

UNIwersytet Technologiczno-Przyrodniczy
IM. JANA I JĘDRZEJA ŚNIADECKICH W BYDGOSZCZY
ZESZYTY NAUKOWE NR 251
ELEKTROTECHNIKA 13 (2008), 37-55

PRESENTATION OF THE DC MACHINE SIMULTANOUSLY BUT SEPARATELY CONTROLLED BY TWO VOLTAGES USING THE STATE-SPACE METHOD

Roman Żarnowski

Electrical Machines and Drives Group
Department of Electrical Engineering,
University of Technology and Life Sciences
Al. S. Kaliskiego 7, 85-796 Bydgoszcz, Poland

Summary: The following paper presents the DC machine working as a motor, described by means of the state-space method. A computer model of the machine, compiled in the MATLAB/SIMULINK[®] environment is described as well. This model takes into account the phenomenon of dynamic inductance in the excitation circuit of the DC machine. This study presents also a comparison between the conventional (linearized) model and the model with a magnetization curve analytically approximated by the arc cotangent function. State trajectories are presented against a background of static characteristics occurring here in the form of a steady-state surface (SSS). The computer model compiled may be used to determine optimal control of these voltages in accordance with the quality coefficient employed.

Keywords: DC machine controlled by two voltages

1. INTRODUCTION

Modern methods of optimization are based on the state-space method [1,6], which excels over classic methods and holds many advantages. The classic control theory is convenient in designing a single input-output system. However modern control theory, which is based on the state-space method, allows for examination of systems subjected to control of signals pertaining to a broad class of input signals, not only in the impulse, step or sinusoidal form. As distinguished from classic methods, the state-space method allows for start and end conditions of the system. The vector-matrix notation simplifies solving of differential equations. However, apart from simple calculations, it is necessary to use a computer, what requires knowledge of numerical values of parameters of the object.

This article describes movement of a drive system based on a direct current motor by the means of the space-state method. For heed establishing, simulations were carried out for a test DC machine – model PZB632a with rated of nominal power 0.8 kW, armature voltage 220 V, armature current 4,6 A, excitation current 0,24 A and nominal rotations 1500 rpm. Simulations were prepared under the assumption of four load types occurring in engineering practice. During model assembly, almost all machine

parameters were varied, which allows modeling of a broad class of DC machines, from small machines up to large mine hoist motors. Results are presented in a new and unexpected manner, i.e. in the form of a steady-state surface (SSS). The state vector movement is presented against the background of this surface.

2. MATHEMATICAL MODEL

This model allows for taking into account the dynamic inductance phenomenon of the machine excitation circuit [2, 9]. It may, therefore, present an accurate description of the phenomena occurring in DC machine. However, simplifying assumptions does not make allowances for the following:

- a) a voltage drop across the brushes,
- b) inducing a flux screening the main flux under the influence of fast, dynamic changes of armature current,
- c) inaccuracies of machine compensation, and
- d) allowing for the character of the magnetization curve, (phenomenon of a machine magnetic core material hysteresis is omitted).

On the basis of the generalized machine model, the following DC machine equations were derived [8]:

$$\left. \begin{aligned} \frac{d\Psi_{sd}(t)}{dt} &= U_{sd}(t) - \frac{1}{T_{sd}}\Psi_{sd}(t) \\ \frac{d\Psi_{wq}(t)}{dt} &= U_{wq}(t) - \omega(t)\Psi_{wsd}(t) - \frac{1}{T_{wq}}\Psi_{wq}(t) \\ \frac{d\omega(t)}{dt} &= \frac{1}{JL_{wq}}\Psi_{wq}(t)\Psi_{wd}(t) - \frac{1}{J}M_{op}(t) \end{aligned} \right\} \quad (1)$$

The variable presented in these equations Ψ_{wsd} can be formulated through Ψ_{sd} as follows:

$$\Psi_{wsd} = \frac{M_{wsd}}{L_{sd}}\Psi_{sd} = \alpha\Psi_{sd} \quad , \quad (2)$$

where:

- α – ratio, constant of the machine
- Ψ_{sd} – stator flux linkage in d axis,
- Ψ_{wq} – rotor flux linkage in q axis,
- Ψ_{wsd} – stator in relation to the rotor flux linkage in d axis, and
- L_{wq} , M_{wsd} , T_{sd} , ω , J , M_{op} respectively: inductance of armature in q axis, inductance of armature in relation to stator in d axis, average time-constant of excitation circuit, angular velocity, moment of inertia, resistance torque.

For marking simplification, the following equations were assumed (Fig. 1.):

$$\left. \begin{aligned} \Psi_{sd} &= \Psi_m; U_{sd} = U_m \\ \Psi_{wq} &= \Psi_t; U_{wq} = U_t \\ L_{wq} &= L_t; T_{wq} = T_t \\ T_{sd} &= T_m \end{aligned} \right\} \quad (3)$$

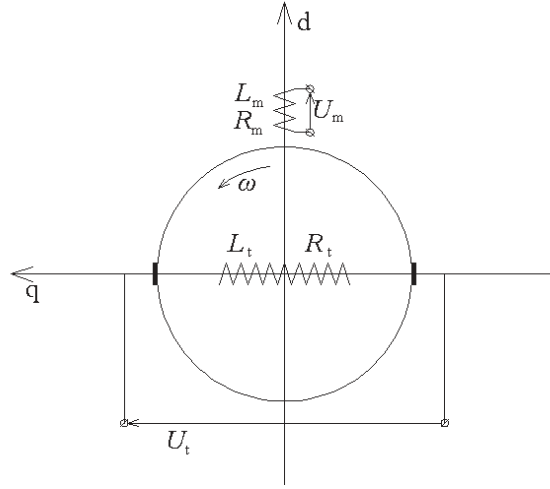


Fig. 1. DC machine diagram

Arranging equations (1) against new designations, the following results were acquired:

$$\frac{d}{dt} \begin{bmatrix} \Psi_m(t) \\ \Psi_t(t) \\ \omega(t) \end{bmatrix} = \begin{bmatrix} U_m(t) - \frac{1}{T_m} \Psi_m(t) \\ U_t(t) - \alpha \omega(t) \Psi_m(t) - \frac{1}{T_t} \Psi_t(t) \\ \frac{\alpha}{J L_t} \Psi_m(t) \Psi_t(t) - \frac{1}{J} M_{op}(t) \end{bmatrix}, \quad (4)$$

$$\frac{d}{dt} \begin{bmatrix} \Psi_m(t) \\ \Psi_t(t) \\ \omega(t) \end{bmatrix} = f(U_m(t), U_t(t), M_{op}(t), \Psi_m(t), \Psi_t(t), \omega(t)), \quad (5)$$

where: $\mathbf{f} = \begin{bmatrix} f_1 \\ f_2 \\ f_3 \end{bmatrix}$ is a vector function of the abovementioned arguments, and

$\Psi_m(t), \Psi_t(t), \omega(t)$ are state vector coordinates. The nonlinear vector-matrix equation (4) constitutes a base for further considerations.

3. MODEL TECHNIQUE IN *SIMULINK*[®]

A comparison of two DC machine models is presented below. A simplified model was built with the assumption, that inductance of the excitation circuit is not undergoing alteration under the influence of the excitation current, and, therefore, is formed by equations (4).

State trajectory equations, allowing for dynamic inductance, were derived on the basis of the following procedure.

The abovementioned equation:

$$U_m = R_m i_m + \frac{d\Psi_m}{dt}, \quad (6)$$

after an analysis of a which DC excitation circuit with a ferromagnetic material, the magnetization curve was approximated by an arc cotangent curve of the following parameters a_0, a_1, a_2 :

$$\Psi(i_m) = (a_0^* \cdot \text{arctg}(a_1 i_m) + a_2^* i_m) \quad a_0^*, a_2^* = \frac{a_0}{\alpha}, \frac{a_2}{\alpha}, \quad (7)$$

assumes a new form:

$$\left. \begin{aligned} \frac{d\Psi_m}{dt} &= \left(\frac{a_0^* a_1}{1 + (a_1 i_m)^2} + a_2^* \right) \frac{di_m}{dt} \\ \frac{di_m}{dt} &= \frac{U_m - R_m i_m}{\frac{a_0^* a_1}{1 + (a_1 i_m)^2} + a_2^*} \\ \frac{di_m}{dt} &= \frac{(1 + (a_1 i_m)^2)(U_m - R_m i_m)}{a_0^* a_1 + a_2^* (1 + (a_1 i_m)^2)} \end{aligned} \right\} \quad (8)$$

Therefore:

$$\frac{d}{dt} \begin{bmatrix} i_m(t) \\ \Psi_t(t) \\ \omega(t) \end{bmatrix} = \begin{bmatrix} \frac{(1 + (a_1 i_m)^2)(U_m - R_m i_m)}{a_0^* a_1 + a_2^* (1 + (a_1 i_m)^2)} \\ U_t(t) - \alpha \omega(t) \Psi_m(t) - \frac{1}{T_t} \Psi_t(t) \\ \frac{\alpha}{J L_t} \Psi_m(t) \Psi_t(t) - \frac{1}{J} M_{op}(t) \end{bmatrix}. \quad (9)$$

Factors a_0 , a_1 , a_2 , were determined in the examination of the test machine. From the examination, a function course was directly assigned and assumed $\alpha\Psi_m = f(i_m)$. The result of this trial is presented on Fig. 2.

Ratio α , in the equations, was determined on the basis of the assumption that in the no-load conditions the following relationships are fulfilled:

$$\alpha = \frac{U_t - i_t R_t}{\omega \Psi_m}; i_t = 0 \quad (10)$$

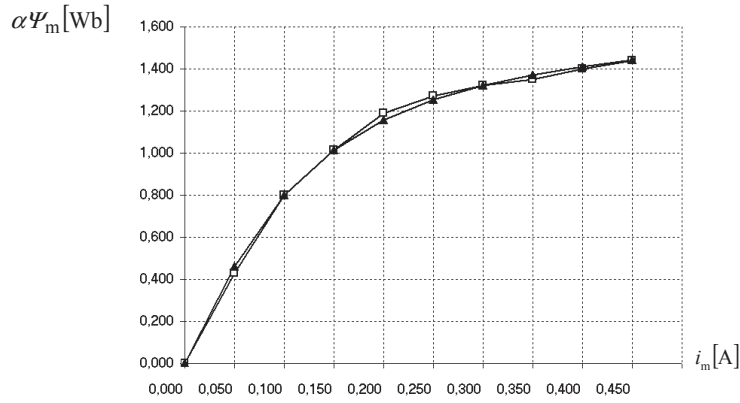


Fig. 2. Function course $\alpha\Psi_m = (a_0 \cdot \arctg(a_1 i_m) + a_2 i_m)$; factors a_0 , a_1 , a_2 amount to, respectively: 1.083; 9.078; 0.002.

The value of excitation circuit temporal constant T_{msr} might be accepted as an average, given by the manufacturer and amounting to 27ms for this machine. Then, for the machine considered, α amounts to 0.3.

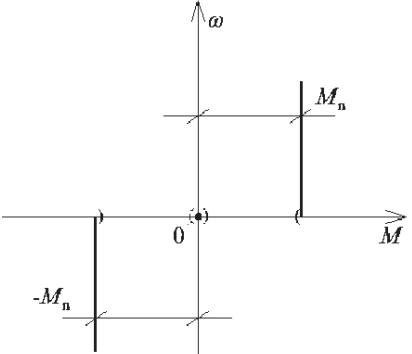
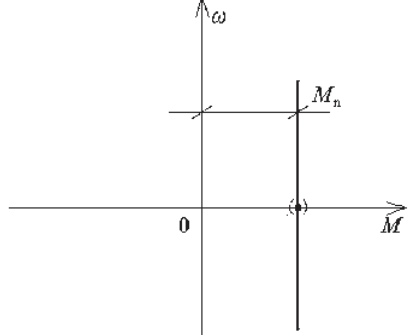
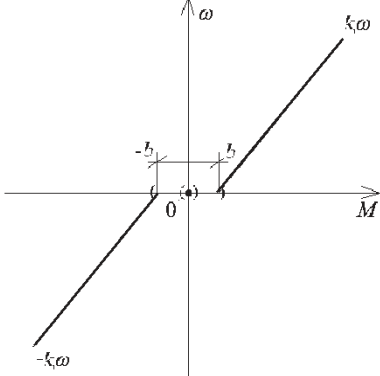
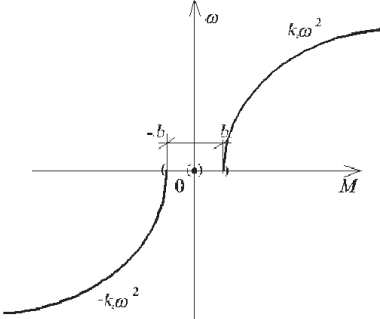
3.1. DISTURBANCES INFLUENCING MACHINE WORK

A number of disturbance classes influencing the machine were considered. The resistance torques, which frequently occur in engineering, are: active resistance torque, generator torque, fan torque, and constant passive torque. These four aspects of load torques may be described by one equation, the versions of which are presented below.

The shape and course of the SSS directly depends upon the course and values of a resistance torque on the shaft. Assuming that operation of a resistance torque, of one of the aforementioned aspects, occurs, it is possible to determine a state-space surface for each of them. Such an approach towards the matter indicates that a specified SSS corresponds to a resistance torque of a chosen class.

$$M(\omega) = \text{sign}(\omega) (b + ak\omega^\gamma), \quad \gamma \in \{0, 1, 2\}, \quad (11)$$

where: resistance torque load ratio $a = \frac{M_{op}}{M_n}$, value of initial friction torque b , factor of proportionality between resistance torque and angle velocity k .

Characteristic of torque	Equation	Type
	$M(\omega) = \text{sign}(\omega) a M_n$ $k = 1,$ $\gamma = 0,$ $b = 0,$ $M(0) = 0$	<p>Passive constant resistance torque</p>
	$M(\omega) = a M_n$ $k = 1,$ $\gamma = 0,$ $b = 0,$ $M(0) = M_n$	<p>Active constant resistance torque (crane torque)</p>
	$M(\omega) = \text{sign}(\omega)(b + a k_1 \omega)$ $k_1 > 0,$ $\gamma = 1,$ $b > 0,$ $M(0) = 0$	<p>Passive generator resistance torque</p>
	$M(\omega) = \text{sign}(\omega)(b + a k_2 \omega^2)$ $k_2 > 0,$ $\gamma = 2,$ $b > 0,$ $M(0) = 0$	<p>Passive fan resistance torque</p>

State trajectory depends on start and end conditions. The application, while altering voltage U_m and U_t in the external and internal loop enables plotting of these surfaces.

The case of active resistance torque

$$\left. \begin{aligned} \Psi_m &= a_0^* \cdot \operatorname{arctg}\left(\frac{U_m a_1}{R_m}\right) + a_2^* \frac{U_m}{R_m} \\ \Psi_t &= \frac{L_t M_{op}}{\alpha \Psi_m} \\ \omega &= \frac{U_m - \Psi_t / T_t}{\alpha \Psi_m} \end{aligned} \right\} \quad (12)$$

The case of generator resistance torque and passive constant resistance torque ($k_1 = 0, b = M_{op}$)

The SSS course of the active resistance torque proceeds according to the following equalities:

$$M_{op} = \operatorname{sign}(\omega)(b + ak_1\omega), \text{ where: } \operatorname{sign}(\omega) = \operatorname{sign}(U_m U_t) \quad (13)$$

Therefore:

$$\left. \begin{aligned} \Psi_m &= a_0^* \cdot \operatorname{arctg}\left(\frac{U_m a_1}{R_m}\right) + a_2^* \frac{U_m}{R_m} \\ \Psi_t &= \frac{L_t \cdot \operatorname{sign}(U_m U_t)(b + ak_1\omega)}{\alpha \alpha_1} \\ \omega &= \left(1 + \frac{R_t ak_1 \cdot \operatorname{sign}(U_m U_t)}{(\alpha \Psi_m)^2}\right)^{-1} \left(\frac{U_t}{\alpha \Psi_m} - \frac{R_t b \cdot \operatorname{sign}(U_m U_t)}{(\alpha \Psi_m)^2}\right) \end{aligned} \right\} \quad (14)$$

The case of fan resistance torque

The SSS course of the active resistance torque was determined according to the following equations:

$$M_{op} = \operatorname{sign}(\omega)(b + ak_2\omega^2) \quad (15)$$

Finally:

$$\left. \begin{aligned} \Psi_m &= a_0^* \cdot \operatorname{arctg}\left(\frac{U_m a_1}{R_m}\right) + a_2^* \frac{U_m}{R_m} \\ \Psi_t &= \frac{L_t \cdot \operatorname{sign}(U_m U_t)(b + ak_1 x_3)}{\alpha \alpha_1} \\ \omega &= \frac{-1 + \operatorname{sign}(U_m U_t) \sqrt{4pq + I}}{2p} \end{aligned} \right\} \quad (16)$$

where:

$$\begin{aligned} \text{sign}(\omega) \frac{R_1 a k_2}{(\alpha \Psi_m)^2} &= p, \\ \frac{U_2}{\alpha \Psi_m} - \frac{R_1 \cdot \text{sign}(\omega) b}{(\alpha \Psi_m)^2} &= q \end{aligned}$$

The first coordinate of the state vector Ψ_m indicates the linkage flux in the excitation circuit and, the state trajectory, allowing for dynamic inductance, is calculated [7] in relation to magnetizing current i_m . It is necessary, therefore, to establish initial conditions of the integrator, in relation to this current. The current i_m determination for the given Ψ_m from equation (8) is not possible due to function implisiting. In this case, for the given current, Ψ_m the value of the current i_m is determined iteratively each time on the basis of the following calculation:

$$\Psi_m = a_0^* \cdot \text{arctg} \left(\frac{U_m a_1}{R_m} \right) + a_2^* \frac{U_m}{R_m} \quad (17)$$

After appropriate conversions we have equation:

$$\text{tg} \left(\frac{\Psi_m - a_2^* i_m}{a_0^*} \right) - a_1 i_m = \varepsilon_m \quad (18)$$

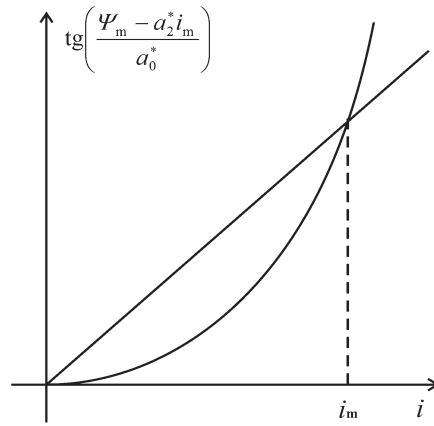


Fig. 3. Interpretation of iterative method of magnetizing current determination, accurate to ε_m (here employed accuracy of: 0.0000001)

Solving this allows for creating a model [3, 4, 5], which, as author argues, presents courses of a real DC machine in a rather accurate manner.

The block diagram in *SIMULINK*[®] corresponding to the vector equation of state trajectory (9)

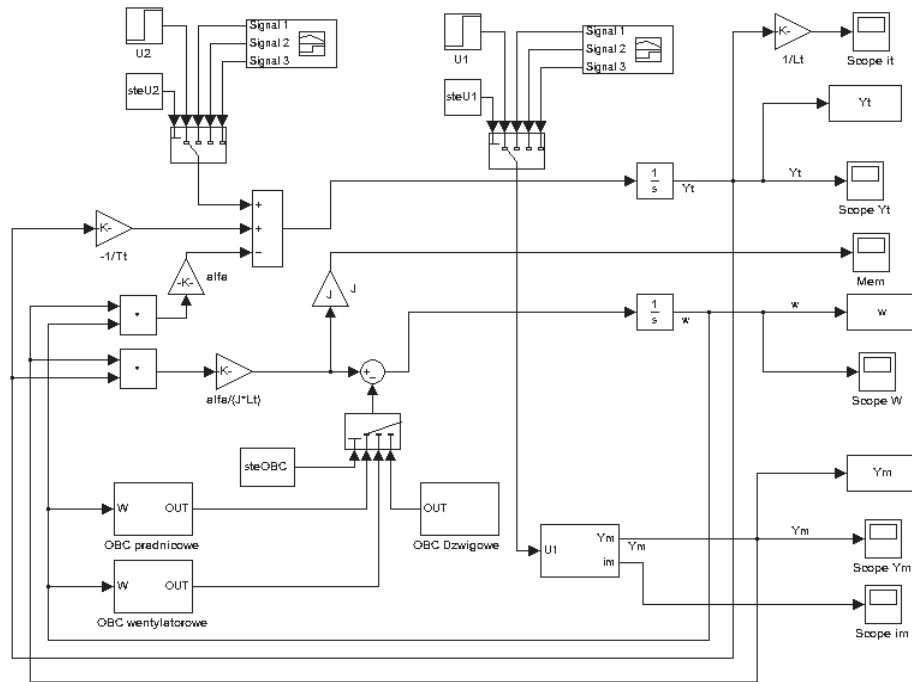
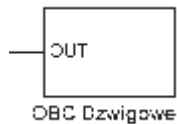


Fig. 4. Block diagram of the DC machine allowing for dynamic inductance of excitation circuit, where $Y_t = \Psi_t$, $Y_m = \Psi_m$, $w = \omega$.

Diagrams included in blocks.



This element includes a hidden diagram presented in Fig. 5.

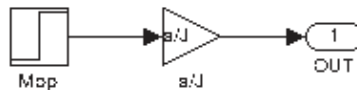


Fig. 5. Active resistance torque simulation diagram.



This element includes a hidden diagram presented in Fig. 6.

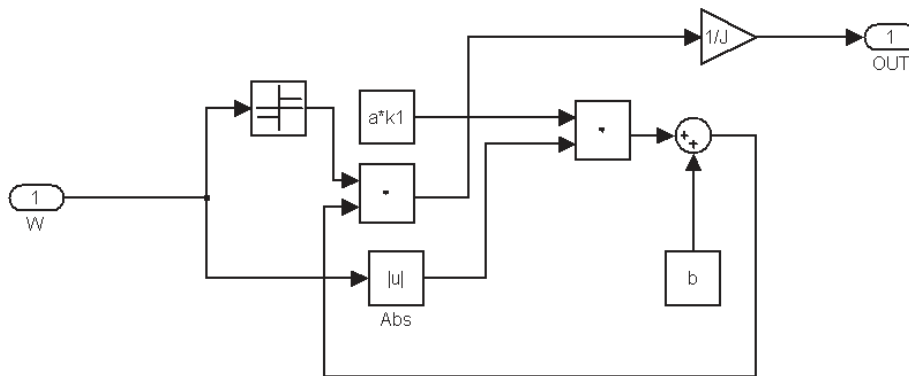
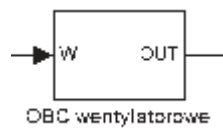


Fig. 6. Generator torque simulation diagram.



This element includes a hidden diagram presented in Fig. 7.

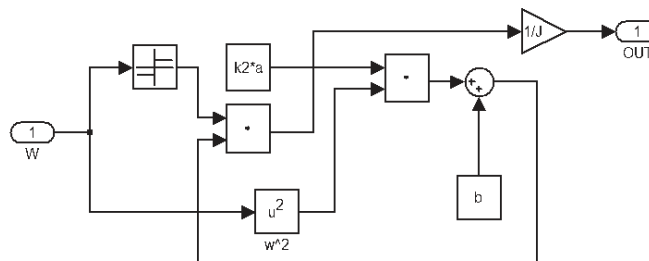
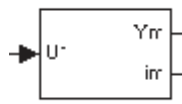


Fig. 7. Fan torque simulation diagram.



The block contains the first trajectory equation for the case taking into account dynamic inductance. The input quantity is a signal of U_m , the output signals are: Ψ_m and i_m . The internal diagram is presented in Fig. 8.

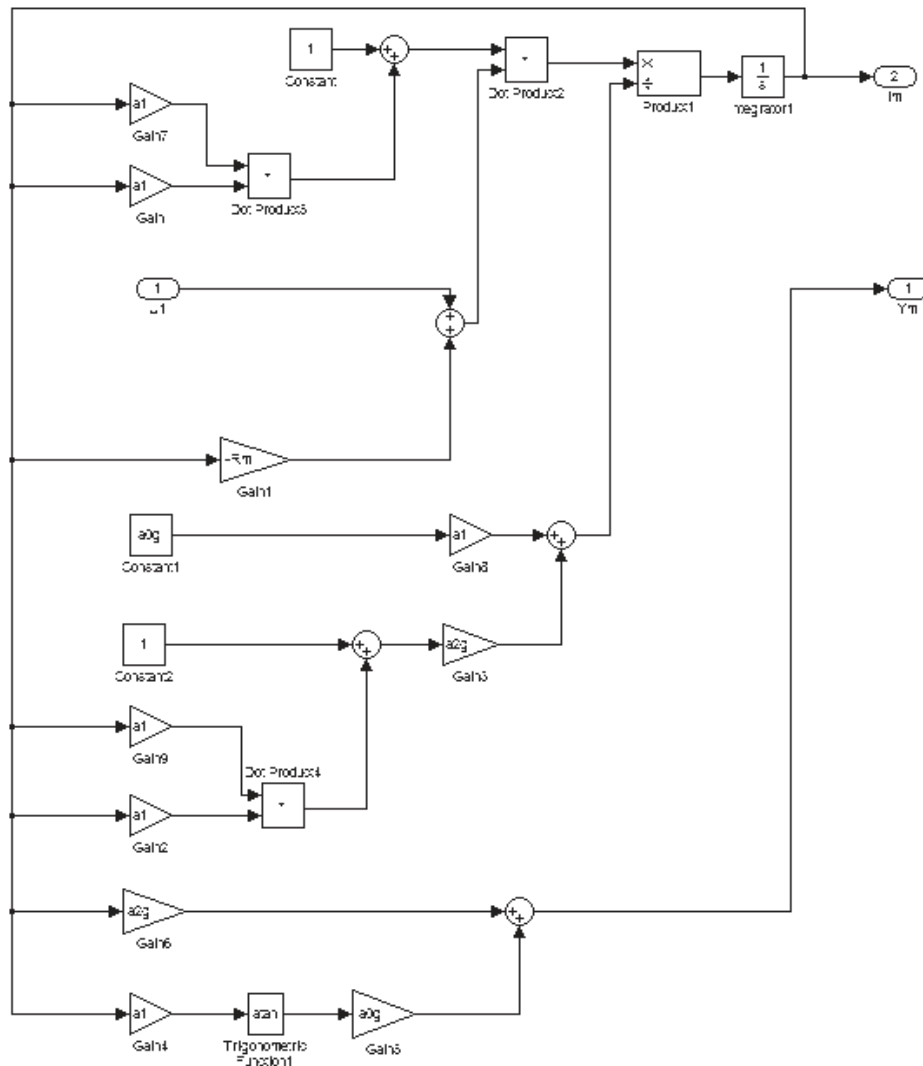
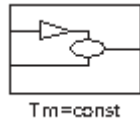


Fig. 8. Excitation circuit simulation diagram of the DC machine allowing for dynamic inductance of excitation circuit.



The interior of the block includes state equations for the linearized circuit, i.e. omitting dynamic inductance. The simulation diagram can be activated in a separate window. This element is included in the diagram presented in Fig. 9.

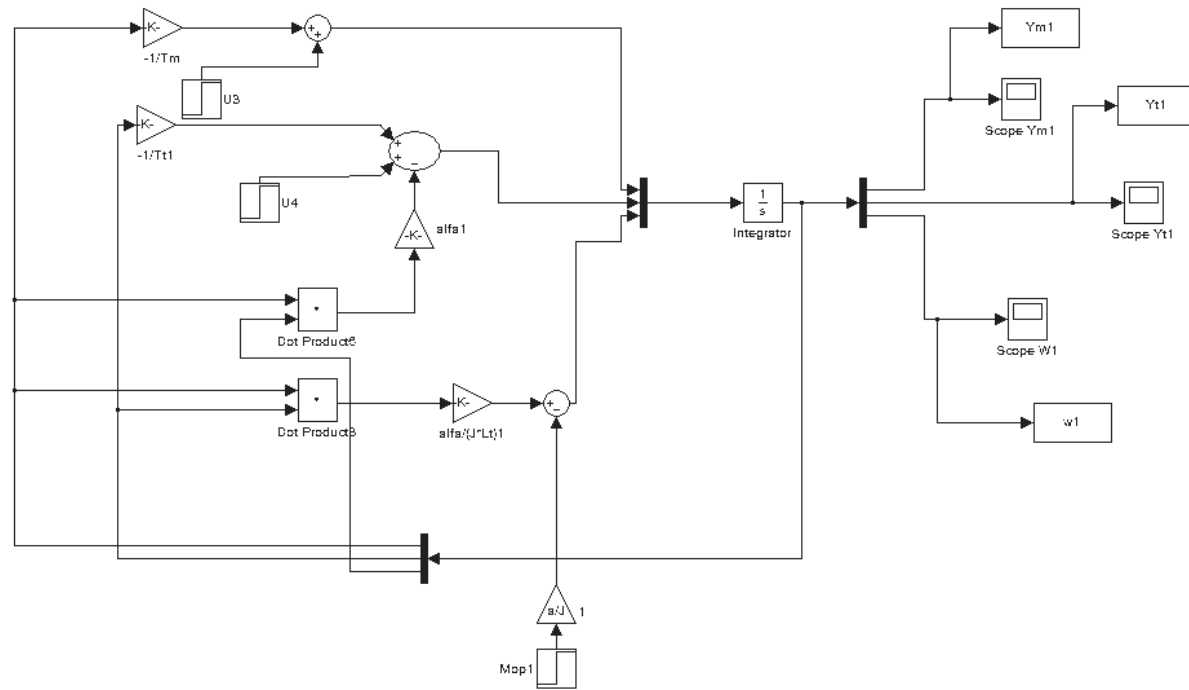


Fig. 9. Excitation circuit simulation diagram of a DC machine with linearized magnetization curve.

Diagram parameters used in calculations are listed in the following table:

Parameter	Value
Mn [Nm] =	5.1
Rm [Ohm] =	726.29
Li [H] =	0.01284
Rt [Ohm]=	4.28
Tm [s]=	0.019
U1n [V]=	230
U2n [V]=	230
alfa =	0.3
a0 =	1.0827
a1 =	9.0783
a2 =	0.002
J [kgm^2]=	0.010039
a (Mop=a*Mn) =	1
b (Mt=b*Mn) =	0.05
k1 [Nms]=	0.034
k2 [Nms^2]=	0.000226
U1 [V] =	0
U2 [V] =	0
steOBC (1-P,2-W,3-D)=	1
steU1 (1,2,3,4)=	1
steU2 (1,2,3,4)=	1
cw (1-1cw 2-4cw)	1

Buttons: OK and run, load

Rated torque
 Effective resistance of excitation circuit
 Inductance of armature circuit
 Effective resistance of armature circuit
 Aver. time-constant of excitation circuit
 Final excitation voltage
 Final armature voltage

Ratio, constant of the machine acc. to eq.(2)
 Magnetization curve shape fac.
 Magnetization curve shape fac.
 Magnetization curve shape fac.

Inertia moment of drive
 Relative load torque
 Relative load of an initial friction passive torque

Gen. torque factor acc. to Fig. 5
 Fan torque factor acc. to Fig. 6

Initial value of excitation volt.
 Initial value of armature volt.
 Load type choice (1- generator, 2- fan, 3- crane)
 Excitation voltage - choice of function course
 Armature voltage - choice of function course
 Chart illustration method choice (1 - in the first quarter, 2 - in four quarters)

Fig. 10. Method of introducing DC machine data to the simulation program.

4. DESCRIPTION OF SIMULATIONS

The test was performed by using the machine parameters obtained from laboratory studies. However, it is necessary to stress that this model is general enough to allow simulation and examination of any given DC machine.

The 3D chart presents the SSS in Fig. 15. Its color depends on the quarter in which the panel was placed; first quarter – red ($U_{m+} + i U_{r+}$); second quarter – yellow ($U_{m+} + i U_{r-}$); third quarter – blue ($U_{m-} + i U_{r-}$); fourth quarter – green ($U_{m-} + i U_{r+}$). The blue line in the chart presents the state trajectory. The next charts also present courses of each vector components versus time function.

Comparison of DC motor allowing for dynamic inductance in excitation circuit to DC machine allowing for static inductance

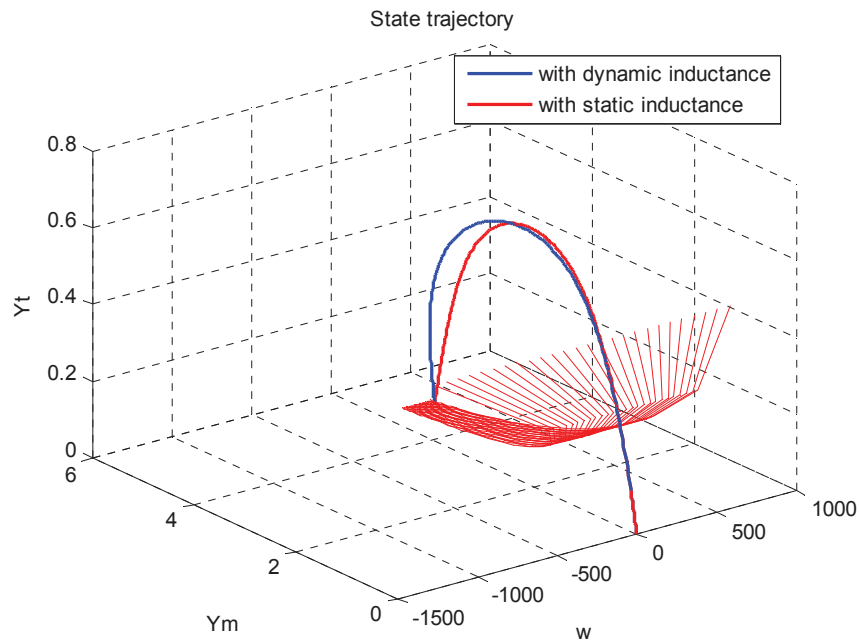


Fig. 11. Result of simulation comparison of a linearised model and a model allowing for changing inductance during start-up.

Fig. 11 presents the results of a comparison between two motor models, based on the trajectory course of the state, during machine start-up. While the red line is the course of the state vector, not allowing for excitation circuit dynamic inductance, the blue line is the response of the system allowing for nonlinearity of the magnetization curve in the machine magnetic core. The results of modeling were inserted for comparison purposes. Although static values of the state vector are the same, the transients differ from each other. Therefore, the model with dynamic inductance of the excitation circuit was assumed for further consideration.

The state trajectory of a motor, loaded with generator passive resistance torque, when start voltages are equal to $U_m = -100$, $U_t = -100$ V and end voltages are equal to $U_m = 230$, $U_t = 230$ V, is presented in Fig.12. Load torque is equal to rated motor torque.

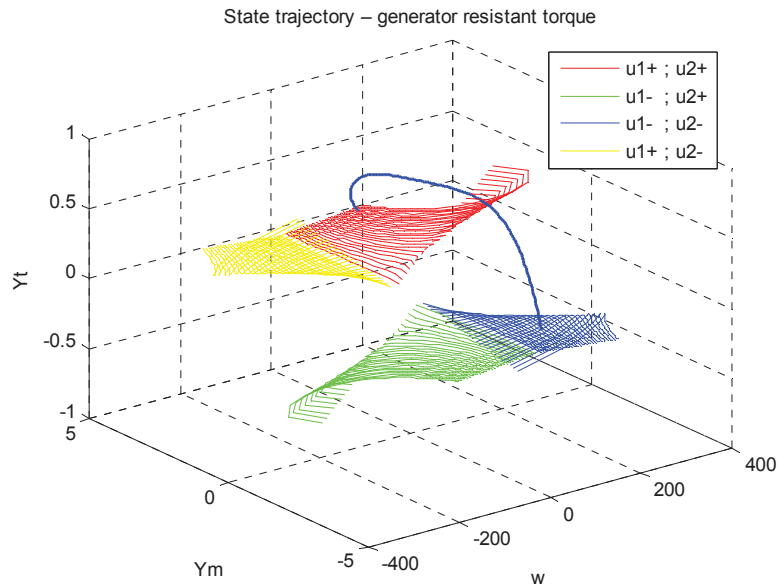


Fig. 12. State trajectory loaded with generator passive resistance torque, with initial voltages equal to $U_m = -100$ V, $U_t = -100$ V and end voltages equal to $U_m = 230$ V, $U_t = 230$ V presented in four quarters of the state surface. Load torque in steady state is equal to rated motor torque.

The state vector components alter the value of Ψ_m and Ψ_t from negative to positive. The shape of the SSS allows that the motor be loaded with the generator passive resistance torque. Courses of the state vector components Ψ_m , Ψ_t and ω , and useful variables such as armature current i_t and magnetizing current i_m are presented on figures 13÷16.

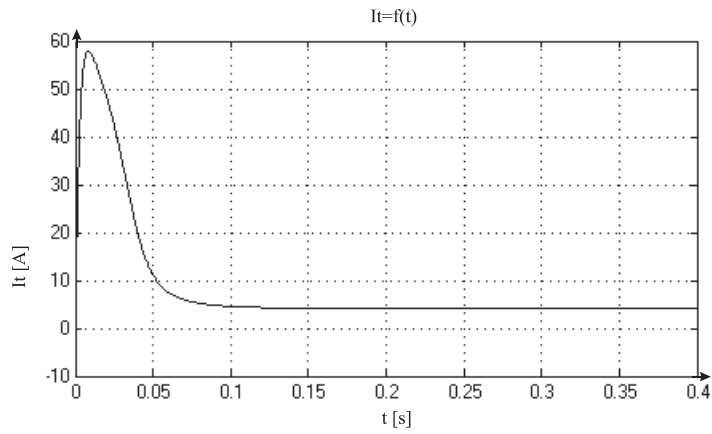


Fig. 13. Armature current course $i_t = f(t)$; machine loaded with generator passive resistance torque, with start voltages equal to $U_m = -100$ V, $U_t = -100$ V, and end voltages equal to $U_m = 230$ V, $U_t = 230$ V. Torque in steady state is equal to rated motor torque.

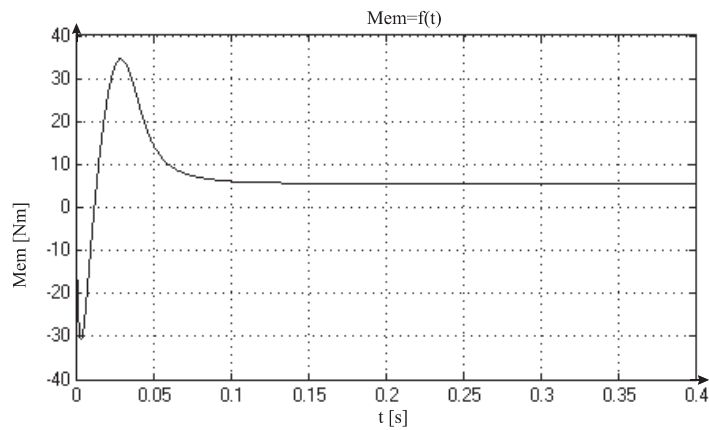


Fig. 14. Armature current course $M_{em} = f(t)$; machine loaded with generator passive resistance torque constant, with initial voltages equal to $U_m = -100$ V, $U_t = -100$ V, and end voltages equal to $U_m = 230$ V, $U_t = 230$ V. Load torque is equal to rated motor torque.

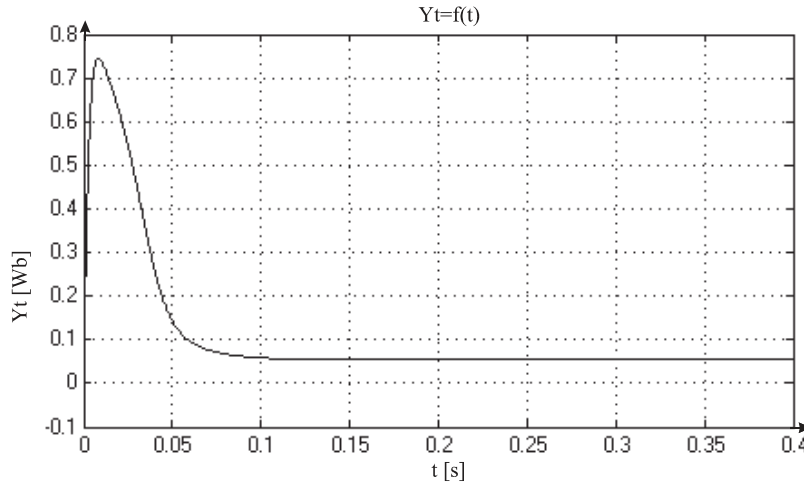


Fig. 15. Armature linkage flux course $\Psi_t = f(t)$; machine loaded with generator passive resistance torque, with initial voltages equal to $U_m = -100$ V, $U_t = -100$ V, and end voltages equal to $U_m = 230$ V, $U_t = 230$ V. Load torque is equal to rated motor torque

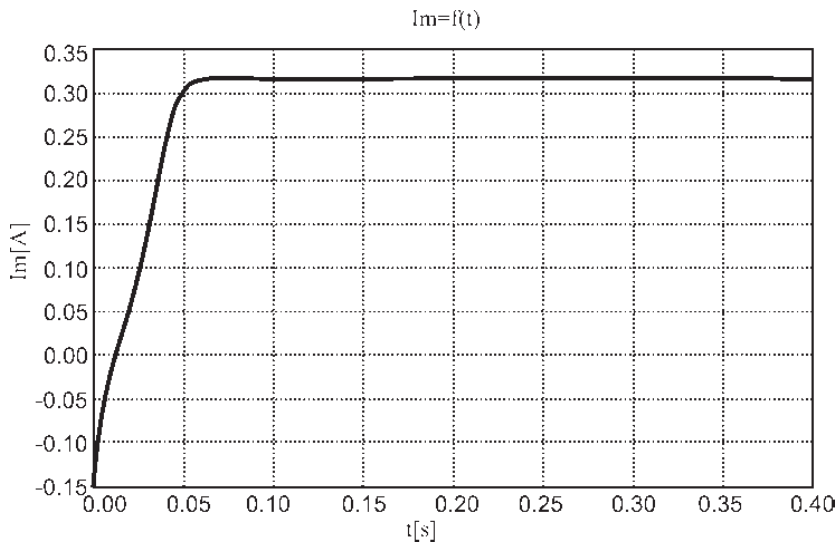


Fig. 16. Magnetizing current course in excitation circuit $i_t = f(t)$; during voltage alteration from -100V up to 220V. Approximated magnetizing curve is allowed

Another example of DC motor state trajectory loaded with nominal active resistance torque in steady state, with initial voltages equal to $U_m = 120$, $U_t = 120$ V, and end voltages equal to $U_m = 230$, $U_t = 230$ V is presented in Fig. 17.

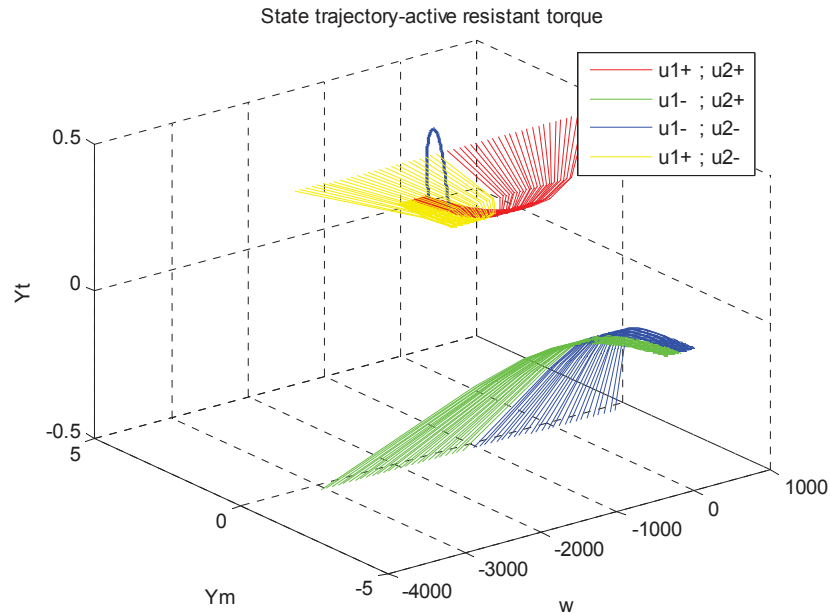


Fig. 17. State trajectories loaded with active resistance torque with start voltages $U_m = 120$, $U_t = 120$ V, and end voltages $U_m = 220$, $U_t = 220$ V presented in four quarters of the state surface. Load torque is equal to rated motor torque.

5. CONCLUSION

The article presents results of DC machine simulation based on the independent DC machine simulator, which is developed by the author. It has been illustrated, that the space-state method used in this simulations allows:

- magnetizing curve of this machine to be nonlinear. (approximated by arc cotangent function),
- introduce the dynamic inductance into DC machine excitation circuit calculations,
- to point noticeable differences in the state trajectory course between a linearized and nonlinear machine model,
- to find future methods for optimal motor control in accordance with the employed quality coefficient.

More-over,

- the state-space surface SSS is composed of four panels and it creates static characteristics in 3D space,
- courses of currents, linkage fluxes and angle velocity of the machine obtained on the basis of simulations confirm the courses available in literature.

This model is universal and enables carrying out simulations loaded with all types of basic load encountered in engineering practice. Motors from small up to large hoist ones, can be simulated, while making allowances for simplification of assumptions.

BIBLIOGRAPHY

- [1] Athans M., Falb P.L., 1966: *Sterowanie optymalne*, WNT Warszawa.
- [2] Hassane M., Djuoja S., Boudjemaa T., 1998: *Identification Parameters Method For DC machine Including Friction*. Power Electronics And Variable Speed Drives 21-23 Sept. 1998, Conf. Publication No 456, IEE.
- [3] Liang Y.C., Gosbell V., 2006: *Realistic Computer Model of DC Machine for CADA Topology on SPICE2*. School of Electrical Engineering, The University of Sydney, NSW, Australia [in] IEEE.
- [4] Liang Y.C., Gosbell V., 1990: *DC Machine Models for SPICE2 Simulation*. IEEE Trans. On Power Electronics, vol. 5. No I.
- [5] Mrozek B., Mrozek Z., 2004: *Matlab i Simulink - poradnik użytkownika*, Wydawnictwo HELION, Gliwice.
- [6] Ogata K., 1976: *Metody przestrzeni Stanów w teorii sterowania*, WNT, Warszawa.
- [7] Stachurski M., 2003: *Metody numeryczne w programie Matlab*, Wydawnictwo MIKOM, Warszawa.
- [8] Stein Z., 1971: *Maszyny elektryczne w automatyce*, Wydawnictwo Uczelniane Politechniki Poznańskiej, Poznań.
- [9] Trutt F.C., Erdplyi E.A., Hopkins R.E., 1968: *Representation of the Magnetization Characteristic of DC Machines for Computer Use*. IEEE Transactions on Power Apparatus And Systems, vol. PAS-87, No. 3.

PRZEDSTAWIENIE MASZYNY PRĄDU STAŁEGO
STEROWANEJ JEDNOCZEŚNIE DWOMA NAPIĘCIAMI
METODĄ PRZESTRZENI STANU

Streszczenie

W pracy przedstawiono maszynę DC pracującą jako silnik, opisaną metodą przestrzeni stanu. Zaprezentowano model komputerowy napisany przy pomocy programu MATLAB/SIMULINK®. Model ujmuje zjawisko indukcyjności dynamicznej obwodu wzbudzenia maszyny. Trajektorie stanu przedstawiono na tle charakterystyk statycznych występujących tu w postaci powierzchni stanów ustalonych (PSU). Ponadto porównano model konwencjonalny (zlinearyzowany) z modelem o charakterystyce magnesowania przybliżonej analitycznie funkcją arcustangens. Opracowany model komputerowy może zostać wykorzystany do wyznaczenia sterowania optymalnego, niezależnie dwoma napięciami, według przyjętego wskaźnika jakości.

Słowa kluczowe: maszyna DC sterowana jednocześnie dwoma napięciami