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## Schedule design for multiprocessor systems

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### Abstract

Efficiency of multiprocessor system usage is strongly dependent on methods of schedule design – the way of task distribution on each processor to decrease overall schedule time. This article is devoted to the part of this process - schedule design on example of software development for LTE and WIMAX base stations.

**Keywords:** schedule, parallel programming, multi-processor system, genetic algorithm.

### Projektowanie harmonogramu dla systemów mikroprocesorowych

#### Streszczenie

Wydajność użytkowania systemów mikroprocesorowych silnie zależy od metody zaprojektowania harmonogramu, tj. od sposobu rozdziału zadań na każdy procesor. Ma to wpływ na zmniejszenie całkowitego czasu wykonywania zadań. W artykule przedstawiono część tego procesu, tj. projektowanie harmonogramu na przykładzie opracowania oprogramowania dla stacji bazowych LTE oraz WIMAX. Wskazano cztery algorytmy możliwe do zastosowania przy wykorzystaniu algorytmów genetycznych. Podano wyniki badań symulacyjnych tych algorytmów, z których wynika, że uzyskuje się dobrą zbieżność przy ograniczonej liczbie generacji. Głównym zadaniem analizowanym w pracy jest skrócenie czasu opracowania oprogramowania za pomocą automatycznego opracowania harmonogramu, znajdowania błędów, uproszczenia debugowania, i wizualizacji za pomocą diagramu. Do rozwoju oprogramowania telekomunikacyjnego proponuje się oryginalną metodę możliwą do zastosowania w formie systemu wbudowanego (SOC). Platformą hardware'ową jest element SOC i kilka różnych jednostek przetwarzających. Algorytm cyfrowego przetwarzania sygnałów jest zdefiniowany przez listę zadań wraz z informacjami o zależnościach. Typ jednostki przetwarzającej i czas przetwarzania są zdefiniowane z góry dla każdego zadania.

**Słowa kluczowe:** harmonogram, programowanie równoległe, system wieloprocessorowy, algorytm genetyczny.

## 1. Introduction

Developers aim to active telecommunication devices growth to constant updating the existing software and develop a new one. With the appearance of multi-processors computer systems and parallel programming this topic got more challenging.

Thus, the main task of this article is decreasing of the telecommunication software development time by automation of schedule design, errors finding, debug simplification and software workflow visualization. This approach based on concept of modified model driven software development was discussed in [4, 5].

To increase telecommunication software development, the original method of feasible schedule design for system on chip (SOC) software is offered. Hardware platform is SOC with a few types of different processing units (further “resources”). The digital signal transformation algorithm is defined by tasks list with dependency information. The resource type and processing time are defined beforehand for each task.

Other tasks resolved during feasible schedule design are minimizing the overall latency, meeting the deadline, and maximizing usage of system resources.

## 2. SOC software framework

SOC software framework is shown on Fig. 1. The messages containing Data and Control information flow between Upper and Lower Subsystems. Application Programming Interface (API) Parser and Data Analysis, and Partitioning (DAP) module is responsible for providing Scheduler, placed on system level, with Task Lists created from these messages. Scheduler is responsible for dispatching and posting Tasks from Tasks Lists to a proper Hardware Abstraction Layer (HAL) driver at the correct time. Therefore, the Task Scheduler's job is to decide “what” and “when” a Task should be executed. In case of multiple resources of the same type, the Task Scheduler may determine the resource number on which a Task runs, or rely on the HAL driver to make this assignment.

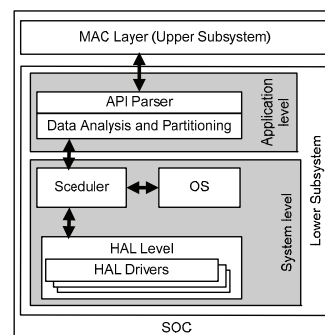


Fig. 1. Lower subsystem framework

Rys. 1. Szelet do budowy dolnego podsystemu

When scheduler can't use resource-intensive scheduling algorithms in real time mode, its debugging becomes a complex task. Therefore schedule analysis is performed on PC in offline mode. In this case scheduler simulator can use different levels of HAL layer emulations.

Online Scheduler, as shown on Fig. 2, scans Task List for available task, selects suitable resource and assigns task to it, till Task List will become empty. The logging stage is added to this process to estimate designed schedule quality and simplify debug process. Log analysis is performed on PC in offline mode and consists of two stages (see Fig. 3). After processing on the stage #1 Task List log information is sending to PC. On stage #2, after log analysis and making a decision about necessary changes on Task List, the device restarts and changes applied before processing Task List. After downloading new log information the conclusions about successfulness of applied changes should be made.

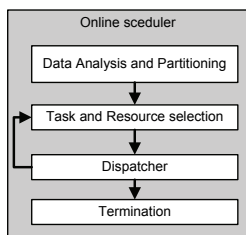


Fig. 2. Online scheduler  
Rys. 2. Schemat programu do tworzenia on line harmonogramu zadań

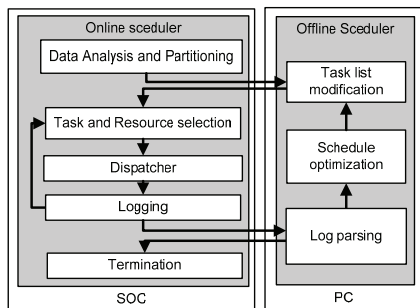


Fig. 3. Online and offline schedulers in cooperative mode  
Rys. 3. Współpraca programów pracujących online i offline przy tworzeniu harmonogramów zadań

### 3. Mathematical model of computational process

The source data for the digital signal transformation algorithm, used during base station operation, consists of following information:

- Set of tasks  $W$  and specified dependency relation: for each task  $\omega \in W$  corresponds certain subset  $P\omega$  of its dependents. Meanwhile, for some tasks,  $P\omega = e$ .
- For each task are assigned: non negative integer value of priority  $\varphi_\omega$ , resource type index  $r_\omega$ , run time  $t_\omega$  and unique key  $k_\omega$ . This key is used to avoid uncertainty during task sorting.
- Set of available in SOC resources is known beforehand and includes information about all resource type count  $R = \{R_0, R_1, \dots, R_i\}$ . A simplest way to visualize task list information is to put it as directed graph  $\langle M, N, T \rangle$  where  $M$  – tasks,  $N$  – dependency relation,  $T$  – mapping of set  $N$  to direct product  $M \times M$ , correlates each dependency  $j \in N$  in ordered tasks pair, first of which is dependent on second. This graph  $G_1 = \langle M, N, T \rangle$  can provide visual information about Task List topology and is used to check source data for loop absence.

In practice, task list visualization as  $G_1$  graph sometimes becomes inconvenient. Due to “arrows mess” graph topology can't be observed and it makes this visualization useless.

To avoid this, it was decided to represent Task List considering tasks as arcs. In this case task's start and stop events will be nodes in the new graph  $G_2$ . New graph  $G_2 = \langle M', N', T' \rangle$  creation needs more time and computational resources but this way of visualization is free of previous method disadvantages and much more usable.

### 4. Scheduling Algorithms

The current problem of the tasks assignment to specific processors is an NP-complete and only can be solved with heuristics [2]. On the other hand real time mode processing resource-intensive algorithms can't be used. So, the scheduler implements several allocations algorithms to minimize the possibility of not finding a schedule. The algorithms 1, 2 and 3 can be used in online mode; the algorithm 4 can be implemented on

Personal Computer (PC) only due to its high computational resource requirements.

#### Algorithm #1: Simple

This algorithm follows two step processes: first assigns the task to resources and second schedules the tasks on each processor using uniprocessor algorithms to guarantee minimum computational resources requirements for scheduling. The algorithm is run every time when a scheduler is invoked and a task is completed.

#### Algorithm #2: Critical path based

Any delays for critical tasks are the cause of increasing overall schedule latency. To avoid this lets set task priorities grounds on task time slack. So tasks belong to critical path will be run first and to reduce delay possibility for critical path. Critical path calculation can be performed in advance using SOC or PC calculating resources.

#### Algorithm #3: Critical path based with resource reservation

In some cases algorithm #2 can be mistaken because of no reservation resources mechanism for critical tasks. Adding such check to algorithm logic will reduce delay possibility for critical path tasks but also will require additional computational resources.

#### Algorithm #4: Genetic

To found suboptimal solution the genetic algorithm was used for task assignment. It is a type of stochastic algorithms that involves heuristic methods using evolutionary mechanism to search and select suboptimal solutions. It is proved as good solution for the current problem [3]. The algorithm scheme is shown on Fig. 4.

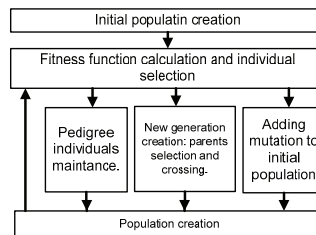


Fig. 4. Genetic algorithm scheme  
Rys. 4. Schemat algorytmu genetycznego

**Initial population creation** generates with setting random priorities and adding some random additional dependencies to initial task list. Adding on this stage to population individual based on algorithm #2 will reduce number of iteration to found suboptimal solution but for results visualization such individuals were not added when calculating.

The time of designed schedule is used as objective function (OF). This time was calculated using algorithm #1. So OF can be written as

$$O(\varphi_0, \varphi_1, \dots, \varphi_n, r_0, r_1, \dots, r_n, P_0, P_1, \dots, P_n, P_0', P_1', \dots, P_n')$$

where  $\varphi$  - task priorities,  $r$  - task indexes,  $P$  - dependencies,  $P'$  - additional dependencies. In terms of objective function two genes types can be defined - task priority  $\varphi$  and additional dependencies  $P'$ . The set of these two genes makes chromosome.

To provide variability for population lets define **mutation** as changing on one gene within chromosome. Task that going to be added as new dependency should have upper level in multilevel graph, according to current task to avoid loops. Next function is used to provide **parent selection** during crossing stage: 80% of parent selected from 20% individuals that have best OF, 10% from 10% individuals that have worst OF and 10% of others. During **crossing** combination of genes from both parents is used to produce new individual. To avoid regression **pedigree individuals maintains** stage is added. Small number of individual with best value of OF is frozen and not be involved in mutation process. Experience has shown that number of such individual should be 0.05% from population size but not less than 1. Genetic algorithm

stops when feasible solution is found or population degradation is detected. Also it can be limited by time or generations size.

After algorithm #4 has completed not only schedule parameters can be used as a result but the best individual chromosome with information about task priorities and additional dependencies can be also used. Applying this information on initial task list will cause decreasing schedule latency using algorithm #2 in online mode. This process is shown on Fig. 5.

## 5. Outcome of experiment

Defined algorithms were implemented using C and C# languages as part of "Transcede 4G Base Station Processor" development process. The series of experiments were done for the algorithms efficiency analysis and setting up its base parameters such as mutation occurrence probability, population size, crossings number and pedigree individuals quantity.

Series of 32 tasks lists produced during WIMAX frame generation were used as test samples. In addition one task list was taken from LTE frame generation. This sample is notable by high paralleling abilities. All tasks list uses two types of resources and consists of from 97 to 1087 tasks and from 116 to 87317 dependencies.

On Fig. 5 are shown computing results when number of first type resources are 2 and number of second type resources are 4 for algorithms #2, #3 and #4 against algorithm #1. For genetic algorithm population of 200 individuals was used and computation stopped on 150<sup>th</sup> generation.

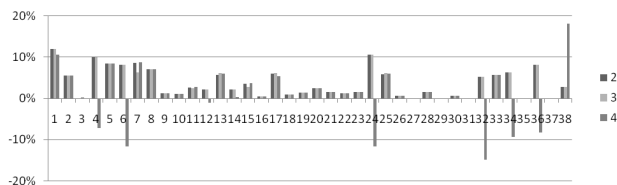


Fig. 5. Algorithms 2, 3 and 4 results considering algorithm 1 result as 100%  
Rys. 5. Wyniki algorytmu 2, 3 i 4 przy założeniu, że wyniki algorytmu 1 stanowią 100%

Algorithms #2 and #3 always show the same or better results than algorithm #1. In most cases algorithm #3 shows the same result as #2 but sometimes deference can be up to 5%. For sample 4, genetic algorithm shows worse result, but with increasing population size to 1000 individuals and generations number to 500 the result becomes the same as for algorithm #2. See Fig. 6. Best solution was found on 378<sup>th</sup> generation and stays the same for 2000 next generations. Similar result was received for other cases when algorithm #4 shows results worse than #2. In all cases population size and number of generation increase allows to get the same or better result against #2 and #3 algorithms. The significant results must be noted and it is shown by genetic algorithm for sample with good paralleling abilities (see sample 38) even for small population size. Eventually for all samples algorithm #4 shows the same or better result among others, but at the important parameter, computing time, is increasing. For example, for sample 4, schedule length 413 was found using algorithm #2 for less than 1 second but finding individual with the same objective function by algorithm #4 takes more than 3 hours.

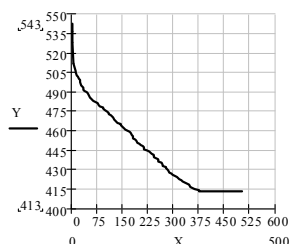


Fig. 6. Sample 4, population 1000, best objective function 413  
Rys. 6. Przykład 4, populacja 1000, najlepsza funkcja po 413 generacji

On Fig. 7 was shown best, worst and average result for population during all computing process. Population degradation can be found for this case on 170<sup>th</sup> generation. So, the situation when best objective function becomes equal to the average value for population can be interpreted as the sign that further computation is not reasonable.

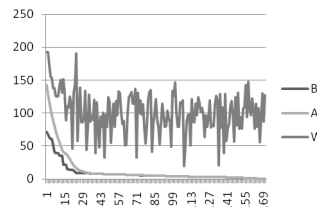


Fig. 7. Sample 13, population 200, best objective function 1734  
Rys. 7. Przykład 13, populacja 200, najlepsza funkcja po 1734 generacji

Computation performed for the cases with more resources number shows that with increasing of available resources number all algorithms shows better results and these results trend to critical path value. On the contrary, with decreasing number of available resources algorithm results trend to sum of all tasks length.

Experience has shown that next parameters should be chosen for efficiency of genetic algorithm: If tasks number in tasks list is  $N$  therefore population size should be  $N \times 3$ , mutation number per generation  $N \times 2$ , number of pair for crossing  $N \times 0.6$ , number of descendants for each pair 2, and getting the result close to optimal will take  $N = 1.5$  iterations.

## 6. Conclusions

For solving the task of schedule design suggested and implemented are following:

- Mathematical model of computational process using node and arrow diagram methods.
- These model analysis and transformation methods for providing visualization of computational process.
- Four types of scheduling algorithms, three of which can be implemented in real time mode and one, which is resource intensive, can be used to found suboptimal solution in offline mode.
- Implemented genetic algorithm, that allows finding schedule close to optimal and use task list parameters obtained during computation to make algorithms running in online mode, get the same result.
- Experiments for more than 30 samples were performed for different number of available resources. Genetic algorithm parameters that help to take better results on shorter computing time found.

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