioxide adsorption. Moreover, the advantages and disadvantages of surface modification by chemical reagents are compared. The mechanism of carbon dioxide adsorption was discussed based on the adsorption kinetic model and thermodynamic parameters.

EXPERIMENT

Materials

CO₂ gas (purity ≥ 99.9%, Jinan Deyang Special Gas Co., Ltd.); iodine (analytically pure, Shanghai Macklin Biochemical Technology Co., Ltd.); activated carbon (Tianjin Beichen Founder Reagent Factory); ethylene glycol (analytically pure, Shanghai Macklin Biochemical Technology Co., Ltd.); 1,2-propylenediamine (analytically pure, Shanghai Macklin Biochemical Technology Co., Ltd.); zinc chloride (analytically pure, Shanghai Macklin Biochemical Technology Co., Ltd.); potassium hydroxide (analytically pure, Shanghai Macklin Biochemical Technology Co., Ltd.); sodium hydroxide (analytically pure, Shanghai Macklin Biochemical Technology Co., Ltd.); laboratory-made deionized water.

Determination of CO₂ adsorption capacity of activated carbon

Gravimetric method was chosen to conduct CO₂ adsorption capacity measurement, using a NETZSCH STA409PC thermogravimetric analyzer. Before the test, the samples were dried at 300 °C for 60 min to remove the moisture and residual gas in the activated carbon. Then the activated carbon samples were cooled to 25 °C for the measurement of the CO₂ adsorption capacity of the chestnut shell-based carbon material. The CO₂ flow rate was 60 mL/min. The formula used to calculate CO₂ adsorption amount q_t (mL · g⁻¹) is:

$$q_t = \frac{m_t - m_0}{m_0} \cdot \frac{1}{44} \cdot 100 \quad (1)$$

Where m_t (g) is the mass of the sample at any time of adsorption, m_0 (g) is the mass of the sample at the initial time of adsorption.

Analytical Test Instruments

Electronic analytical balance (FA224TC, Shanghai International Scientific Instrument Co., Ltd.); electric heating blast drying oven (FCHB-C6000, Zhongyi Guoke Beijing Technology Co., Ltd.); collector-type constant temperature heating magnetic stirrer (DF-101S, Shanghai Bangxi Lichen Instruments Technology Co., Ltd.); specific surface area and pore size tester (ASAP 2020 HD88, Mike Instruments, USA); thermal analyzer (STA409PC, Agilent Technologies Co., Ltd.).

Surface modification of activated carbons

The surface modification of activated carbons is carried out as follows:

(1) Accurately weighed 1g of activated carbon was placed in a 100 mL conical flask. Then 50 mL of deionized water was added into the conical flask, which was

subsequently placed in a constant temperature heating magnetic stirrer. The stirring temperature was set at 25 °C. The conical flask was taken out after 3 hours and put in an electric heating blast drying oven. The drying temperature was 120 °C. After drying for 24 h, the surface-modified activated carbon was used to adsorb CO₂. The adsorption temperature was set at 25 °C, and the adsorption pressure was 1.0 MPa. The CO₂ adsorption capacity was determined to be 10.32 mL/g. The sample number was BAC.

(2) Accurately weighed 1g of activated carbon was placed in a 100 mL conical flask. The concentration of ethylene glycol solution was 0.25 mol/L, 0.5 mol/L, 0.75 mol/L, 1.0 mol/L, 2.0 mol/L, 3.0 mol/L, 4.5 mol/L, 6.0 mol/L, respectively, and the volume was 50 mL. The samples were labeled as HA-01, HA-02, HA-03, HA-04, HA-05, HA-06, HA-07 and HA-08, respectively; the stirring temperature was set at 25 °C. After 3 hours, the conical flask was taken out and put into an electric heating blast drying oven. The drying temperature was 120 °C. After drying for 24 hours, it was used to adsorb CO₂. The adsorption temperature was 25 °C, and the adsorption pressure was 1.0 Mpa. The optimum concentration for surface modification is determined by the amount of CO₂ adsorption. The optimum concentration of ethylene glycol for surface modification was 1.0 mol/L, and the corresponding CO₂ adsorption capacity was 14.71 mL/g. The sample was labeled as HA-04.

(3) 1,2-propylenediamine, zinc chloride, potassium hydroxide and sodium hydroxide were used for surface modification, respectively, and the treatment was the same as that in step 2 for each surface modifier. The optimum concentration of 1,2-propylenediamine for surface modification was 1.0 mol/L, the corresponding CO₂ adsorption capacity was 23.88 mL/g, and the sample number was RW-04; the optimum concentration of zinc chloride for surface modification was 1.0 mol/L, the corresponding CO₂ adsorption capacity was 20.34 mL/g, and the sample was labeled as Zn-04; the optimum concentration of potassium hydroxide for surface modification was 2.0 mol/L, the corresponding CO₂ adsorption capacity was 33.52 mL/g, and the sample number was K-05; the optimum concentration of sodium hydroxide for surface modification was 0.75 mol/L, the corresponding CO₂ adsorption capacity was 32.69 mL/g, and the sample was labeled as Na-03.

Characterization of activated carbons

The apparent density of activated carbons was determined in accordance with the national standard GB/T12496.1-1999¹⁷, and the iodine adsorption value was determined in accordance with the national standard GB/T12496.8-2015¹⁸. Surface pore structure parameters of activated carbons were determined with nitrogen as the adsorbate at 77K using a specific surface area and pore size analyzer (ASAP 2020 HD88, Mike Instruments, USA), and the type of nitrogen adsorption/desorption curve was determined¹⁹. The BET equation²⁰ was used to calculate the specific surface area of activated carbon, and the BJH equation²¹ was employed to determine the pore volume and pore size of activated carbons. The physical parameters of the activated carbon materials are shown in Table 1.

Table 1. Physical property parameters of activated carbon materials

Activated carbon	BAC	HA-04	RW-04	Zn-04	K-05	Na-03
Apparent density/ ($\text{g} \cdot \text{mL}^{-1}$)	0.455	0.467	0.477	0.481	0.483	0.479
Particle size/(μm)	75	75	75	75	75	75
Iodine adsorption value / ($\text{mg} \cdot \text{g}^{-1}$)	231	245	262	274	287	289
N_2 adsorption line type	Type II	Type II	Type II	Type II	Type II	Type II
Specific surface area / ($\text{m}^2 \cdot \text{g}^{-1}$)	10.366	6.974	7.323	21.083	7.539	9.907
Pore volume / ($\text{cm}^3 \cdot \text{g}^{-1}$)	0.02969	0.02411	0.02609	0.1272	0.02621	0.02539
Average pore size / (nm)	8.302	15.108	9.864	17.549	8.711	15.808
Median pore size / (nm)	27.058	24.941	23.567	42.551	20.648	18.582

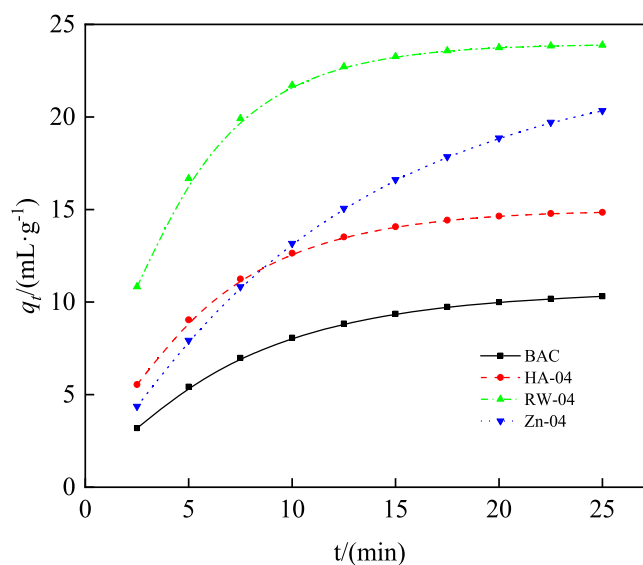
EXPERIMENTAL RESULTS AND DISCUSSION

Analysis of CO_2 adsorption performance of activated carbons

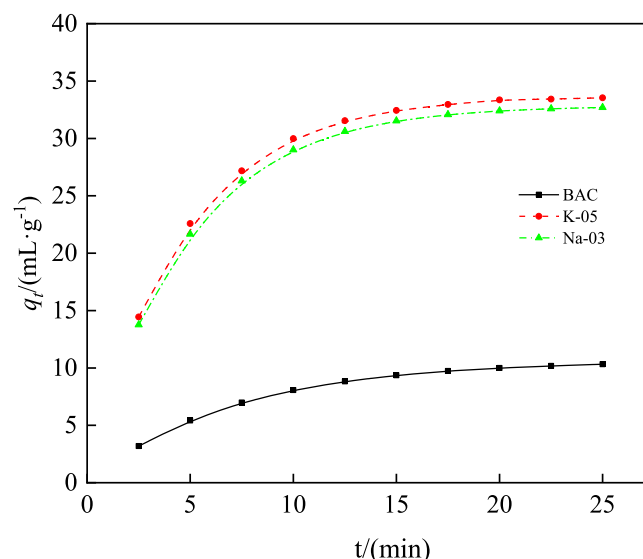
The adsorption temperature was set at 25°C , and the CO_2 flow rate was 60 mL/min . The saturation capacities of activated carbons for CO_2 adsorption were determined. Fig. 1 shows the adsorption process. It can be seen that the adsorption of CO_2 by BAC is a relatively gradual process, that is, no dramatic increase occurred at a certain time point. The adsorption reached saturation around 15 min in a gradual manner, and the adsorption amount changed little after 15 min. The surface modification of ethylene glycol not only enhances the adsorption capacity of activated carbons but also increases the adsorption efficiency. HA-04 gradually reached adsorption equilibrium around 10 minutes. Compared with ethylene glycol, 1, 2-propylenediamine can improve the adsorption efficiency greatly. During the entire adsorption process, the adsorption amount of RW-04 increased steadily, which indicates that the adsorption of RW-04 for CO_2 may involve a certain degree of chemical adsorption²². In this case, the adsorption was affected by the surface chemical bonds, resulting in a continuous adsorption process. Zn-0, K-05 and Na-03 exhibit similar adsorption processes. To be specific, the adsorption capacity increased rapidly within 7.5 min, adsorption basically reached saturation within 10 min, and there was no marked change after 10 min. Therefore, the adsorption of Zn-04, K-05 and Na-03 fall into the category of physical adsorption²³ and is mainly affected by the van der Waals force, that is, directional force, inductive force and dispersion force. The adsorbed CO_2 molecules were prone to desorption. Desorption and adsorption reached equilibrium within a very short time range, which means the amount of CO_2 adsorption reached saturation within a short period of time and then stabilized over time.

CO_2 diffusion coefficient

Adsorption is defined as follows: the surface of activated carbons spontaneously uses its unsaturated free valence at a certain temperature to capture the molecules in the adsorbed phase, reducing the surface Gibbs free energy of molecules by concentrating them on the phase interface. The indicators for evaluating the adsorption performance of activated carbons are adsorption capacity and adsorption speed. The adsorption capacity is measured by the amount of CO_2 adsorption, while the



(a) BAC, HA-04, RW-04, Zn-04



(b) BAC, K-05, Na-03

Figure 1. Saturation process of CO_2 adsorption by activated carbons

adsorption speed is determined by the amount of CO_2 adsorption per unit mass of activated carbon per unit time. The adsorption process can be divided into three stages: (1) the external diffusion stage of the particles when the adsorbate diffuses from the adsorbed phase to the surface of the adsorbent; (2) the pore diffusion stage when the adsorbate continues to diffuse to the adsorption

site through the adsorbent pores; (3) adsorption reaction stage when the adsorbate is adsorbed on the surface of adsorption sites within the pores of the adsorbent. Among the three stages, adsorption reaction is completed in a very short time; therefore, the adsorption speed is mainly determined by the speed of external diffusion and pore diffusion. The diffusion behavior of adsorbate molecules inside the adsorbent is described by Fick's second law²⁴. The adsorption kinetic curve can generally be divided into fast adsorption in the initial stage of adsorption and slow adsorption in the stable adsorption stage. Due to the instability of the system in the initial stage, the kinetic equation for slow adsorption is suitable for the calculation of the diffusion coefficient.

Assuming that activated carbon consists of homogeneous particles, that the adsorbate concentration on the particle surface is constant, and that the temperature of the entire adsorption system is constant, then for the slow adsorption stage ($q_t/q_\infty > 0.5$) we get:

$$\frac{q_t}{q_\infty} = 1 - \frac{6}{\Pi^2} \exp\left(-\frac{D\Pi^2 t}{r^2}\right) \quad (2)$$

Where q_∞ ($\text{mL} \cdot \text{g}^{-1}$) is the saturated adsorption capacity, D ($\text{m}^2 \cdot \text{s}^{-1}$) is the diffusion coefficient, t (min) is the adsorption time, and r (m) is the average particle radius.

Taking the natural logarithm of equation (2) gives:

$$-\ln\left(1 - \frac{q_t}{q_\infty}\right) = \frac{D\Pi^2}{r^2} t - \ln \frac{6}{\Pi^2} \quad (3)$$

In formula (3), the dependent variable and the independent variable are $-\ln(1 - q_t/q_\infty)$ and t respectively; then the value of $D\Pi^2/r^2$ can be obtained by linear regression within the range of $q_t/q_\infty > 0.5$, and the value of diffusion coefficient D can be obtained. Based on formula (3), a linear regression was performed on the change curve of CO_2 adsorption amount relative to time in Fig. 1, and the results are shown in Table 2. It can be seen that surface modification increases the diffusion coefficient. Generally, the diffusion of molecules within porous media can be classified into four categories: free diffusion ($D: 10^{-5} \sim 10^{-4}$), Kundsens diffusion ($D: 10^{-7} \sim 10^{-6}$), surface diffusion ($D < 10^{-7}$) and crystal diffusion ($D < 10^{-9}$). According to Table 2, the diffusion of CO_2 within activated carbons before and after surface modification belong to crystal diffusion.

Table 2. Diffusion coefficient of CO_2 in activated carbons

Activated carbon	$D/(\text{m}^2 \cdot \text{s}^{-1})$	R^2
BAC	$3.963 \cdot 10^{-10}$	0.991
HA-04	$4.218 \cdot 10^{-10}$	0.993
RW-04	$4.878 \cdot 10^{-10}$	0.992
Zn-04	$4.674 \cdot 10^{-10}$	0.994
K-05	$5.689 \cdot 10^{-10}$	0.995
Na-03	$5.311 \cdot 10^{-10}$	0.991

Table 3. Fitting parameters of CO_2 adsorption using the quasi-first-order kinetic model

Quasi-first-order kinetic model	BAC	HA-04	RW-04	Zn-04	K-05	Na-03
$q_{e,exp}/(\text{mL} \cdot \text{g}^{-1})$	10.317	14.850	23.885	20.351	33.543	32.698
$q_{e,cal}/(\text{mL} \cdot \text{g}^{-1})$	10.606	15.015	23.936	23.231	32.658	32.828
K_1	0.143	0.184	0.239	0.084	0.221	0.216
R^2	0.999	0.999	0.999	0.999	0.999	0.999

Kinetic analysis of CO_2 adsorption on activated carbons

The quasi-first-order kinetic model, the quasi-second-order kinetic model, the intra-particle diffusion model, the Elovich kinetic model and the Bangham kinetic model are the most widely used kinetic models in the investigation of adsorption kinetics. Among them, the quasi-first-order kinetic model and the Bangham model are used to clarify whether the adsorption process is physical adsorption. And, the quasi-second-order kinetic model is used to indicate whether the adsorption process is chemical adsorption, the intra-particle diffusion model is used to judge the location of physical adsorption. Moreover, the Elovich model is used to judge the reaction between adsorbent and adsorbent.

Quasi-first-order kinetic model

The quasi-first-order kinetic model²⁵ is based on the membrane diffusion theory, which assumes that the adsorption is subject to the diffusion stages and that the adsorption reaction rate of the adsorbate is positively proportional to the first power of the difference between the values of equilibrium adsorption capacity and the actual adsorption capacity in the system. The adsorption rate can be calculated using the Lagergren equation:

$$\frac{dq_t}{dt} = K_1(q_e - q_t) \quad (4)$$

Applying the boundary conditions $t = 0$ to $t = t$ and the corresponding values $q_t = 0$ to $q_t = q_t$ to equation (4) for integration, we can obtain:

$$q_t = q_e - q_e e^{-K_1 t} \quad (5)$$

Where q_t ($\text{mL} \cdot \text{g}^{-1}$) is the adsorption amount of CO_2 at time t , q_e ($\text{mL} \cdot \text{g}^{-1}$) is the adsorption amount of CO_2 at equilibrium, t (min) is the adsorption time, and K_1 (min^{-1}) is quasi-first-order adsorption rate constant.

The fitting parameters of CO_2 adsorption on activated carbon using the quasi-first-order kinetic model are shown in Table 3, and the curve fitting is shown in Fig.2.

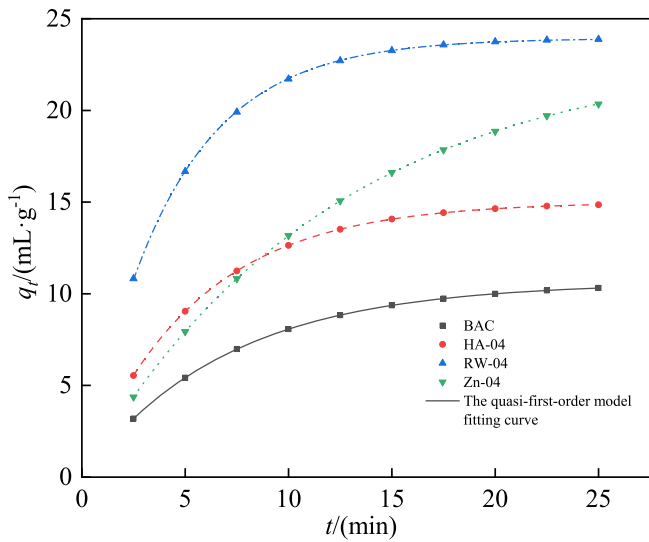
Quasi-second-order kinetic model

The quasi-second-order kinetic model²⁶ assumes that the adsorption rate is determined by the square of the number of unoccupied adsorption vacancies on the adsorbent surface and that the adsorption process is subject to chemisorption mechanism, which involves the sharing or transfer of electrons between adsorbents and adsorbates. The equation is:

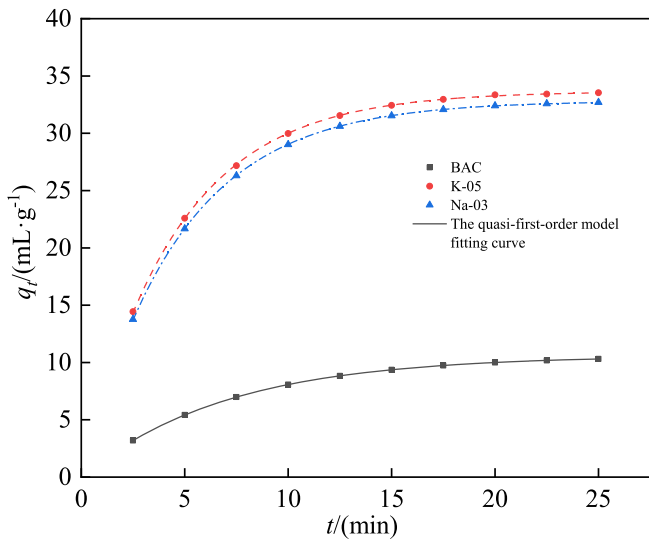
$$\frac{dq_t}{dt} = K_2(q_e - q_t)^2 \quad (6)$$

Applying the boundary conditions $t = 0$ to $t = t$ and the corresponding values $q_t = 0$ to $q_t = q_t$ to integrate equation (6), we get:

$$\left(\frac{t}{q_t}\right) = \frac{1}{K_2 q_e^2} + \frac{t}{q_t} \quad (7)$$



(a) BAC, HA-04, RW-04, Zn-04



(b) BAC, K-05, Na-03

Figure 2. Curve fitting of CO₂ adsorption by activated carbons using the quasi-first-order kinetic model

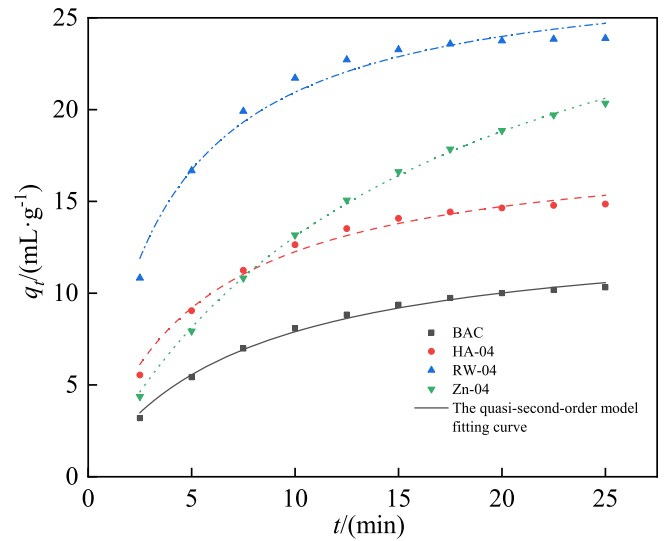
Rearranging formula (7), we get:

$$q_t = \frac{K_2 q_e^2 t}{1 + K_2 q_e t} \quad (8)$$

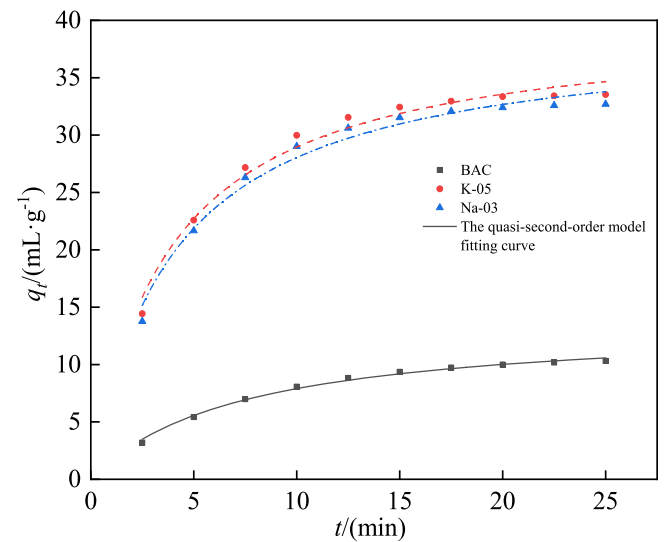
Where q_t (mL · g⁻¹) is the CO₂ adsorption amount at time t , q_e (mL · g⁻¹) is the CO₂ adsorption amount when the adsorption reaches equilibrium, t (min) is the adsorption time, and K_2 (mL · g⁻¹ · min⁻¹) is quasi-second order adsorption rate constant. The initial adsorption rate can be calculated using the quasi-second-order adsorption rate constant, and the calculation formula is as follows:

$$h = K_2 q_e^2 \quad (9)$$

Table 4 shows the fitting parameters of CO₂ adsorption by activated carbon using the quasi-second-order kinetic model, and the curve fitting is shown in Fig. 3.



(a) BAC, HA-04, RW-04, Zn-04



(b) BAC, K-05, Na-03

Figure 3. Curve fitting of CO₂ adsorption by activated carbons using the quasi-second-order model

Intra-particle diffusion model

The intra-particle diffusion model²⁷ assumes the following conditions: (1) the diffusion resistance of the adsorption contact surface is negligible or the diffusion resistance only works for a short time in the initial stage of adsorption; (2) the diffusion direction is random, and the adsorbate concentration is independent of the particle position; (3) the internal diffusion coefficient is constant and does not change with the adsorption time

Table 4. Fitting parameters of CO₂ adsorption using the quasi-second-order kinetic model

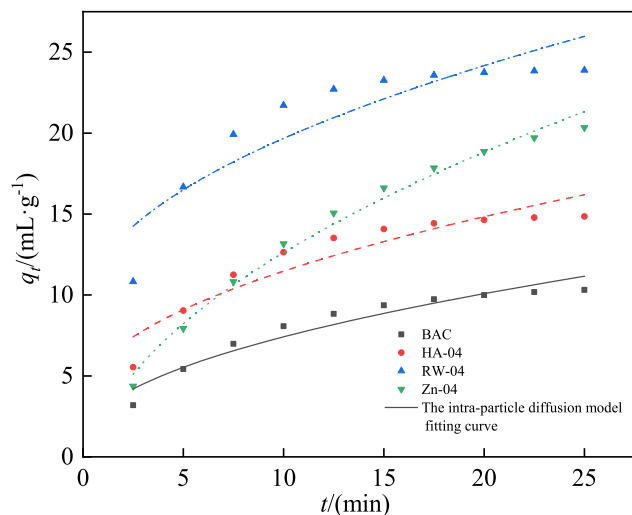
Quasi-Second-Order Dynamics Model	BAC	HA-04	RW-04	Zn-04	K-05	Na-03
$q_{e,exp}$ (mL · g ⁻¹)	10.317	14.850	23.885	20.351	33.533	32.698
$q_{e,cal}$ (mL · g ⁻¹)	13.6537	18.408	28.023	33.482	39.925	39.123
K_2	0.011	0.011	0.011	0.001	0.006	0.006
h (mL · min ⁻¹)	2.052	3.727	8.638	1.121	9.564	9.183
R^2	0.994	0.987	0.977	0.998	0.981	0.982

and adsorption position. Therefore, the intraparticle diffusion model is a kinetic model that studies the rate limit of adsorption. Its calculation formula is:

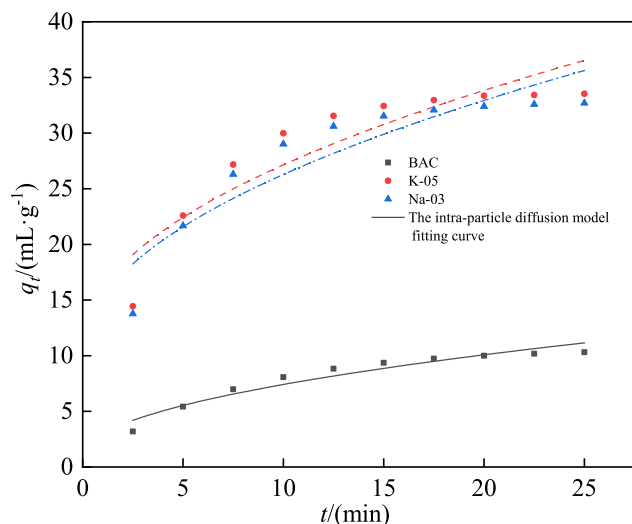
$$q_t = K_{dif}t^{1/2} + C \quad (10)$$

Where q_t ($\text{mL} \cdot \text{g}^{-1}$) is the amount of CO_2 adsorption at time t , C is the intercept constant, t (min) is the adsorption time, and K_{dif} ($\text{mL} \cdot \text{g}^{-1} \cdot \text{min}^{-1/2}$) is the intraparticle diffusion rate constant

The parameters related to the fitting of CO_2 adsorption by activated carbon using the intra-particle diffusion model are shown in Table 5, and the curve fitting is shown in Fig.4.



(a) BAC, HA-04, RW-04, Zn-04



(b) BAC, K-05, Na-03

Figure 4. The intra-particle diffusion model fitting curve of CO_2 adsorption by activated carbons

Table 5. Fitting parameters of CO_2 adsorption using the intra-particle diffusion model

Intraparticle diffusion model	BAC	HA-04	RW-04	Zn-04	K-05	Na-03
K_{dif}	2.035	2.569	3.432	4.745	5.104	5.078
C	0.982	3.346	8.824	-2.385	11.009	10.225
R^2	0.934	0.883	0.818	0.987	0.839	0.846

Table 6. Fitting parameters of CO_2 adsorption using the Elovich kinetic model

Elovich kinetic model	BAC	HA-04	RW-04	Zn-04	K-05	Na-03
α	3.678	7.565	21.296	4.701	24.889	22.749
β	0.313	0.243	0.179	0.138	0.121	0.122
R^2	0.989	0.966	0.927	0.993	0.941	0.944

Elovich kinetic model

The Elovich kinetic model²⁸ is used to analyze the adsorption behavior of adsorbates on the surface of heterogeneous solid adsorbents. Although this model does not make any explicit assumptions for the interaction mechanism between adsorbates and adsorbents, it can describe the kinetics of chemical adsorption. The Elovich kinetic model can reveal the irregular shape of data ignored by other kinetic models and is suitable for adsorption reaction processes with large activation energy. It can be expressed as:

$$\frac{dq_t}{dt} = \alpha \exp(-\beta q_t) \quad (11)$$

Assuming $\alpha\beta \gg t$ for formula (11), using boundary conditions $t=0$, $t=t$, and its corresponding values $q_t=0$, $q_t=q_t$, the above formula can be rearranged as:

$$q_t = \frac{1}{\beta} \ln(\alpha\beta) + \frac{1}{\beta} \ln(t) \quad (12)$$

Where q_t ($\text{mL} \cdot \text{g}^{-1}$) is the amount of CO_2 adsorption at time t , t (min) is the adsorption time, α ($\text{mL} \cdot \text{g}^{-1} \cdot \text{min}^{-1}$) is the initial rate constant, and β ($\text{g} \cdot \text{mL}^{-1}$) is the desorption rate constant.

The fitting parameters of CO_2 adsorption by activated carbon using the Elovich kinetic model are shown in Table 6, and the curve fitting is shown in Fig. 5.

Bangham kinetic model

The Bangham formula²⁹ can be written in the following form:

$$\frac{dq_t}{dt} = K_B(q_e - q_t)^2 \quad (13)$$

Using the boundary conditions $t = 0$, $t = t$ and its corresponding values $q_t = 0$, $q_t = q_t$ to integrate the formula, we get:

$$\ln\left(\frac{q_e}{q_e - q_t}\right) = K_B t^2 \quad (14)$$

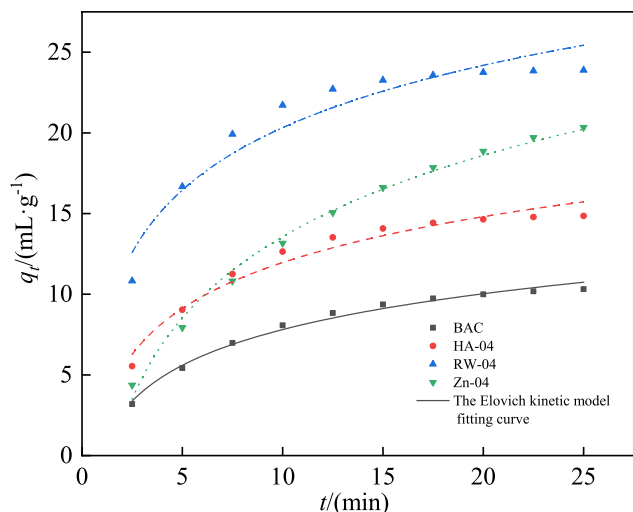
Equation (14) can be rearranged into the following linear form:

$$q_t = q_e - q_e e^{-K_B t^2} \quad (15)$$

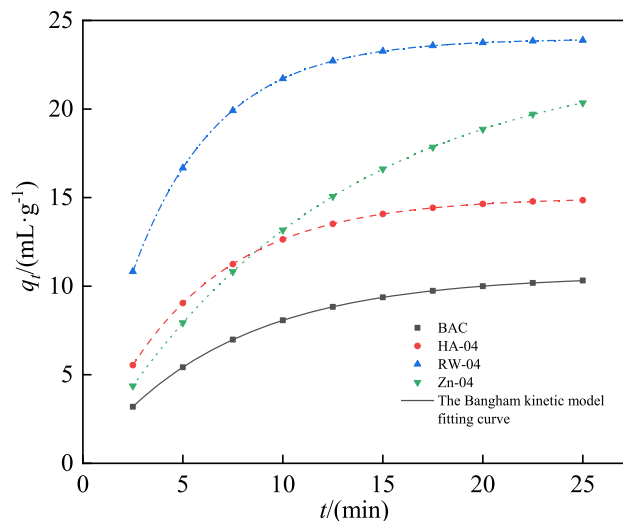
Where q_t ($\text{mL} \cdot \text{g}^{-1}$) is the CO_2 adsorption amount at time t , q_e ($\text{mL} \cdot \text{g}^{-1}$) is the CO_2 adsorption amount when the adsorption reaches equilibrium, and t (min) is the adsorption time, and K_B and Z are constants.

Table 7 shows the fitting parameters of CO_2 adsorption by activated carbon using the Bangham kinetic model, and the curve fitting is shown in Fig. 6.

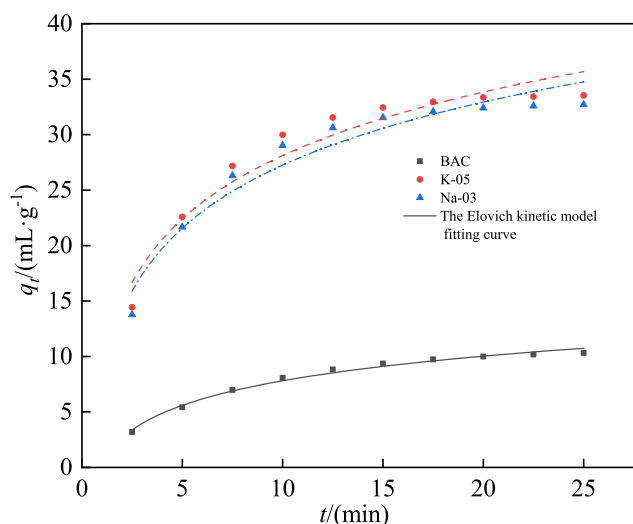
The quasi-first-order kinetic model, the quasi-second-order kinetic model, the intra-particle diffusion model,



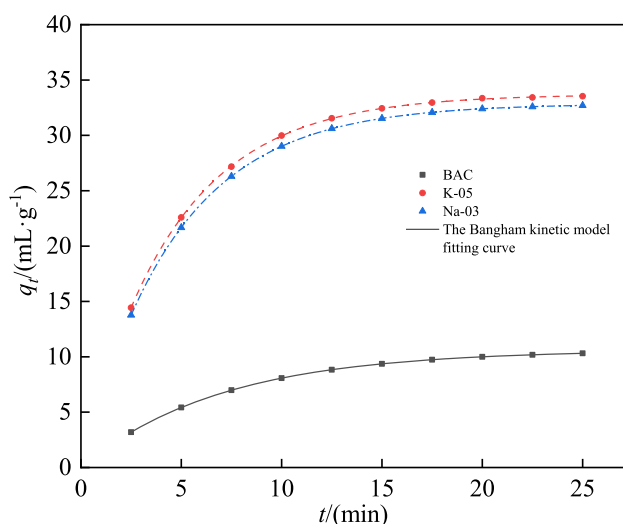
(a) BAC, HA-04, RW-04, Zn-04



(a) BAC, HA-04, RW-04, Zn-04



(b) BAC, K-05, Na-03



(b) BAC, K-05, Na-03

Figure 5. Curve fitting of CO₂ adsorption by activated carbons using the Elovich kinetic model

Figure 6. Curve fitting of CO₂ adsorption by activated carbons using the Bangham kinetic model

the Elovich kinetic model and the Bangham kinetic model were used to investigate the variation of adsorption capacity along with time. The fitting adaptability of these five kinetic models can be evaluated by fitting correlation coefficient R^2 . With respect to the best fit (R^2), the order was: the Bangham kinetic model > the quasi-first-order kinetic model > the Elovich kinetic model > the quasi-second-order kinetic model > the intra-particle diffusion model. From fitting correlation coefficient R^2 , it can be seen that the experimental data were best described by the Bangham model, which reveals that there is a linear relationship between the carbon dioxide adsorption capacity and the adsorption pressure. Therefore, the linear relationship indicated that

the adsorption process is dominated by physisorption. Moreover, the quasi-second-order kinetic model is not suitable for describing the adsorption process. The result indicated that the CO₂ adsorption is not built on the basis of chemical adsorption.

Thermodynamic analysis of activated carbons adsorption of CO₂

Isosteric heat analysis

The heat of adsorption refers to the thermal effect produced in the adsorption process. During adsorption, the gas molecules move onto the surface of the adsorbent and their molecular motion is greatly reduced, resulting

Table 7. Fitting parameters of CO₂ adsorption using the Bangham kinetic model

Bangham kinetic model	BAC	HA-04	RW-04	Zn-04	K-05	Na-03
$q_{e,exp}$ (mL·g ⁻¹)	10.317	14.850	23.885	20.351	33.543	32.698
$q_{e,cal}$ (mL·g ⁻¹)	10.069	15.011	23.966	21.164	33.719	32.866
K_B	0.143	0.184	0.243	0.833	0.226	0.219
Z	0.999	1.001	0.988	1.004	0.986	0.991
R^2	1	1	1	1	0.999	1

in heat release. Isotheric heat of adsorption³⁰ refers to the enthalpy change of adsorbing 1 mol of gas when the adsorption temperature, adsorption pressure, and adsorbent surface area are constant. It can reflect in an indirect manner the adsorption strength, the inhomogeneity of the adsorbent surface, and the type of adsorption. Isotheric heat of adsorption is usually calculated using the Clausius-Clapeyron equation:

$$\frac{1}{P} \frac{dP}{dT} = \frac{q_{\text{est}}}{RT^2} \quad (16)$$

Rewriting and integrating give:

$$\ln P = -\frac{q_{\text{est}}}{RT} + C \quad (17)$$

Where q_{est} (KJ mol⁻¹) is the isotheric heat of adsorption (a value equal to the enthalpy change ΔH during the adsorption process), R (J · mol⁻¹ · K⁻¹) is the ideal gas constant, T (K) is the adsorption temperature, P (Pa) is the adsorption equilibrium pressure, and C is constant. The isotheric adsorption heat q_{est} for CO₂ adsorption by activated carbon is shown in Table 8.

It can be seen from Table 8 that the chemical reagents can reduce the adsorption heat during the adsorption process, which indicates that the chemical reagents are helpful carbon dioxide molecules entering the interior of coal-based activated carbon more easily. Based on the specific numerical value of isotheric heat of adsorption, the equal heat of adsorption is less than 40 KJ/mol. It indicated that the adsorption process is physical adsorption. And, potassium hydroxide shows the best modification effect.

Adsorption free energy analysis

Free energy refers to the part of internal energy that is reduced within the system that can be converted into work during a thermodynamic process. The Gibbs free energy in the adsorption process³¹ refers to the increase of the free energy of the system with the increase of the unit area of the adsorbent under constant temperature and pressure. The adsorption free energy ΔG can be used to determine the adsorption mechanism, and its formula is:

$$\Delta G = -RT \ln K_d \quad (18)$$

Where ΔG (KJ · mol⁻¹) is the Gibbs free energy change of adsorption, R (J · mol⁻¹ · K⁻¹) is the ideal gas constant, T (K) is the adsorption temperature, and K_d is the adsorption thermodynamics equilibrium constant.

In our study, K_d is calculated using the fitting parameters of the Freundlich equation, that is, $K_d = K_{\text{fn}}$. The Freundlich equation is:

$$q_e = K_{\text{fn}} P^{\frac{1}{n_{\text{fn}}}} \quad (19)$$

Table 8 shows the adsorption thermodynamic equilibrium constant K_{fn} and adsorption free energy ΔG of activated carbon for CO₂ adsorption.

In Table 8, it can be judged that the addition of chemical reagents lead to the increase of the adsorption free energy of carbon dioxide during the adsorption process. Generally, the adsorption free energy of chemical adsorption than of physical adsorption, which indicates that the addition of chemical reagents lead to the change of structure of coal-based activated carbon. Consequently, the capacity of chemical adsorption of coal-based activated carbon increases. However, physical adsorption plays a dominant role.

Adsorption entropy analysis

Entropy is a measure of the degree of rearrangement or disorder of a thermodynamic system. Adsorption entropy ΔS ³² refers to the change in the entropy of the adsorbate during the adsorption process. Reflecting the interaction between the adsorbate and the adsorbent, adsorption entropy ΔS can be used to understand the movement or arrangement of the adsorbate molecules on the surface of the adsorbent. The adsorption entropy ΔS can be calculated using the Gibbs-Helmholtz equation:

$$\Delta S = \frac{\Delta H - \Delta G}{T} \quad (20)$$

Where ΔS (J · mol⁻¹ · K⁻¹) is the adsorption entropy, ΔH (KJ · mol⁻¹) is the adsorption enthalpy change, ΔG (KJ · mol⁻¹) is the Gibbs free energy change of adsorption, and T (K) is the adsorption temperature. The adsorption entropy ΔS of activated carbon for CO₂ adsorption is shown in Table 8.

From Table 8, it can be concluded that the modification of chemical reagents leads to the reduction of adsorption entropy in the process of carbon dioxide adsorption, which indicated that the addition of chemical reagents is beneficial to promoting the carbon dioxide molecules into the coal-based activated carbon. The chaos degree of carbon dioxide molecules in coal-based activated carbons was reduced. So, more carbon dioxide molecules can be stored in coal-based activated carbons.

Table 8. Thermodynamic parameters of CO₂ adsorption by activated carbons

Thermodynamic parameters	BAC	HA-04	RW-04	Zn-04	K-05	Na-03
$q_{\text{est}}(\text{KJ} \cdot \text{mol}^{-1})$	-34.221	-29.257	-18.154	-23.569	-13.784	-14.412
K_{fn}	10.422	15.263	24.508	21.004	34.641	33.373
$\Delta G(\text{KJ} \cdot \text{mol}^{-1})$	-5.087	-6.752	-7.879	-7.543	-6.499	-6.611
$\Delta S(\text{J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1})$	-97.716	-75.482	-34.463	-53.751	-24.434	-26.165

Table 9. Comparison with CO₂ adsorbents from other studies

CO ₂ adsorbents	CO ₂ adsorption capacity	Modified chemical reagent	Citing paper
Activated carbon	33.54 mL/g	KOH	This paper
Sawdust	4.25 mmol/g	KOH	Jin et al. ³²
Silica	164 mg/g	Non-modified reagent	Jiao et al. ³³
Nitride/HKUST-1 Hybrid Materials	163 cm ³ /g	Non-modified reagent	Jia et al. ³⁴
Zeolite	1.48 mmol/g	Non-modified reagent	Pham et al. ³⁵
Activated carbon fibers	250 mg/g	KOH	Lee et al. ³⁶

Comparison with CO₂ adsorbents from other studies

According to the comparison of CO₂ adsorption capacity in Table 9, it can be seen that surface modification of activated carbon by KOH in this paper can obtain a large CO₂ adsorption capacity, which indicates that modification of activated carbon by KOH can effectively promote the adsorption of CO₂ by activated carbon.

CONCLUSION

(1) Fick's law can well describe the diffusion behavior of CO₂ in activated carbons before and after surface modification. The diffusion of CO₂ in activated carbons belongs to crystal diffusion. Surface modification can increase the diffusion coefficient, which means that surface modification will make it easier for CO₂ molecules to enter the activated carbons.

(2) The Bangham kinetic model has the highest fitting degree. The correlation coefficient R² obtained through Bangham kinetic model fitting was higher than 0.99, and the expected value q_e calculated from the Bangham kinetic model was fairly close to the experimental value of q_e. Those results show that the Bangham kinetic model can describe the adsorption kinetics of CO₂ on activated carbons very well.

(3) From the adsorption curve of activated carbons before and after surface modification, it can be concluded that the adsorption amount increased rapidly in the initial stage of adsorption, which indicates that the adsorption of CO₂ by activated carbons mainly occurs in the monolayer outer surface and that surface modification increases the adsorption rate of activated carbons in the initial stage.

(4) The isosteric adsorption heat q_{est} was less than 40KJ · mol⁻¹, which indicates that the adsorption of CO₂ by activated carbons is physical adsorption and that the adsorption force in play is van der Waals force. Surface modification reduced the isosteric adsorption heat q_{est}, resulting in easier adsorption. The adsorption free energy ΔG increased, which indicates that the kinetic energy of the adsorbed gas increased. The adsorption entropy ΔS decreased, which indicates that the surface modification reduces the degree of freedom of the adsorbed CO₂ molecules, contributing to more orderly adsorption on the surface of the activated carbons.

SYMBOL DESCRIPTION

D – Diffusion coefficient, m² · s⁻¹
 h – Initial adsorption rate, mL · min⁻¹
 K_1 – The quasi-first-order adsorption rate constant, min⁻¹
 K_2 – The quasi-second-order adsorption rate constant, mL · g⁻¹ · min⁻¹
 K_B – Bangham kinetic model constants
 K_d – Adsorption thermodynamic equilibrium constant
 K_{dif} – Intraparticle diffusion rate constant, mL · g⁻¹ · min^{-1/2}
 K_{fn} – Freundlich isotherm constant
 m_p, m_0 – the weights of activated carbon before and after CO₂ adsorption, respectively, g
 P – Adsorption equilibrium pressure, Pa
 R – Universal Gas Constant, J · mol⁻¹ · K⁻¹
 R^2 – Fitting correlation coefficient

r – Average radius of activated carbon particles, m
 T – Adsorption temperature, K
 $q_e, q_{e,cab}, q_{e,exp}, q_p, q_\infty$ – Respectively, the adsorption amount of CO₂ when the equilibrium is reached, the theoretically calculated adsorption amount of CO₂, the experimentally measured adsorption amount of CO₂, the adsorption amount of CO₂ at any time, and the saturated adsorption amount of CO₂, mL · g⁻¹
 q_{est} – Isosteric heat of adsorption, KJ · mol⁻¹
 Z – Bangham kinetic model constants
 α – Elovich kinetic model initial rate constant, mL · g⁻¹ · min⁻¹
 β – Elovich kinetic model desorption rate constant, g · mL⁻¹
 ΔG – Adsorption Gibbs free energy change, KJ · mol⁻¹
 ΔH – The enthalpy change during the adsorption process, KJ · mol⁻¹
 ΔS – The entropy change during the adsorption process, J · mol⁻¹ · K⁻¹

Subscript

t – Any time of adsorption
 0 – Initial time of adsorption

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