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CHANGE CAPACITY AND FRICTION FORCE IN SLIDE JOURNAL BEARING BY TORSIONAL SHAFT VIBRATION

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Abstract

This paper shows results of numerical solutions an modified Reynolds equations for laminar unsteady oil flow in slide journal bearing gap. Laminar unsteady oil flow is performed during periodic and unperiodic perturbations of bearing load or is caused by the changes of gap height in time. During modelling crossbar bearing operations in combustion engines, bearing movement perturbations from engine vertical vibrations causes velocity flow perturbations of lubricating oil on the shaft in the circumferential direction. This solution example apply to isothermal bearing model with infinity length. Lubricating oil used in this model has Newtonian properties and constant dynamic viscosity. Results are presented in the dimensionless hydrodynamic pressure and tangential tension distribution diagrams. Diagrams also presents capacity and friction force change during the time of velocity perturbations. Received solutions were compared with the solution received by the stationary lubrication flow in the slide journal bearing, which were made with the same parameter assumption by constant dynamic oil viscosity. Isothermal bearing model is similar to friction node model by steady-state heat load conditions. Described effect can be used as on example of modeling the bearing friction node operations in reciprocating movement during exploitation of engines and machines.

Keywords: laminar unsteady lubrication, journal bearing, pressure, capacity and friction forces

1. Introduction

This article refer to the unsteady, laminar flows issue, in which modified Reynolds number Re* is [5],[6] smaller or equal to 2. Laminar, unsteady oil flow is performed during periodic and unperiodic perturbations of bearing load or is caused by the changes of gap height in the time. Above perturbations occur mostly during the starting and stopping of machine. Lubricated oil disturbance velocity the pin and on the bearing shell was also consider in the article. Reynolds equation system describing Newtonian oil flow in the gap of transversal slide bearing was discussed in the articles [4],[5]. Velocity perturbations of oil lubricated flow on the journal can be caused by torsion journal vibrations during the rotary movement of the shaft. Perturbations are proportional to torsion vibration amplitude, frequent constraint and to journal radius of the shaft. Oil velocity perturbations on the shell surface can be caused by rotary vibration of the shell together with bearing casing. This movement can be consider as kinematical constraint for whole bearing friction node. Isothermal bearing model can be approximate to bearing operation in friction node under steady thermal load conditions for example bearing in generating set on ship.

2. Hydrodynamic pressure and capacity forces

The unsteady, laminar and isotherm flow Newtonian oil in journal bearing gap is described for modified Reynolds equation [1],[2] from Newtonian oil with constant and variable dynamic viscosity depended for pressure. In considered model we assume small unsteady disturbances and in order to maintain the laminar flow, oil velocity V_i^* and pressure p_1^* are total of dependent quantities \widetilde{V}_i ; \widetilde{p}_1 and independent quantities V_i ; p_1 from time [4], [6] according to equation (1).

$$V_i^* = V_i + \widetilde{V}_i$$
, $p_I^* = p_I + \widetilde{p}_I$, $i = 1, 2, 3$ (1)

Unsteady components of dimensionless oil velocity and pressure are [4] in following form of infinite series:

$$\widetilde{V}_{i}(\varphi, r_{1}, z_{1}, t_{1}) = \sum_{k=1}^{\infty} V_{i}^{(k)}(\varphi, r_{1}, z_{1}) exp(jk\omega_{0}t_{0}t_{1}) \qquad i=1,2,3$$

$$\widetilde{p}_{I}(\varphi, r_{1}, z_{1}, t_{1}) = \sum_{k=1}^{\infty} p_{I}^{(k)}(\varphi, r_{1}, z_{1}) exp(jk\omega_{0}t_{0}t_{1}) \qquad (2)$$

where:

 ω_0 – angular velocity perturbations in unsteady flow,

j - imaginary unit $j = \sqrt{-1}$.

Components of oil velocity V_{ϕ} , V_r , V_z in cylindrical co-ordinates r, ϕ ,z have presented as V_1 , V_2 , V_3 in dimensionless [1] form:

$$V_{\varphi} = UV_{1} \qquad V_{r} = \psi UV_{2} \qquad V_{z} = \frac{U}{L_{1}}V_{3}$$
(3)

where:

U – peripheral journal velocity $U=\omega R$,

 ω – angular journal velocity,

R – radius of the journal,

 ψ - dimensionless radial clearance ($10^{-4} \le \psi \le 10^{-3}$),

2b – length of bearing,

 L_1 – dimensionless bearing length,

 ε – radial clearance :

$$\psi = \frac{\varepsilon}{R} \; ; \qquad \qquad L_I = \frac{b}{R} \tag{4}$$

Putting following quantities [1],[5]: dimensionless values density ρ_1 , hydrodynamic pressure p_1^* , time t_1 , longitudinal gap height h_1 , radial co-ordinate r_1 and co-ordinate z_1 .

$$\rho = \rho_0 \, \rho_1 \,, \qquad p = p_0 \, p_1 \,, \qquad t = t_0 \, t_1$$

$$z = b \, z_1 \,, \qquad r = R(1 + \psi r_1) \,, \qquad h = \varepsilon h_1$$
(5)

Rule of putting dimensionless velocity and pressure quantities in unsteady and steady part of the flow stays similar. Following symbols with bottom zero index signify density ρ_0 , dynamic viscosity η_0 , pressure p_0 and time t_0 describe characteristic dimension values assigned to adequate quantities. Reynolds number Re , modified Reynolds number Re* are in form [1]:

$$p_0 = \frac{U\eta_0}{\psi^2 R}$$
; $Re = \frac{U\rho_0 \psi R}{\eta_0}$; $Re^* = \psi Re$; (6)

The equation solution Reynolds equation [2],[3] with disturbances of peripheral velocity V_{10} on the journal for bearing with infinity length determine unsteady dimensionless hydrodynamic pressure function \tilde{p}_1 in following form:

$$\tilde{p}_{1} = \frac{1}{2} \rho_{1} R e^{*} n \gamma_{V} V_{10} \left(\varphi - h_{1e}^{3} \int_{0}^{\varphi} \frac{d\varphi}{h_{1}^{3}} \right) \sum_{k=1}^{\infty} A_{(k)} - \gamma_{V} p_{10} V_{10} \sum_{k=1}^{\infty} B_{(k)}$$
(7)

where:

h₁ - height of gap,

 h_{1e} - height of gap by film ended $\phi = \phi_e$,

 λ - eccentricity ratio.

$$h_l(\varphi) = l + \lambda \cos \varphi$$
; $h_{1e} = h_1(\varphi_e)$ (8)

Quantity γ_V are factor of scale for velocity perturbations, dependent for acceptant of term series (2). Pressure p_{10} is located in the oil gap by steady flow and by constant oil dynamic viscosity. Sum for series $\sum_{k=1}^{\infty} A_k$ and $\sum_{k=1}^{\infty} B_k$ in right side of Reynolds solution equation (7) are results from conservation of the momentum solutions and were define in work [1],[2].

$$\sum_{k=1}^{\infty} A_{(k)} = \sum_{k=1}^{\infty} \frac{\sin(k\omega_{0}t_{0}t_{1})}{k} = \begin{cases} \frac{\pi - \omega_{0}t_{0}t_{1}}{2} & 0 < t_{1} < 1\\ 0 & t_{1} = 0; 1 \end{cases}$$

$$\sum_{k=1}^{\infty} B_{(k)} = \sum_{k=1}^{\infty} \frac{\cos(k\omega_{0}t_{0}t_{1})}{k^{2}} = \frac{1}{4} \left[(\pi - \omega_{0}t_{0}t_{1})^{2} - \frac{\pi^{2}}{3} \right] \quad 0 \le t_{1} \le 1$$
(9)

In presented calculation way an expression value is assumed $n\rho_1Re^*=12$, what is approximately equivalent to force over first frequency torsion vibrations force of six cylinder engine shaft. Examples apply to bearing with constant dependent eccentricity $\lambda=0,6$. In case where oil velocity perturbations are caused by forced vibrations of engine then the number n in equation (7) define multiplication of perturbation frequency ω_0 to angular velocity of engine crankshaft ω . Multiplication factor n is equal to number of cylinder c in two-stroke engine (s=2) or in four-stroke engine (s=4) to number of cylinders c/2:

$$n = \frac{\omega_0}{\omega} = \begin{cases} c & s = 2\\ \frac{c}{2} & s = 4 \end{cases} \tag{10}$$

We analyst cylindrical bearing infinite length with circumferential velocity perturbations on the journal V_{10} . Circumferential velocity perturbations are caused by torsional vibrations shaft (on the journal). In the further numerical analysis relation time t_0 was taken into account as a propagation period of axial velocity perturbation of lubricating oil.

Four velocities perturbations will analysed in this article. Pressure perturbation \tilde{p}_1 course in point ϕ =160° presented Fig.1 by following circumferential velocity perturbations on the journal V₁₀=

0,01; 0,025; 0,05; 0,075. Changes of pressure \tilde{p}_1 are asymmetrical in relation to the time. The growth of the pressure is smaller than his fall. Sizes these grow when the size of the perturbations of the velocity grows up.

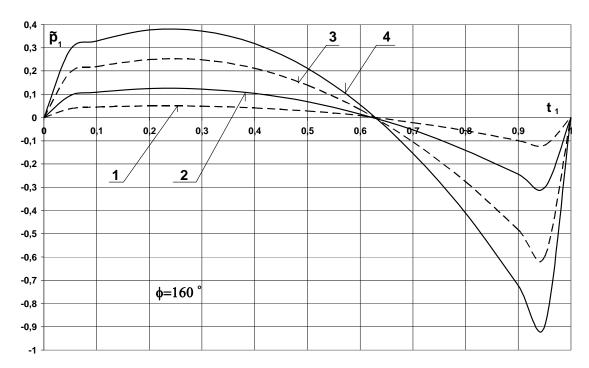


Fig.1. Pressure distributions \tilde{p}_1 in place $\varphi=160^\circ$ in the time t_1 by velocity perturbations: 1) $V_{10}=0,01$; $V_{1h}=0$; 2) $V_{10}=0,025$; $V_{1h}=0$; 3) $V_{10}=0,05$; $V_{1h}=0$; 4) $V_{10}=0,075$; $V_{1h}=0$

Capacity force W for cylindrical slide journal bearing has following components W_x and W_y to be determined [2],[6] in the local co-ordinate systems in Fig. 2. Capacity force W is resultant force from concurrent pressure forces configuration.

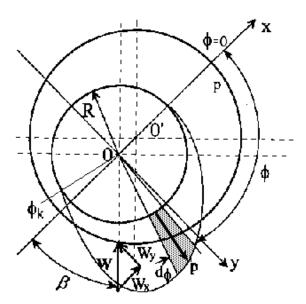


Fig. 2. Capacity force W and components W_x and W_y in the local co-ordinate system

Thus dimensionless components W_{1x} and W_{1y} of capacity forces W_1 are as follows [2]:

$$W_{Ix} = \frac{W_x}{W_0} = -\int_0^{\varphi_k} p_I \cos\varphi \, d\varphi; \qquad W_{Iy} = \frac{W_y}{W_0} = -\int_0^{\varphi_k} p_I \sin\varphi \, d\varphi \tag{11}$$

$$W_1 = \sqrt{W_{Ix}^2 + W_{Iy}^2} = \frac{W}{W_0}$$

where:

 W_0 - characteristic value of capacity force $W_0 = 2Rbp_0$

Hydrodynamic capacity force change caused by the pressure perturbation is calculate from:

$$\widetilde{W}_{1} = W_{1}^{*} - W_{1}$$

$$W_{1}^{*} = W_{1}(p_{1}^{*}) ; W_{1} = W_{1}(p_{1})$$
(12)

where:

Pressure in the bearing during the perturbation is a total of stationary flow pressure and perturbation pressure according to (1) According to mentioned equation [2] if we provide stationary flow pressure p_1 we will obtain capacity force W_1 . Figure 3 also presents change capacity calculation results by four oil viscosity perturbations. Hydrodynamic capacity force \tilde{W}_I changes periodically with a period equal to perturbation velocity. In case of velocity perturbation in the bearing pin, increase of capacity force above the stationary condition value last no longer than half of the perturbation period and the increase of capacity force is bigger than the decrease in the remaining time.

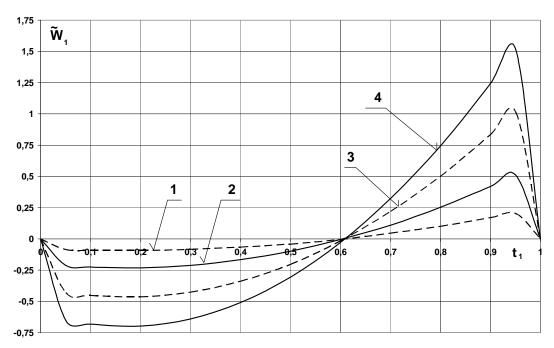


Fig.3. Change the dimensionless capacity forces \widetilde{W}_1 in the time t_1 by velocity perturbations: 1) V_{10} =0,01; 2) V_{10} =0,025; 3) V_{10} =0,05; 4) V_{10} =0,075;

increase of capacity force than decrease. It is opposite in case of oil peripheral velocity perturbation on the shell surface, but his diagrams are not presented in his article. Capacity force

course in time is not symmetrical for different perturbation of velocity quantities on the pin. The fall of change the capacity force is smaller than his growth. Sizes these grow when the size of the perturbations of the velocity grows up.

3. Elementary friction force and friction force in bearing gap

Elementary friction forces τ and this change $\tilde{\tau}$ for dimension an dimensionless form $\tilde{\tau}_I$, we calculated as tangential stress (pressure) by newtonian oil in formula:

$$\tau = \eta \frac{\partial V_{\varphi}}{\partial r} \bigg|_{r=h}; \quad \tau_{I} = \eta_{I} \frac{\partial V_{I}}{\partial r_{I}} \bigg|_{r_{I}=h_{I}}; \quad \widetilde{\tau}_{I} = \eta_{I} \frac{\partial \widetilde{V}_{I}}{\partial r_{I}} \bigg|_{r_{I}=h_{I}};$$

$$\tau = p_{0} \psi \tau_{I} = \tau_{0} \tau_{I}; \quad \tau_{0} = \psi p_{0}$$

$$(13)$$

Velocity circumferential perturbation (7) [3] are in formula:

$$\widetilde{V}_{I} = \frac{6\eta_{I}}{\rho_{I}Re^{*}n}\gamma_{V}V_{I0}\frac{h_{I}-h_{Ie}}{h_{I}^{3}}\sum_{k=I}^{\infty}\frac{P(k)}{k^{3}}\cos(2k\pi t_{I}) + \gamma_{V}V_{I0}\sum_{k=I}^{\infty}\frac{A(k)}{k^{2}}\cos(2k\pi t_{I}) + \frac{\gamma_{V}V_{I0}}{2}\sum_{k=I}^{\infty}\frac{A(k)}{k^{2}}\cos(2k\pi t_{I}) + \frac{\gamma_{V}V_{I0}}{2}\sum_{k=I}^{\infty}\frac{A(k)}{2}\cos(2k\pi t_{I}) + \frac{\gamma_{V}V_{I0}}{2}\sum_{k=I}^{\infty}\frac{A(k)}{2}\sum_{k=I}^{\infty}\frac{A(k)}{2}\cos(2k\pi t_{I}) + \frac{\gamma_{V}V_{I0}}{2}\sum_{k=I}^{\infty}\frac{A(k)}{2}\sum_{k=I}^{\infty}\frac{A(k)}{2}\sum_{k=I}^{\infty}\frac$$

Components of series P(k), A(k) i B(k) from formula (14) are in following forms [3]:

$$P(k) = \frac{\sin(sh_{1}X_{k}) \sinh((1-s)h_{1}X_{k}] + \sin((1-s)h_{1}X_{k}] \sinh(sh_{1}X_{k})}{\cosh(sh_{1}X_{k}) + \cos(sh_{1}X_{k})}$$

$$A(k) = \frac{-\cosh(sh_{1}X_{k}) \cos((2-s)h_{1}X_{k}] + \cosh((2-s)h_{1}X_{k}] \cos(sh_{1}X_{k})}{\cosh(2h_{1}X_{k}) - \cos(2h_{1}X_{k})}$$

$$s = \frac{r_{1}}{h_{1}}; \quad \gamma_{V} = \frac{6}{\pi^{2}}; \quad X_{k} = \sqrt{k\frac{\rho_{1}}{2\eta_{1}}Re^{*}n} \qquad k=1,2,3.....$$
(15)

Additional symbol s marking dimensionless parameter height of gap ($0 \le s \le 1$). In numerical calculation example oil with constant density was assume, what is equivalent to quantity ρ_1 .

$$\frac{\partial \tilde{V}_{I}}{\partial r_{I}}\Big|_{r_{I}=h_{I}} = \frac{6\eta_{I}}{\rho_{I}Re^{*}n}\gamma_{V}V_{I0}\frac{h_{I}-h_{Ie}}{h_{I}^{3}}\sum_{k=I}^{\infty}\frac{P'(k)}{k^{3}}\cos(2k\pi t_{I}) + \gamma_{V}V_{I0}\sum_{k=I}^{\infty}\frac{A'(k)}{k^{2}}\cos(2k\pi t_{I}) + \frac{\gamma_{V}V_{I0}}{2}\sum_{k=I}^{\infty}\frac{A'(k)}{k^{2}}\cos(2k\pi t_{I}) + \frac{\gamma_{V}V_{I0}}{2}\sum_{k=I}^{\infty}\frac{A'(k)}{2}\cos(2k\pi t_{I}) + \frac{\gamma_{V}V_{I0}}{2}\sum_{k=I}^{\infty}\frac{A'(k)}{2}\sum_{k=I}^{\infty}\frac{A'(k)}{2}\cos(2k\pi t_{I}) + \frac{\gamma_{V}V_{I0}}{2}\sum_{k=I}^{\infty}\frac{A'(k)}{2}\sum_{k=I}^{\infty}\frac{A$$

where:

$$P'(k) = \frac{dP(k)}{dr_l}\bigg|_{r_l = h_l} = -X_k \frac{\sin(h_l X_k) + \sinh(h_l X_k)}{\cosh(h_l X_k) + \cos(h_l X_k)}$$

$$A'(k) = \frac{dA(k)}{dr_{l}}\Big|_{r_{l}=h_{l}} = -2X_{k} \frac{\sinh(h_{l}X_{k})\cos(h_{l}X_{k}) + \cosh(rh_{l}X_{k})\sin(h_{l}X_{k})}{\cosh(2h_{l}X_{k}) - \cos(2h_{l}X_{k})}$$
(17)

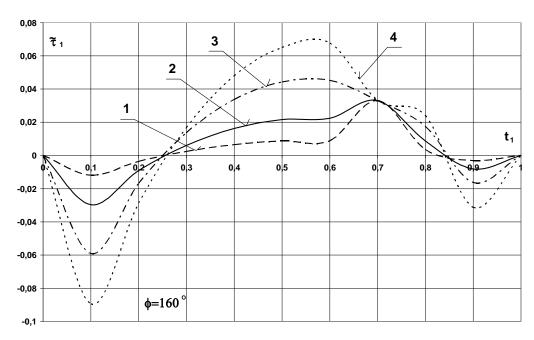


Fig.4. Tangential pressure distributions $\tilde{\tau}_1$ in place φ =160° in the time t_1 by velocity perturbations:1) V_{10} =0,01; 2) V_{10} =0,025; 3) V_{10} =0,05; 4) V_{10} =0,075

The results change tangential pressure $\tilde{\tau}_I$ distribution in the time t_1 show Fig. 4. in place of coordinate ϕ =160°. Change elementary friction forces (tangential pressure) $\tilde{\tau}_I$ perturbation are values different sign from initial perturbations V_{10} and absolutely lesser.

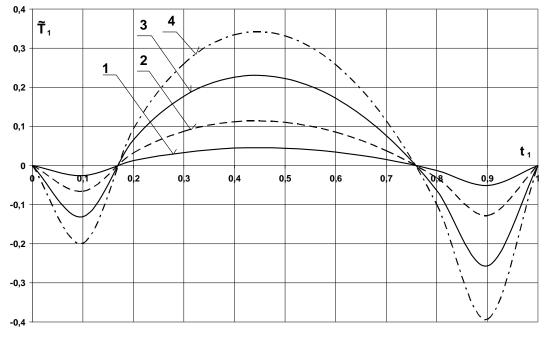


Fig.5. Change the dimensionless friction forces \widetilde{T}_l in the time t_l by velocity

Friction forces T and this change \tilde{T} for dimension an dimensionless form \tilde{T}_I , we calculated as sum tangential stress (pressure) in circumference co-ordinate bearing by formula:

$$\widetilde{T} = \int_{0}^{\varphi_{e}} Rb \, \eta \, \frac{\partial \widetilde{V}_{\varphi}}{\partial r} \Big|_{r=h} d\varphi = T_{0} \widetilde{T}_{I}$$

$$\widetilde{T}_{I} = \int_{0}^{\varphi_{e}} \widetilde{\tau}_{I}(\varphi) d\varphi$$
(18)

where:

 T_0 - characteristic value of friction force $T_0 = W_0 \psi$

In Fig. 5 presented change the dimensionless friction forces \tilde{T}_I in the time t_1 by four of velocity perturbation.

4. Conclusions

Presented Reynolds equation solution for unsteady laminar Newtonian flow of lubricated oil to enable initial opinion to hydrodynamic pressure, elementary friction pressure distribution and capacity, friction forces as a basic slide bearing operating parameter. Unsteady velocity perturbation on the journal and sleeve effect on capacity and friction forces in lubricated gap. Capacity and friction forces variation in bearing have periodical character equal to periodical velocity perturbation time and this variations value and character depend on type of perturbation. Author is aware of simplifications that were assumed in presented model which apply to Newtonian oil and to isothermal bearing model. Despite that presented calculation example apply to bearing with infinity length, obtained conclusions can be useful to elementary friction pressure and friction forces distribution by laminar, unsteady lubrication of cylindrical slide bearing with finite length.

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