

A novel approach for calculating packed column height based on new correlation of mass transfer coefficient

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The calculation of column's height plays an important role in packed columns precise design. This research is based on experimentally measurement of mass transfer coefficients in different heights of packed column to predict its height. The objective of presented work is to introduce a novel conceptual method to predict column height via new correlation for mass transfer coefficient. As the mass transfer coefficient is decreased with increase of column height, the HTU's are not constant figures along the column so this new approach is called increasing HTU's. The results of the proposed idea were compared with other correlations and the conventional method i.e. constant HTU's. Since the results are in very good agreement with experimental data comparing to conventional method, it seems this approach can be a turning point in design of all differential columns like packed columns. Making use of this method is suggested for design of differential columns.

Keywords: separation, liquid-liquid extraction, packed column, mass transfer, column design, diffusion.

INTRODUCTION

The liquid-liquid extraction is one of the most widely used unit operations in the process industry. The operation consists of separating one or several substances (solute) present in a liquid phase by the addition of another liquid phase in which these substances are transferred preferentially. The mass transfer process underlined the extraction often happens in counter-current type contactors. These contactors are generally classified into two groups, namely stage-wise and differential.

One of the major challenges in designing an industrial extraction column lies in the choice of the geometrical parameters specially height of the column. In order to design or scale up an extraction column, having a reasonable prediction of the mass transfer behaviors by a suitable mathematical model is essential. Furthermore, all previously proposed correlations for prediction of mass transfer coefficient in the extraction columns are independent of column height and would not provide reliable estimation when the mass transfer coefficient is a function of column height, In order to tackle with this deficiency, in a previous work the column height was introduced as a new parameter in the mass transfer coefficient equation which lead to a correlation with a high accuracy without which the data could not be fitted with an acceptable error¹. The possibility of finding a similar correlation in counter-current mode (which shows dependency of mass transfer on height of column) is investigated in the present work. This experimental study confirms that a similar correlation for prediction of mass transfer coefficient can be obtained for counter-current operation with an acceptable average errors comparing to existing correlations. According to this new correlation, as the mass transfer coefficient is decreased with increase of column height, the HTU's are not constant figures along the column so this new approach is called *increasing HTU's*. With this new idea, increasing *HTU's*, the height of transfer unit (HTU), the height equivalent to a theoretical tray or plate, is not a constant value in the column. So this concept can introduce a novel approach in differential column design.

Therefore understanding of relevant column height and the mass transfer coefficients in these columns is of paramount importance for the precise design. Since one phase is dispersed in the other phase the explanation of mass transfer behavior in droplets is necessary for designing the extraction process.

Three important theoretical equations for prediction of the mass transfer coefficient are reviewed briefly. Also many other correlations have been proposed yet². A similar job has been done on this extraction column for single drop system previously¹. In this research we are trying to obtain an equivalent equation for counter-current conditions which considers the effect of height in correlation. Then a new mathematical method is applied to calculate height of packed column. The aim of this study is to introduce a novel conceptual method to predict column height via the new correlation for mass transfer coefficient. This method shows that the HTU is not a fixed value in column. This is a new and useful idea for more precise design of column.

PREDICTION OF MASS TRANSFER COEFFICIENT

The mass transfer coefficient of dispersed phase is one of the fundamental and essential parameters in the design of an extraction column. Several correlations have been proposed in past studies for calculation of mass transfer coefficient. The results of these studies have usually been interpreted in the light of three mechanisms of mass transfer inside drops. These three mechanisms are: i) considering the mass transfer rate of solute in a drop to be the molecular diffusion in a stagnant spherical drop³, ii) laminar diffusion with circulation induced by relative motion of drop and continuous phase⁴, and iii) eddy diffusion between internal toroidal stream lines⁵. The governing equations are summarized in Table 1. The small drops are found to be subject to the molecular diffusion rate control, but, large drops may exhibit Handlos-Baron behavior. The criteria of transition between different mechanisms of behavior are usually based on

Table 1. Three proposed mechanisms of dispersed phase mass transfer coefficient

Molecular diffusion in stagnant drops (Newman equation)	
$K_d = -\left(\frac{d}{6t}\right) \text{Ln} \left[\left(\frac{6}{\pi^2} \sum_{n=1}^{\infty} \left(\frac{1}{n^2} \right) \exp \left(-\frac{4D_d \pi^2 n^2 t}{d^2} \right) \right) \right]$	$\text{Re} \leq 10$ (1)
Laminar diffusion with circulation induced by relative motion of drop and continuous phase (Kronig and Brink equation)	
$K_{od} = -\frac{d}{6t} \text{Ln} \left[\frac{3}{8} \sum_{n=1}^{\infty} B_n^2 \exp \left(-\frac{64\lambda_n D_d t}{d^2} \right) \right]$	$10 \leq \text{Re} \leq 200$ (2)
Eddy diffusion between internal toroidal stream lines (Handlos and Baron equation)	
$K_{od} = -\frac{d}{6t} \text{Ln} \left[6 \sum_{n=1}^{\infty} B_n^2 \exp \left(-\frac{\lambda_n V_d t}{128d(1+\kappa)} \right) \right]$	$200 \leq \text{Re}$ (3)

Reynolds or Weber or other factors which are found to be not very reliable.

Calderbank and Korchinski proposed an alternative approach involving the use of an enhanced molecular diffusivity, $\Re D_d$, (also referred to as effective diffusivity) in the equation of Kronig and Brink with the dimensionless enhancement factor⁶, $\Re = 2.25$:

$$K_d = -\left(\frac{d}{6t}\right) \text{Ln} \left[1 - \left\{ 1 - \exp \left(-\frac{4\pi^2 \Re D_d t}{d^2} \right) \right\}^{1/2} \right] \quad (4)$$

The circulation patterns and mixing intensity in oscillating drops are not well understood. The values of the mass transfer coefficients are experimentally similar to those predicted by the simple model of Handlos and Baron. This might be due to the internal circulation of drops. Photographic study of oscillating drops by Rose and Kintner shows that the toroidal circulation patterns postulated by Handlos and Baron deviate from reality. When the drop oscillates, the surface area changes with time⁷.

Johnson and Hamielec suggested the following equation with a new formula for determining \Re ⁸:

$$K_{od} = \left(-\frac{d}{6t} \right) \text{Ln} \left[6 \sum_{n=1}^{\infty} B_n \exp \left(-\frac{4\lambda_n^2 \Re D_d t}{d^2} \right) \right] \quad (5)$$

Since in their experiments which was the transfer of ethyl acetate into (vigorously circulating) water drops a rapid approach to equilibrium was observed, they considered only the first term of the series in the above equation and determined \Re values:

$$\Re = \frac{dV_t}{2048D_d(1+\kappa)} \quad (6)$$

Boyadzhiev et al. presented the following equation for calculating \Re in equation (4) based on their own experimental data⁹:

$$\Re = 0.0125 \left[\frac{\text{Re}}{2(1+\kappa)} \right], \text{ for } \Rightarrow \frac{D_d t}{d^2} > 10^{-2} \quad (7)$$

Steiner also used equation (5) reduced to its first term of the summation series and evaluated \Re values on the basis of data from nine sources. The equation proposed was¹⁰:

$$\Re = 1 + 0.177 \text{Re}^{0.043} Sc_d^{0.23} (1+\kappa)^{-0.89} \text{ for } \Rightarrow \Re < 10 \quad (8)$$

Temos et al presents the relation between eddy diffusivity and molecular diffusivity in a simple way¹¹:

$$\Re = 1 + 0.44D_E / D_d \quad (9)$$

Where:

$$D_E = 3.29 \times 10^{-4} (\rho_d V_d / \mu_d) \times \left[1 - \exp \left(-3.29 \times 10^{-4} (\rho_d V_d / \mu_d) \right) \right] \times \left(\frac{\mu_d}{\rho_d} \right) \quad (10)$$

V_i for $\text{Re} > 1$ is given by:

$$V_i = \left\{ 1 - \left[\frac{2+3\kappa}{1 + (\mu_d \rho_d / \mu_c \rho_c)^{0.5}} \right] \frac{1.45}{\text{Re}^{0.5}} \right\} V_t \quad (11)$$

The mass transfer coefficient is considered independent on height of column in all above mentioned correlations.

EXPERIMENTAL

Set-up Description

The packed column set up used in this study for continuous counter-current separation of acetic acid from dispersed phase was a 91 mm × 1250 mm Pyrex glass column packed with two pieces of Penta-Pak TM PS-500M1 structured packing (Fig. 1). The total height of packing was 40 cm (Fig. 2). The packing was made of corrugated sheets in a cylindrical structure with a diameter equal to the internal diameter of column. The inclination of the corrugation is 45°.



Figure 1. Applied structure packing

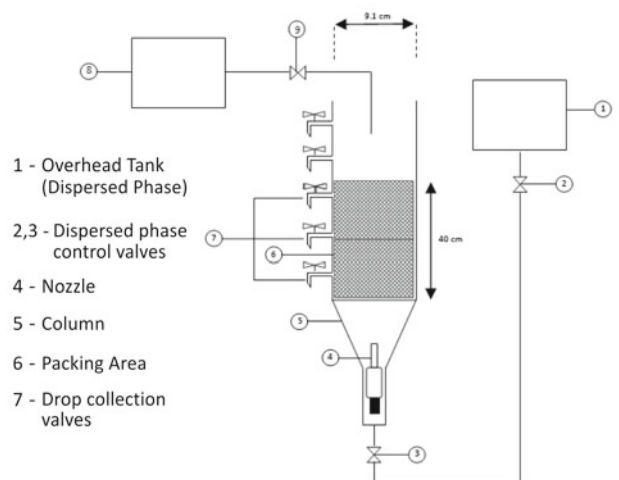


Figure 2. Schematic diagram of the apparatus

The experiment was carried out at room temperature under steady-state conditions. At the lower end of column, there is a discharge valve and glass entrance nozzle which can be used to connect to different nozzles for dispersed phase inlet. The dispersed phase enters through the bottom of column. The entrance nozzle of

the dispersed phase has a valve which controls the speed of drops to the continuous phase. To collect the drops in different heights several plug type valves were used. The drops were collected and analyzed at the heights of 11, 24.5, 39 cm from the bottom of the column.

Chemical Systems

Two different dispersed phases was provided by adding 5 vol% acetic acid to the saturated toluene and butyl acetate. Distilled water saturated with toluene and butyl acetate was used as the continuous phase. These two chemical systems, system 1: toluene-acetic acid-water (high interfacial tension) and system 2: *n*-butyl acetate-acetic acid-water (medium interfacial tension) were selected to increase the range of the interfacial tensions. The physical properties of these chemical systems are provided in Table 2.

Table 2. Physical properties of systems at 20°C

Physical property	System 1 T/A/W	System 2 B/A/W
ρ_c [kg/m ³]	1009.7	1010.2
ρ_d [kg/m ³]	882.7	895.9
μ_c [mPa.s]	1.016	1.013
μ_d [mPa.s]	0.611	0.684
γ [mN/m]	27.5–30.1	12.4–13.2
D_d [m ² /s]	2.92×10^{-9}	2.66×10^{-9}

Calculation of experimental dispersed-phase mass transfer coefficient

Considering the mass balance for a single drop the following equation can be obtained:

$$K_d = \left(-\frac{d}{6t} \right) \ln(1-E) \quad (12)$$

where:

$$E = \frac{c_0 - c}{c_0 - c^*} \quad (13)$$

c_0 , c , c^* are solute concentration in primary drop (before contact), concentration in specific position and the concentration in equilibrium with continuous phase, respectively which is measured through collecting the drops and doing titration using normal NaOH.

In each experiment and for different heights of the column by measuring Acetic Acid concentration, mean diameter and terminal velocity of droplets and the contact time between two phases, the mass transfer coefficients are calculated considering equation (12).

In order to find a correlation for the effective diffusivity for the counter-current conditions, the experimental values of the mass transfer coefficients are used in the Newman equation. In practice the drops will experience different events during their passage through the column such as breakage, coalescence and so on. The effective diffusivity can consider all above mentioned events. The experimental values of the mass transfer coefficients obtained from equation 12 are used in Newman equation to find the effective diffusivity. The molecular diffusivity obtained from experimental data in the Newman equation would act as the effective diffusivity.

CALCULATION OF COLUMN HEIGHT

In all previously published works, the HTU is considered as a fixed value in a specified column^{12,13}. There are also tables which give the values of HTU for a specific type of packing¹⁴. Although the variation of HTU has been confirmed by some people, no theoretical explanation has been proposed to support this finding. As it has been discussed¹, the mass transfer coefficient is intensively affected by height of packing in a single drop system. The present work aims to study the existence of similar trend for counter current condition. Such trend may happen due to the fact that by approaching the end of the column decreasing the solute concentration results in less mass transfer rate and less values for mass transfer coefficients. Thus, assumption of a constant mass transfer coefficient in calculating the height of column is not correct anymore. Indeed, with increasing the packing height while the mass transfer coefficient is decreasing, the equivalent height of column (theoretical plate) increases. The counter-current differential extractors such as packed columns are characterized by a continuous change in the concentration profile from top to bottom, rather than step changes. The flux of solute through the interface is related to the change of solute concentration across the section as follows¹⁵:

$$dN_a = -U_d dC_d = K_d a (C_d - C_d^i) dh \quad (14)$$

Where C_d is the concentration of the dispersed phase, C_d^i is that at the interface and dh is the differential height.

In order to calculate the height of column, equation (14) was rearranged and integrated in the following form:

$$H = \frac{U_d}{K_d a} \int_{C_{d0}}^{C_{d1}} \frac{dC_d}{(C_d - C_d^i)} \quad (15)$$

In that approach, as stated before, it is assumed that the mass transfer coefficient is constant and is not depended on the height of column. The total height of packed column needed can be established by the product of NTU and HTU.

Eq. (15) may be conveniently expressed as:

$$H = HTU * NTU \quad (16)$$

where NTU, termed the number of transfer units, is given by:

$$NTU = \int_{C_{d0}}^{C_{d1}} \frac{dC_d}{(C_d - C_d^i)} \quad (17)$$

The HTU, the height of transfer unit is constant and given by:

$$HTU = \frac{U_d}{K_d a} \quad (18)$$

This is a simple method of representation which has been widely used as a method of design.

In the new approach proposed here, the mass transfer coefficient is a function of column height, thus Eq. (14) can be rewritten as:

$$\int_0^H K_d dh = \frac{U_d}{a} NTU \quad (19)$$

For a specific separation NTU is fixed and the integration calculation should be repeated for the number of transfer units.

In the first step to determine the first HTU, NTU is considered to be equal to 1 and the integral limits are defined as below:

$$\int_{H_0}^{H_1} K_d dh = \frac{U_d}{a} * 1 \quad (20)$$

H_0 is very small and considered to be 0.001 to initiate the calculations.

As discussed before, the correlation of mass transfer coefficient applied here is²:

$$K_d = \frac{-d}{6t} \ln \left(\frac{61}{\pi^2} \sum_{i=1}^{100} \frac{1}{i^2} \exp \left(\frac{-4i^2 \pi D_{eff}(h)}{d^2} \right) \right) \quad (21)$$

Equation (20) can be solved to obtain H_1 . The first HTU, HTU1, is then obtained as:

$$HTU1 = H1 - H0 \quad (22)$$

To calculate HTU2 the following equation should be solved:

$$\int_{H_1}^{H_2} K_d dh = \frac{U_d}{a} * 1 \quad (23)$$

HTU2 is then obtained as:

$$HTU2 = H2 - H1$$

This approach is continued for the number of transfer units. The total required height is the summation of these HTU's.

Although other mathematical procedures can be applied to solve Eq. (19), the presented method is desirable as it is a very simple and apprehensible method. Moreover, the concept of different HTU's (in contrast to identical ones) can be readily expressed by this method.

RESULTS AND DISCUSSIONS

Mass transfer coefficients

The results of this experimental study show that the mass transfer coefficient is strongly affected by column height. The effect of column height on mass transfer coefficients is given in Figures 3 and 4. In these Figures effective diffusivity versus Reynolds number is presented in different heights of the column for two chemical systems. Figure 3 presents data for the first chemical system, toluene-acetic acid-water and the counterpart values for second chemical system, n-butyl acetate-acetic acid-water, are shown in Figure 4. As shown in these figures, the diffusivity of the dispersed phase increases by decreasing column height. This happens due to the fact that by approaching the end of the column the decrease in solute concentration results in less mass transfer driving force and smaller values for the mass transfer coefficients. Comparison of the effective diffusivities of

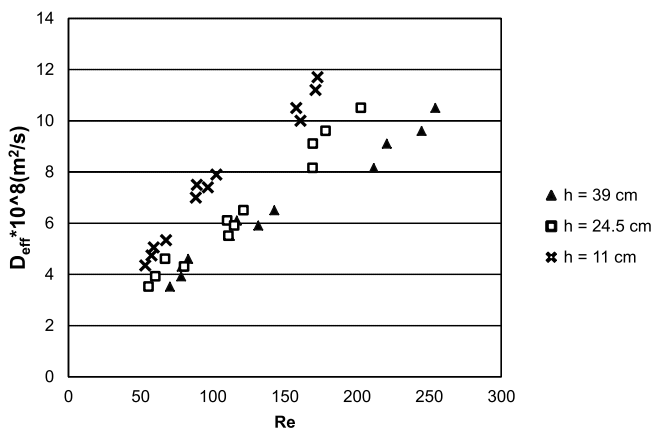


Figure 3. D_{eff} versus Re in different heights of column, T/O/A.

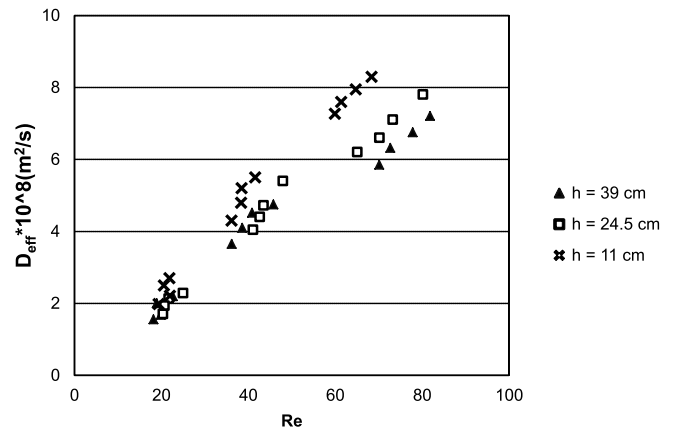


Figure 4. D_{eff} versus Re in different heights of column, B/O/A

two systems also shows that the second system, n-butyl acetate-acetic acid-water, has less values of D_{eff} . This is due to lower interfacial tension in this system. It means that for a system with lower values of interfacial tension, the mass transfer coefficients are smaller because of less internal circulations of droplets.

Regression of the experimental data based on the diffusion concept discussed before leads to the following correlation.

$$D_{eff} = 2.18 * 10^{-9} * h^{-0.25} * Re^{0.66} \quad (24)$$

This correlation is similar to the one previously proposed for a single drop system¹.

The predictions of the proposed correlation are compared with the experimental data for the dispersed phase mass transfer coefficient in Figure 5. As the Figure shows, the suggested correlation can accurately predict the experimental data with an average error of 14%.

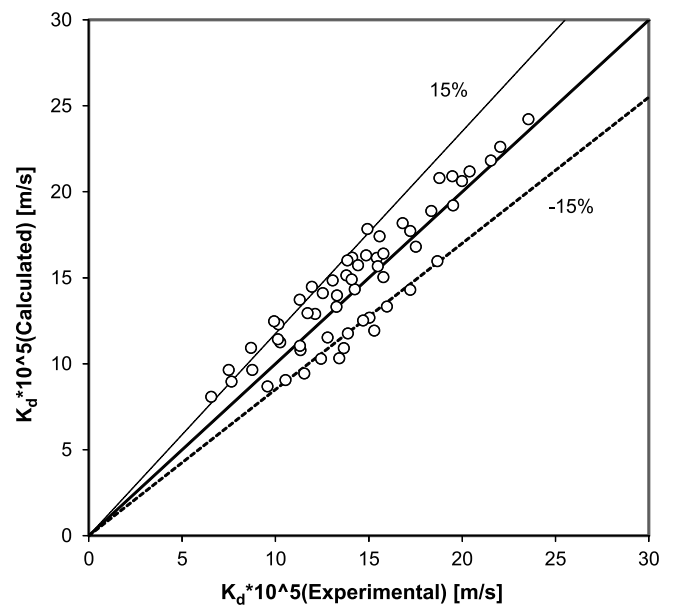


Figure 5. Comparison of experimental results with calculated values

Height of Packed Column

For our experimental study with a specific separation the explained mathematical procedure is applied. The required heights of packed column are derived for different conditions.

The obtained HTU's using the proposed approach are presented in Tables 3–8. A large number of correlations for prediction of mass transfer coefficient are

available in the literature^{6–10}. Three major correlations were chosen for comparison to the correlation proposed here. As can be seen in the first row of Table 5, the

Table 3. Experimental and calculated height using selected equations, T/A/W, h = 11 cm

C _{out} [mole/lit]	NTU	Experimental [m]	Newman		Kronig and Brink		Handlos and Baron		Present Work	
			Calculated [m]	Err. [%]	Calculated [m]	Err. [%]	Calculated [m]	Err. [%]	Calculated [m]	Err. [%]
0.107	1.84	0.11	0.69	523.8	0.37	238.9	0.05	52.4	0.081	26.02
0.102	1.89	0.11	0.67	509.5	0.37	232.2	0.04	59.3	0.084	23.86
0.112	1.80	0.11	0.64	481.3	0.35	216.8	0.04	63.4	0.079	27.89
0.116	1.76	0.11	0.61	452.0	0.33	201.4	0.04	67.5	0.078	28.89
0.168	1.39	0.11	0.79	616.6	0.41	275.8	0.04	62.2	0.077	29.72
0.171	1.37	0.11	0.76	589.9	0.40	262.5	0.04	65.4	0.076	31.24
0.157	1.46	0.11	0.77	604.5	0.41	271.5	0.04	66.6	0.081	25.96
0.170	1.38	0.11	0.74	570.9	0.39	253.7	0.03	69.1	0.076	30.94
0.273	0.91	0.11	0.87	694.2	0.43	294.0	0.02	77.5	0.108	2.22
0.287	0.85	0.11	0.86	677.3	0.43	286.8	0.02	79.3	0.101	7.74
0.286	0.86	0.11	0.83	650.8	0.41	274.5	0.02	81.2	0.102	7.43
0.302	0.81	0.11	0.80	626.3	0.40	261.5	0.02	82.7	0.099	10.02
Average Absolute Error				583.1		255.8		68.9		20.99

Table 4. Experimental and calculated height using selected equations, T/A/W, h = 24.5 cm

C _{out} [mole/lit]	NTU	Experimental [m]	Newman		Kronig and Brink		Handlos and Baron		Present Work	
			Calculated [m]	Err. [%]	Calculated [m]	Err. [%]	Calculated [m]	Err. [%]	Calculated [m]	Err. [%]
0.025	3.28	0.245	1.56	538.4	0.86	251.6	0.11	54.0	0.142	41.92
0.053	2.54	0.245	1.57	539.5	0.86	252.5	0.08	67.7	0.105	57.24
0.036	2.93	0.245	1.43	484.5	0.79	222.1	0.08	68.5	0.148	39.79
0.045	2.71	0.245	1.35	452.9	0.75	204.9	0.06	76.3	0.155	36.79
0.084	2.09	0.245	1.85	654.0	1.00	307.7	0.08	68.6	0.203	17.34
0.085	2.07	0.245	1.76	616.8	0.95	288.7	0.07	72.6	0.197	19.65
0.089	2.02	0.245	1.78	627.0	0.96	293.2	0.07	72.6	0.192	21.68
0.099	1.92	0.245	1.68	583.9	0.91	270.1	0.06	75.4	0.178	27.40
0.189	1.27	0.245	2.05	735.7	1.05	329.3	0.04	82.7	0.228	7.11
0.183	1.31	0.245	1.98	707.9	1.02	317.1	0.04	84.7	0.226	7.56
0.195	1.24	0.245	1.84	652.6	0.95	289.2	0.03	86.4	0.214	12.83
0.211	1.16	0.245	1.76	616.7	0.91	270.0	0.03	87.7	0.202	17.45
Average Absolute Error				600.8		274.7		74.8		25.56

Table 5. Experimental and calculated height using selected equations, T/A/W, h = 39 cm

C _{out} [mole/lit]	NTU	Experimental [m]	Newman		Kronig and Brink		Handlos and Baron		Present Work	
			Calculated [m]	Err. [%]	Calculated [m]	Err. [%]	Calculated [m]	Err. [%]	Calculated [m/s]	Err. [%]
0.014	3.89	0.39	2.83	627.2	1.56	299.8	0.14	64.4	0.308	21.08
0.016	3.74	0.39	2.69	590.2	1.48	279.3	0.12	68.8	0.253	35.01
0.023	3.40	0.39	2.47	533.6	1.36	248.4	0.11	72.6	0.255	34.54
0.025	3.31	0.39	2.30	490.8	1.26	224.1	0.09	76.6	0.239	38.78
0.059	2.44	0.39	2.94	654.0	1.61	312.0	0.10	73.4	0.269	31.11
0.047	2.67	0.39	2.92	649.8	1.61	311.7	0.09	76.8	0.295	24.38
0.066	2.33	0.39	2.74	605.0	1.50	285.7	0.09	77.6	0.269	30.90
0.057	2.46	0.39	2.69	590.5	1.48	279.2	0.08	80.3	0.274	29.84
0.162	1.43	0.39	3.26	737.2	1.69	334.1	0.06	85.1	0.336	13.95
0.175	1.35	0.39	3.07	688.2	1.59	308.8	0.05	86.8	0.319	18.11
0.169	1.39	0.39	3.00	671.2	1.57	301.7	0.05	88.0	0.322	17.41
0.183	1.30	0.39	2.79	617.5	1.46	274.1	0.04	89.4	0.289	25.88
Average Absolute Error				621.3		288.2		78.3		26.75

Table 6. Experimental and calculated height using selected equations, B/A/W, h = 11 cm

C _{out} [mole/lit]	NTU	Experimental [m]	Newman		Kronig and Brink		Handlos and Baron		Present Work	
			Calculated [m]	Err. [%]	Calculated [m]	Err. [%]	Calculated [m]	Err. [%]	Calculated [m]	Err. [%]
0.016	3.73	0.11	0.61	455.2	0.33	199.8	0.05	53.9	0.082	25.49
0.023	3.37	0.11	0.57	413.6	0.31	178.1	0.04	65	0.079	28.16
0.046	2.68	0.11	0.49	346.4	0.27	143.7	0.03	72.8	0.067	39.17
0.048	2.64	0.11	0.46	316.7	0.25	126.5	0.02	77.5	0.065	40.53
0.059	2.43	0.11	0.8	624	0.44	296.5	0.04	68.1	0.113	3.11
0.059	2.44	0.11	0.77	602.3	0.42	285.2	0.03	71.2	0.113	3.06
0.071	2.25	0.11	0.72	556.2	0.4	259.8	0.03	74	0.105	4.91
0.081	2.12	0.11	0.67	507.2	0.37	233.2	0.02	77.6	0.098	11.33
0.108	1.83	0.11	0.88	703.2	0.47	322.9	0.03	71.3	0.127	15.82
0.113	1.79	0.11	0.87	694.3	0.46	320.3	0.03	74.1	0.124	13.07
0.117	1.75	0.11	0.85	673	0.45	309.5	0.03	76.8	0.123	11.57
0.129	1.66	0.11	0.82	644.8	0.43	294.1	0.02	79.8	0.12	9.52
Average Absolute Error				544.7		247.5		71.8		17.15

Table 7. Experimental and calculated height using selected equations, B/A/W, h = 24.5 cm

C _{out} [mole/lit]	NTU	Experimental [m]	Newman		Kronig and Brink		Handlos and Baron		Present Work	
			Calculated [m]	Err. %	Calculated [m]	Err. [%]	Calculated [m]	Err. [%]	Calculated [m]	Err. [%]
0.002	6.05	0.245	1.42	480.4	0.71	190.6	0.1	59.6	0.163	33.48
0.002	6.05	0.245	1.36	455.2	0.67	175.3	0.08	67.7	0.168	31.46
0.003	5.55	0.245	1.24	407.9	0.62	151.7	0.07	73	0.156	36.53
0.005	4.85	0.245	1.15	367.5	0.57	134.3	0.05	79.1	0.146	40.48
0.01	4.18	0.245	2.11	761.4	1.16	375.2	0.07	71.3	0.275	12.16
0.013	3.97	0.245	1.92	683.9	1.06	331.9	0.06	75.9	0.252	3.05
0.017	3.7	0.245	1.8	635	0.99	305.1	0.05	78.7	0.238	2.98
0.02	3.5	0.245	1.68	586.7	0.93	278.3	0.05	81	0.223	9.06
0.039	2.84	0.245	2.23	811.1	1.21	395.7	0.06	76	0.283	15.36
0.042	2.78	0.245	2.11	761.7	1.15	370.1	0.05	79	0.273	11.24
0.048	2.65	0.245	2	715.9	1.09	345.4	0.05	81.5	0.261	6.46
0.05	2.6	0.245	1.92	684.9	1.05	329.1	0.04	83.8	0.257	4.91
Average Absolute Error				612.6		281.9		75.6		17.26

Table 8. Experimental and calculated height using selected equations, B/A/W, h = 39 cm

C _{out} [mole/lit]	NTU	Experimental [m]	Newman		Kronig and Brink		Handlos and Baron		Present Work	
			Calculated [m]	Err. [%]	Calculated [m]	Err. [%]	Calculated [m]	Err. [%]	Calculated [m]	Err. [%]
2.70E-05	10.11	0.39	2.54	551.3	1.17	198.9	0.15	61	0.305	21.91
1.70E-05	10.61	0.39	2.4	514.3	1.08	175.9	0.13	67.1	0.313	19.78
1.90E-04	8.19	0.39	1.99	410	0.91	132.4	0.1	74.8	0.243	37.61
3.10E-04	7.7	0.39	1.86	376.2	0.85	116.7	0.08	80.1	0.239	38.77
1.50E-03	6.1	0.39	3.57	815.9	1.93	395.1	0.1	73.9	0.444	13.77
1.20E-03	6.35	0.39	3.52	801.8	1.89	384.3	0.09	76.4	0.458	17.45
1.80E-03	5.93	0.39	3.24	730.4	1.74	345.1	0.08	80	0.426	9.35
2.70E-03	5.54	0.39	2.95	656.5	1.58	304.2	0.07	83	0.392	0.42
1.30E-02	3.96	0.39	3.73	857	2.05	426.6	0.09	78.2	0.466	19.55
1.60E-02	3.76	0.39	3.64	834.2	2.01	414.9	0.07	80.9	0.444	13.84
1.60E-02	3.71	0.39	3.5	797.1	1.93	394.9	0.07	82.8	0.433	11.03
2.10E-02	3.46	0.39	3.27	738.8	1.8	362.7	0.06	85.2	0.41	5.09
Average Absolute Error				673.6		304.3		76.9		17.38

NTU is 3.89. It means that 3.89 stages are required to reach the desired concentration in the height of 39 cm. Applying the Newman model to predict the mass transfer coefficient and determining the required height of the column using the conventional method leads to 0.73 m for each stage and totally a column of 2.8 m is required. However with our proposed approach, 3.89 stages with different heights are needed. i.e. HTU₁ = 5.4 cm, HTU₂ = 7.7 cm, HTU₃ = 8.9 cm and HTU₄ = 9.8 cm. As it was predicted, HTU's are increasing in each experimental run. The corresponding errors for the conventional method applying Newman model and our proposed approach are 627% and 21%, respectively. The average absolute error of the predicted column height applying proposed correlation for mass transfer coefficient is about 20%. The counterpart values for Newman, Kronig-Brink and Handlos-Baron models are 606%, 275% and 75%, respectively.

CONCLUSION

In this study mass transfer coefficients is measured experimentally in different heights of packed column to predict its height. The study leads to introduction of a novel conceptual method to predict column height via new correlation for mass transfer coefficient. This new approach is called *increasing HTU's*. According to the results, the following conclusions are obtained:

– In contrast to previously believed concept, HTU is not a fixed value in column. While the height of column increases the value of HTU increases too.

– The mass transfer coefficient can be obtained with much better precision by applying the effective diffusivity in Newman equation and by introducing the height of the packing in the correlation.

– The experimental results show that the mass transfer coefficient is meaningfully a function of the height of the packing. While the height of packing increases solute concentration decreases and this results in less mass transfer rates.

– Presenting of the mass transfer coefficient as a function of height of packing is a new approach which can provide a theoretical basis for the calculation of column height.

– The conventional method for calculating the column height does not predict the height of column with a satisfactory accuracy while applying the new approach can significantly reduce the average error.

APPENDIX A. NOMENCLATURE

- a – Specific Area
- B_n – Constants of Eqs. (2)&(3)
- c – Solute concentration in dispersed phase (kg/m³)
- d – Drop diameter (m)
- D_d – Molecular diffusivity (m²/s)
- D_{eff} – Effective diffusivity (m²/s)
- E – Extraction Efficiency
- h – Height of packing (m)
- K_d – Dispersed phase mass transfer coefficient (m/s)
- K_{od} – Overall dispersed phase mass transfer coefficient (m/s)
- ℜ – Enhancement factor for mass transfer

Re	– Reynolds number ($=\rho_c U d / \mu_c$)
t	– Contact time (s)
U	– Drop velocity (m/s)
V_t	– Terminal velocity (m/s)
NTU	– Number of Transfer Units
HTU	– Height of Mass Transfer Unit (m)

Greek symbols

γ	– Interfacial tension (kg/s ²)
K	– Ratio of dispersed phase viscosity to continuous phase viscosity ($=\mu_d / \mu_c$)
λ_n	– Constants of Eqs. (2), (3), (5) and (12)
μ	– Viscosity (kg/m.s)
ρ	– Density (kg/m ³)

Subscripts

c	– Continuous phase
d	– Dispersed phase
0	– Initial Drop

Superscripts

*	– Equilibrium
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