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# Synthesis of Moore FSM with encoding of collections of microoperations implemented with ASIC

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#### Abstract

The method for reduction of hardware amount in logic circuit of the Moore finite state machine is proposed. The method is oriented on customized matrix technology. It is based on representation of the next state code as a concatenation of the code for class of collection of microoperations and the code of the vertex. Such an approach allows elimination of a dependence between states and microoperations. As a result, both circuits for generation of input memory functions and microoperations are optimized.

Keywords: Moore FSM, graph-scheme of algorithm, pseudoequivalent states, customized matrices, logic circuit.

# Syneza skończonego automatu stanu typu Moore'a z kodowaniem zbiorów mikrooperacji implementowanego w układach o strukturze matrycowej

#### Streszczenie

Model skończonego automatu stanu typu Moore'a jest często stosowany w jednostkach sterujących [1]. Postęp technologii półprzewodnikowej pozwala na tworzenie coraz bardziej złożonych układów cyfrowych. W przypadku produkcji masowej szeroko stosowane są układy ASIC (ang. Application-Specified Integrated Circuits). W układach ASIC automaty skończone są projektowane przy użyciu struktur macierzowych (rys. 1). Jednym z głównych problemów syntezy automatów skończonych ze strukturami macierzowymi jest zmniejszenie powierzchni układu scalonego zajmowanej przez układ logiczny automatu Moore'a. W artykule proponowana jest metoda, która jest zorientowana na redukcję zasobów sprzętowych potrzebnych do implementacji skończonego automatu stanu typu Moore'a implementowanego w układach o strukturze matrycowej. Ta metoda jest oparta na przedstawieniu następnego kodu stanu jako konkatenacji kodu klas zbiorów mikrooperacji i kodów wierzchołków. Takie podejście pozwala zmniejszyć liczbę linii w tabeli przejść automatu Moore'a do liczby linii równoważnej automatowi z wyjściami typu Mealy'ego. Oprócz tego przy zastosowaniu danej metody nie istnieje zależność między kodami stanów i kodami zbiorów mikrooperacji co pozwala zmniejszyć liczbę termów w bloku mikrooperacji. Artykuł przedstawia także przykład zastosowania proponowanej metody.

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Slowa kluczowe: automat typu Moore'a, sieć działań, stany pseudorównoważne, układ logiczny.

#### 1. Introduction

The model of the Moore finite state machine (FSM) [5] is often used during digital control systems realization [1-3]. The development of microelectronics has led to appearance of different programmable logic devices used for implementing FSM circuits. But in the case of mass production they use ASIC (Application-Specified Integrated Circuits) [7]. In the case of ASIC, the logic circuits of FSM are designed, as a rule, using the so called matrix structures. In these customized matrices the principle of distributed logic is used [9].

One of the important problems of FSM synthesis with ASIC is decrease of the chip area occupied by its logic circuit. One of the ways to solve this problem is optimal coding of FSM [5]. However, this approach does not allow optimization of the circuit generated output signals. In this work some new optimization method is proposed. It is based on representation of the next state code as a concatenation of codes for class of pseudoequivalent states and operator vertex where this collection is generated. Such an approach allows reducing the hardware amount in both parts of FSM circuits and does not lead to speed loss. A control algorithm to be implemented is represented by the graph-scheme of algorithms[2].

# 2. General aspects and the basic idea of the proposed method

Let Moore FSM be represented by the structure table (ST) with columns [2]:  $a_m$ ,  $K(a_m)$ ,  $a_s$ ,  $K(a_s)$ ,  $X_h$ ,  $\Phi_h$ , h. Here  $a_m$  is an initial state of FSM, (m=1,...,M);  $K(a_m)$  is a code of state  $a_m \in A$  of capacity  $R = \lceil log_2 M \rceil$ , to code the states the internal variables from the set  $T = \{T_1,...,T_R\}$  are used;  $a_s$ ,  $K(a_s)$ , are a state of transition and its code respectively;  $X_h$  is an input, which determines the transition  $\langle a_m, a_s \rangle$ , and equal to conjunction of some elements (or their complements) of a logic conditions set  $X = \{x_1,...,x_L\}$ ;  $\Phi_h$  is a set of input memory functions for flip-flops of FSM memory, which are equal to 1 for memory switching from  $K(a_m)$  to  $K(a_s)$ ,  $\Phi_h \subseteq \Phi = \{\phi_1,...,\phi_R\}$ ;  $h = 1, \ldots, H$  is a number of transition. In the column  $a_m$  a set of microoperations  $Y_q$  is written, which is generated in the state  $a_m \in A$ , where  $Y_q \subseteq Y = \{y_1,...,y_N\}$ , q = 1,...,Q. This table is a basis to form the system of functions.

$$\Phi = \Phi(T, X), \tag{1}$$

$$Y = Y(T)$$
<sup>(2)</sup>

which determines an FSM logic circuit. Systems (1)-(2) describe the matrix model of Moore FSM  $U_1$  shown in Fig. 1.



Fig. 1. Matrix implementation of FSM  $U_1$ Rys. 1. Matrycowy układ automatu Moore'a  $U_1$ 

Let us analyze the components of the matrix circuit shown in Fig. 1. In FSM  $U_1$  the conjunctive matrix  $M_1$  implements the system of terms  $F = \{F_1, ..., F_H\}$ ; the disjunctive matrix  $M_2$  implements the system (1); the conjunctive matrix  $M_3$  implements the terms  $A_m$  corresponding to FSM states; the disjunctive matrix  $M_4$  implements functions (2). The register RG keeps state codesit controlled by signals Start (clearing) and Clock (changing content depending on functions  $\Phi$ ). The matrices  $M_1$  and  $M_2$  form the block of input memory functions (BIMF), whereas the matrices  $M_3$  and  $M_4$  - the block of microoperations (BMO).

The model of the Moore FSM is very often used in the practice of digital design because its outputs are stable [8]. But, as a rule, it has more states than an equivalent Mealy FSM [1]. It leads to the fact that the number  $H_1$  is much greater than the number of lines  $H_0$  of ST for an equivalent Mealy FSM. Let  $M_0$  be the number of states of the equivalent Mealy FSM and  $R_0$  be defined as  $R_0 = \lceil \log_2 M_0 \rceil$ . Then the following relations are true for practical cases:

$$H_0 < H_1; R_0 = \lceil \log_2 M_0 \rceil < R.$$
 (3)

The hardware amount is determined for the matrix circuits as a chip area occupied by an FSM circuit [1].

Complexity of each matrix is defined by the area S(Mi) of a crystal demanded for its implementation ( $i = \overline{1,4}$ ). In theoretical papers this area is defined in arbitrary units [5, 7]. Next estimations can be obtained for FSM  $U_1$ :

$$S(M_1) = 2(L+R)H_1; S(M_2) = H_1R;$$
  

$$S(M_3) = 2R \cdot M; S(M_4) = M \cdot N.$$
(4)

The area  $S(U_1)$  that is occupied by a logic circuit of FSM  $U_1$  is defined as sum of the areas (4).

Because of relations (3), the chip area occupied by the circuit of the Moore FSM is always greater than this value for the equivalent Mealy FSM. There are a lot of methods targeting at hardware reduction of the Moore FSM circuit [3, 4, 6]. But they deal with either CPLD or FPGA chips. Because of it, they cannot be directly used in the case of ASIC. Taking it into account, we propose a new method targeting at ASIC.

One of the Moore FSM features is existence of pseudoequivalent states [2], which are the states with the same transitions by the effect of the same inputs. Such states correspond to the control algorithm operator vertices [1], outputs of which are

connected with an input of the same vertex. The known methods of optimizations of the matrix circuit  $U_1$  are based on existence of pseudoequivalent states. There are two main optimization methods [3].

*Optimal state encoding.* The state  $a_m \in A$  is encoded so that each class of pseudoequivalent states  $B_i \in \Pi_A$  is represented by the single generalized interval of R-dimensional Boolean space. In this case  $M_1$  realizes only  $H_0 = H_2 < H_1$  terms. However, such coding is not always possible [3]. It leads to  $H_2 > H_0$ .

Method of transformation of the states codes. The classes  $B_i \in \Pi_A$  are encoded by the binary codes  $K(B_i)$  with  $R_1 = \lceil \log_2 I \rceil$  bits. Let us point out that  $I = M_0$ , where  $M_0$  is the number of the states of the equivalent Mealy FSM. The variables  $\tau_r \in \tau$  are used for such encoding, where  $|\tau| = R_1$ . Next the system of functions is formed  $\tau = \tau(I)$ . The system  $\tau = \tau(I)$  specifies the law of transformations of the codes  $K(a_m)$  into the codes  $K(B_i)$ . ST is transformed in such a way that the states  $a_m \in B_i$  are replaced with the classes  $B_i \in \Pi_A$  in the column of the initial state. Such approach allows decreasing ST to  $H_0$  and the number of variable feedback is reduced to  $R_1 < R$ .

The area of BIMF can be decreased using the approach of optimal state encoding. The area of BMO can be decreased due to refined state encoding. But these methods cannot be used together. In this paper the method permitting mutual area decrease for both blocks of FSM [3] is proposed.

Let  $\Pi_A = \{B_1, ..., B_I\}$  be a partition of a set A on classes of pseudoequivalent states. Let us code classes  $B_i \in \Pi_A$  by binary codes  $K(B_i)$  having  $R_B$  bits, where  $R_B = \lceil log_2 I \rceil$ .

Let initial GSA  $\Gamma$  include Q different collections of microoperations (CMO)  $Y_q \subseteq Y$ . Let us code set  $Y_q$  with binary code  $K(Y_q)$  having  $R_Y$  bits, where  $R_Y = \lceil \log_2 Q \rceil$ .

Let  $E_1 = \{b_1, \dots, b_D\}$  be a set of operator vertices from GSA  $\Gamma$ . Let us use the following relation  $\alpha$  on this set  $E_1$ 

$$b_i \alpha b_j \leftrightarrow Y(b_i) = Y(b_j).$$
 (5)

In (5), the symbols  $Y(b_i), Y(b_j) \subseteq Y$  stand for collections of MO from vertices  $b_i$  and  $b_j$   $(i, j \in \{1, ..., D\})$ . The relation  $\alpha$  determines the partition  $\Pi_{\alpha} = \{C_1, ..., C_{\eta}\}$ . Let us encode each vertex  $b_q \in C_j$  by the binary code  $K(b_q)$  having

$$R_{\alpha} = \left\lceil \log_2 G \right\rceil \tag{6}$$

bits. In (6),  $G = max(|C_1|,...,|C_\eta|)$ . Let us use variables  $z_r \in Z_1$  for this encoding, where  $|Z_1| = R_\alpha$ . In this case, the code for state  $a_m \in A$  can be represented as:

$$K(a_m) = K(Y_q) * K(b_q), \qquad (7)$$

where  $b_q \in E_1$  is the operator vertex marked by state  $a_m \in A$ ,  $Y_q = Y(b_q)$ , and \* is the sign of concatenation.

Let us construct the system

$$B = B(A), \tag{8}$$

which describes the dependence among the classes  $B_i \in \prod_A$  from the states  $a_m \in A$ . Each function  $B_i \in B$  is represented as the following

$$B_{i} = \bigvee_{i=1}^{I} C_{im} A_{m} (i = 1, ..., I), \qquad (9)$$

where the symbol  $C_{im}$  stands for the Boolean variable equal to 1,  $a_m \in B_i$ . The proposed matrix implementation of the Moore FSM  $U_2$  is shown in Fig. 2.



Fig. 2. Matrix implementation of FSM U<sub>2</sub>Rys. 2. Matrycowy układ automatu Moore'a U<sub>2</sub>

In FSM  $U_2$ , the matrix  $M_5$  implements the system of terms  $F_0$  corresponding to rows of the transformed table of transitions and depending on logical conditions  $x_l \in X$  and additional variables  $\tau_r \in \tau$ , used for encoding the classes  $B_i \in \Pi_A$ , where  $|\tau| = R_B$ . The matrix  $M_6$  implements the input memory functions

$$\Phi_0 = \Phi_0(\tau, X), \tag{10}$$

The system (10) includes  $R_Y + R_\alpha$  functions; it is the number of flip-flops from RG. The matrix  $M_7$  implements terms  $Y_0$ , entering the system  $y_n \in Y$  and depending from variables  $z_r \in Z$ , where  $|z| = R_Y$ . The matrix  $M_8$  implements functions  $y_n \in Y$ , depending on terms  $\Delta_q \in Y_0$ . The matrix  $M_9$  implements the terms  $A_0$  from (9), whereas the matrix  $M_{10}$  functions  $\tau_r \in \tau$ , used for encoding classes  $B_i \in \Pi_A$ , where  $|\tau| = R_B$ .

The matrices  $M_5$  and  $M_6$  form the block BIMF, the matrices  $M_7$  and  $M_8$  form the block BMO implementing the functions

$$Y = Y(Z) \,. \tag{11}$$

The matrices  $M_9$  and  $M_{10}$  form the block of the code transformer (BCT) generating functions

$$\tau = \tau(z, z_1) . \tag{12}$$

Let us estimate the areas of the matrixes of  $U_2$ :

$$S(M_5) = 2(L + R_B)H_0; S(M_6) = (R_Y + R_\alpha)H_0;$$
  

$$S(M_7) = 2R_Y q; S(M_8) = qN;$$
  

$$S(M_9) = 2(R_Y + R_\alpha)H'; S(M_{10}) = R_BH'.$$
(13)

There are some positive features in the proposed method. Now the codes of collections of microoperations do not depend on the state codes. It allows encoding the collections  $Y_q \subseteq Y$  minimizing the area of BMO. The number of rows in the table of transitions for FSM  $U_2$  is always equal to  $H_0$ . It allows such their encoding that diminishes the area occupied by BIMF. As it was mentioned before, there are enough  $R_A = \lceil log_2 M \rceil$  variables for state encoding in case of FSM  $U_1$ . The main drawback of  $U_2$  is increase in the number of inputs for BIMF if the following condition is true:

$$R_Y + R_\alpha > R_A . \tag{14}$$

Besides, the model  $U_2$  includes the block BCT which requires some area of the chip. But these drawbacks are compensated by the area decrease for blocks BIMF and BMO in comparison with the model  $U_1$ .

# 3. The proposed synthesis method for Moore FSM

In this work a method of the Moore FSM  $U_2$  synthesis using

- a GSA  $\,\Gamma\,$  is proposed. The method includes the next stages:
- 1. Marking of the GSA  $\Gamma$  and creation of the state set A.
- 2. Partition of the set A on classes of pseudoequivalent states.
- 3. Coding of microoperation collections  $Y_q \subseteq Y$ .
- 4. Construction of the partition  $\Pi_{\alpha}$  and encoding of operator vertices  $b_q \in E_1$ .
- 5. Encoding the classes  $B_i \in \Pi_A$ .
- 6. Construction of the transformed table of transitions.
- 7. Construction of the system (12) by the table of BCT.
- 8. Implementation of matrices  $M_5 M_{10}$ .

For the first step of implementation the known method [1] is used, when every operator vertex is marked by a unique state. The second step is trivially done by the use of pseudoequivalent states definition [3]. Bear in mind that states  $a_m$ ,  $a_s \in A$  are named pseudoequivalent if marked by them operator vertices of GSA are connected with the input of the same vertex.

The main goal of the third step is maximal decrease in the number of terms in the system  $Y_0$ . In the best case each microoperation  $y_n \in Y$  is represented by a single term and the matrix  $M_8$  is absent [1]. The fourth step is executed on the basis of (5). The codes of states  $a_m \in A$  are determined using formula (7). Classes  $B_i \in \Pi_A$  are encoded in such a manner that the number of terms in (12) is maximally decreased. It is reduced to the well-known task of symbolic encoding [2].

The transformed table of transitions includes the columns  $B_i$ ,  $K(B_i)$ ,  $a_s$ ,  $K(a_s)$ ,  $X_k$ ,  $\Phi_k$ , h. Here  $\Phi_h \subseteq \Phi_0$  is a collection of input memory functions equal to 1 to write the code  $K(a_s)$  into the register;  $h = 1, ..., H_0$  is the number of transition. The table of BCT includes the columns  $a_m$ ,  $K(a_m)$ ,  $B_i$ ,  $K(B_i)$ ,  $\tau_m$ , m. Here  $\tau_m \subseteq \tau$  is the collection of variables equal to 1 into the code  $K(B_i)$  from the m-th line of the table, where m = 1, ..., M. The last step is discussed in the proposed example.

## 4. Example of application for the proposed method

Let the symbol  $U_i(\Gamma_j)$  mean that the GSA  $\Gamma_j$  is interpreted by the model  $U_i$  (*i* = 1,2). Let us discuss the example of design for Moore FSM  $U_2(\Gamma_1)$ , where GSA  $\Gamma_1$  is shown in Fig. 3.



Fig. 3. Initial graph-scheme of algorithm  $\Gamma_1$ Rys. 3. Sieć działań  $\Gamma_1$ 

It can be found from GSA  $\Gamma_1$ , that  $A = \{a_1,...,a_8\}$ , M = 8, and  $R_A = 3$ . There is the partition  $\Pi_A = \{B_1,...,B_4\}$ , where  $B_1 = \{a_1\}$ ,  $B_2 = \{a_2,a_3,a_4\}$ ,  $B_3 = \{a_5,a_6\}$ ,  $B_4 = \{a_7,a_8\}$ . It gives us I = 4,  $R_B = 2$ ,  $\tau = \{\tau_1, \tau_2\}$ . There are five different collections of microoperations in GSA  $\Gamma_1$ :  $Y_1 = 0$ ,  $Y_2 = \{y_1, y_2\}$ ,  $Y_3 = \{y_3\}$ ,  $Y_4 = \{y_4\}$ ,  $Y_5 = \{y_1, y_3\}$ . To encode them, it is enough  $R_Y = 3$  variables from the set  $Z = \{z_1, z_2, z_3\}$ . Let us encode the collections  $Y_q \subseteq Y$  as it is shown in Fig. 4.

The following system of equations can be obtained using Figs. 3 and 4:

$$y_1 = Y_2 \lor Y_5 = z_2 \overline{z_3} = \Delta_1; \ y_2 = Y_2 = \overline{z_1} z_2 \overline{z_3} = \Delta_2;$$
  

$$y_3 = Y_3 \lor Y_5 = z_1 = \Delta_3; \ y_4 = Y_4 = \overline{z_1} z_3 = \Delta_4;$$
(15)

$z_1$	$^{23}_{00}$	01	11	10
0	$\mathbf{Y}_1$	*	$Y_4$	$\mathbf{Y}_2$
1	*	*	$Y_3$	$Y_5$

Fig. 4.Codes of collections of microoperations  $U_2(\Gamma_1)$ Rys. 4.Kody zbiorów mikrooperacji  $U_2(\Gamma_1)$ 

The partition  $\Pi_{\alpha}$  includes four classes:  $C_1 = \{b_1, b_4, b_7\}$ ,  $C_2 = \{b_2\}$ ,  $C_3 = \{b_3, b_6\}$ ,  $C_4 = \{b_5\}$ . It gives G = 3,  $R_{\alpha} = 2$ ,  $Z_1 = \{z_4, z_5\}$ . There is the following system (8) in our example:  $B_1 = A_1$ ;  $B_2 = A_2 \lor A_3 \lor A_4$ ;  $B_3 = A_5 \lor A_6$ ;  $B_4 = A_7 \lor A_8$ .

Let us encode the vertices  $b_q \in E_1$  in such a manner that the state codes (7) are determined from Fig. 5.

$\sum Z_1$	$Z_2Z_3$							
$z_4 z_5$	000	001	011	010	110	111	101	100
00	$a_1$	*	$a_4$	$a_2$	*	<i>a</i> <sub>3</sub>	*	*
01	*	*	*	$a_5$	$a_6$	*	*	*
11	*	*	*	*	*	*	*	*
10	*	*	$a_8$	<i>a</i> <sub>7</sub>	*	*	*	*

Fig. 5. State codes for Moore FSM  $U_2(\Gamma_1)$ 

Rys. 5. Kody stanów automatu Moore'a  $U_2(\Gamma_1)$ 

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The following codes can be found from the Karnaugh map (Fig. 5):  $B_1 = \overline{z_2}$ ;  $B_2 = z_2 \overline{z_4 z_5}$ ;  $B_3 = z_5$ ;  $B_4 = z_4$ .

Let us encode the classes  $B_i \in \Pi_A$  in the following manner  $K(B_1) = 01$ ,  $K(B_2) = 00$ ,  $K(B_3) = 10$ ,  $K(B_4) = 11$ . The following system can be derived from these codes:

$$\tau_1 = B_3 \lor B_4 = z_5 \lor z_4; \ \tau_2 = B_1 \lor B_4 = \overline{z_2} \lor z_4.$$
(16)

The system (16) determines the block BCT, where the matrix  $M_9$  is absent.

Let us construct the system of generalized formulae of transitions for GSA  $\Gamma_{\!1}$  :

$$B_{1} \rightarrow x_{1}a_{2} \vee \overline{x_{1}}x_{2}a_{3} \vee \overline{x_{1}}x_{2}a_{4};$$
  

$$B_{2} \rightarrow x_{3}x_{2}a_{5} \vee x_{3}\overline{x_{2}}a_{6} \vee \overline{x_{3}}x_{4}a_{7} \vee \overline{x_{3}}\overline{x_{4}}a_{8};$$
 (17)  

$$B_{3} \rightarrow a_{2}; B_{4} \rightarrow a_{1}.$$

This system together with state codes from Fig. 5 leads to the transformed table of transitions for FSM  $U_2(\Gamma_1)$ , having  $H_0 = 9$  lines (Table 1). This table is used to derive the system (10). For example, the following functions can be found from Table 1:  $D_1 = F_2 \lor F_5 = \overline{\tau_1} \tau_2 \overline{x_1} x_2 \lor \overline{\tau_1} \tau_2 x_3 \overline{x_2}$ ;  $D_2 = F_2 \lor \ldots \lor F_8$ ;  $D_3 = F_2 \lor F_3 \lor F_7$ ;  $D_4 = F_6 \lor F_7$ ;  $D_5 = F_4 \lor F_5$ . In the case of matrix implementation, there is no need in minimizing these functions. The table for BCT is absent on our example because the system (16) determines the functions (12). Let us find the areas for matrices  $M_5 - M_{10}$ , determined as the product for the numbers of inputs and outputs of the matrix.

Tab. 1.Transformed table of transitions for FSM  $U_2(\Gamma_1)$ Tab. 1.Tabela przejść automatu Moore'a  $U_2(\Gamma_1)$ 

B <sub>i</sub>	$K(B_i)$	$a_s$	$K(a_s)$	$X_h$	$\Phi_h$	h
<i>B</i> <sub>1</sub>	01	<i>a</i> <sub>2</sub>	01000	<i>x</i> <sub>1</sub>	$D_2$	1
		<i>a</i> <sub>3</sub>	11100	$\overline{x_1}x_2$	$D_{1}D_{2}D_{3}$	2
		<i>a</i> <sub>4</sub>	01100	$\overline{x_1}\overline{x_2}$	$D_{2}D_{3}$	3
B <sub>2</sub>	00	<i>a</i> <sub>5</sub>	01001	<i>x</i> <sub>3</sub> <i>x</i> <sub>2</sub>	$D_{2}D_{5}$	4
		<i>a</i> <sub>6</sub>	11001	$x_3\overline{x_2}$	$D_{1}D_{2}D_{5}$	5
		a <sub>7</sub>	01010	$\overline{x_3}x_4$	$D_2D_4$	6
		<i>a</i> <sub>8</sub>	01110	$\overline{x_3x_4}$	$D_{2}D_{3}D_{4}$	7
<i>B</i> <sub>3</sub>	10	<i>a</i> <sub>2</sub>	01000	1	<i>D</i> <sub>2</sub>	8
$B_4$	11	<i>a</i> <sub>1</sub>	00000	1	-	9

From the system of functions we can find the following areas of matrices:  $S(M_5) = 2(4+2)*9 = 108$ ,  $S(M_6) = 9*5 = 45$ ,  $S(M_7,M_8) = 5*4 = 20$  and  $S(M_9,M_{10}) = 3*2 = 6$ . Thus, it is necessary 179 area units [1] to implement the logic circuit of Moore FSM  $U_2(\Gamma_1)$ . It can be found for FSM  $U_1(\Gamma_1)$  that H = 19,  $S(M_1) = 2(4+3)*19 = 166$ ,  $S(M_2) = 19*3 = 57$ ,  $S(M_3) = 2*3*7 = 42$  and  $S(M_4) = 7*4 = 28$ .

It means that the logic circuit of FSM  $U_1(\Gamma_1)$  occupies 293 area units. Besides, the circuit of  $U_1(\Gamma_1)$  has 4 levels of logic, whereas the circuit for  $U_2(\Gamma_1)$  only three (because functions  $\tau$  and Y are generated in the same time). Thus, application of the proposed method for encoding the collections of microoperations with the state code presentation in the form (7) allows decreasing the area for 1,7 times Moore FSM.

### 5. Conclusions

The proposed method of state code presentation aims at area decrease under implementation of the Moore FSM logic circuit with customized matrices. This approach allows decreasing the number of terms in the system of input memory functions up to corresponding value of the equivalent Mealy FSM. Besides, this method permits decreasing the number of terms in the system of microoperations due to the lack of dependence between the state codes and the codes of collections of microoperations.

Investigations of the effectiveness of the proposed method were conducted on the standard examples [10]. They show that the proposed method permits decreasing the average chip area occupied by the FSM circuit up to 52% in comparison with the standard FSM implementation. At the same time it was the increase for FSM performance in 86% of examples. The further direction of our research is application of the proposed method to the case of FPGA.

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