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**CORE DATA STATISTICAL ANALYSIS  
FOR NATURAL GAS RESERVOIRS  
FROM THE SOUTHERN PART OF TRANSYLVANIAN DEPRESSION**

**1. INTRODUCTION**

The analysis performed in this paper has the following targets:

- the statistical analysis of the main parameters of the rock (porosity, permeability) and of the rock-fluid system (gas saturation) determined from the cores of the natural gas reservoirs of the Southern part of Transylvanian Depression;
- fulfilment of some correlations between the parameters: porosity/gas saturation, porosity/permeability, gas saturation/permeability, porosity/depth, gas saturation/depth, permeability/depth, such as to be estimated average values for these parameters for the reservoirs that does not have so many analysis from cores;
- the presentation of the results obtained after the correlations between the parameters;
- a comparison between the resulted parameters from statistical analysis and the present parameters used in the volumetric estimation of the resources from the natural gas reservoirs.

**2. GENERAL DATA REGARDING THE PHYSICAL PARAMETERS  
DETERMINED FROM CORES**

In the Southern part of Transylvanian Depression there are 87 natural gas reservoirs and there were analysed 8401 de cores from Meotian, Pliocene, Sarmatian, Buglovian, Badenian, Helvetian, Eocene, Cretacic and Jurassic.

The number of cores analysed on each reservoir varies from 1 and 736. The cores were grouped on geological formations and the most important from the determination of the physical parameters point of view are: Badenian (3386 determinations), Buglovian (1896 determinations), Sarmatian (2460 determinations) and Pliocene (461 determinations).

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There are determinations of physical parameters in the geological formations situated under the Acvitanian salt in the cores taken from the few high depth wells: Eocene (82 determinations), Cretacic (49 determinations) and Jurassic (73 determinations).

The available data from the core analysis of the natural gas reservoirs in the Southern part of Transylvanian Depression are: effective porosity, permeability parallel with stratum, permeability perpendicular on stratum, water saturation, core salt content, water salt content, calcium carbonate content, specific gravity and grain-size analysis.

In this paper there were used for statistical analysis and correlations the physical parameters referring to the reservoir rock geometry, fluid saturation and fluid flow through rock properties: effective porosity, permeability parallel with stratum, permeability perpendicular on stratum, water saturation.

It was observed that there are missing from core analysis data referring to connate water saturation and there is available information on pores water saturation. In order to estimate the gas saturation it was considered that the water saturation determined in the lab is similar with the connate water saturation, ignoring the zero values only. There were eliminated from the initial data the zero values of the porosity and of the permeability.

The other data resulted from core analysis (core salt content, water salt content, calcium carbonate content, specific gravity and grain-size analysis) are not representative for the correlations with the physical parameters for natural gas resources estimation.

### **3. PROPOSED WORK IN ORDER TO KNOW THE PHYSICAL MODEL**

The main part of the gas reservoirs are already in the production period and plenty of them are even at the end of production. For these reservoirs is not required to know the physical model, as it is already contoured, based on production data and production history.

For the new discovered reservoirs, where the initial physical parameters can be determined, in order to know better the physical model at production starting, it is proposed to extract cores and to analyse the parameters as those are the only direct reservoir information. The main uncertainties of the core analysis come from the fact the obtained data are isolated, not continuous. From this reason, for a continuous description of the reservoir properties it is proposed the analysis of the geophysics properties, from complex well logs interpretation, 3 D seismic and well testing.

### **4. POROSITY-DEPTH CORRELATION**

The regression lines and the correlation coefficients for porosity-depth variation were determined for each reservoir, each geological formation and total gas reservoirs and total geological formations.

It was noticed a rather good porosity-depth correlation and generally porosity goes down when depth grows. The correlation coefficient is between  $-0.31$  (Sarmatian) and  $-0.57$  (Jurassic), on total formations. The worst porosity-depth correlation is for Pliocene, where the correlation coefficient is  $-0.02$ .

## 5. GAS SATURATION-DEPTH CORRELATION

The regression lines and the correlation coefficients for gas saturation-depth variation were determined for each reservoir, each geological formation and total gas reservoirs and total geological formations (Fig. 1).

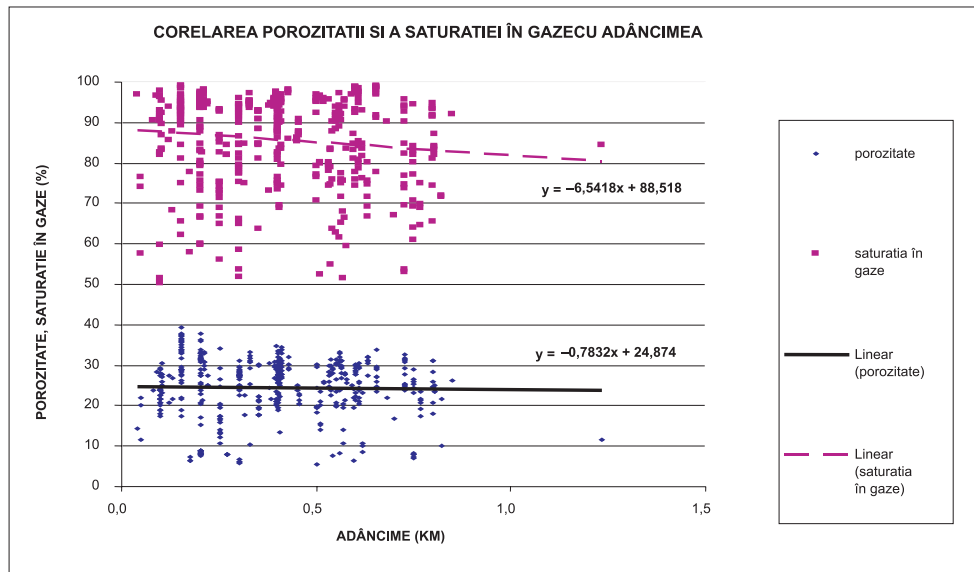


Fig. 1. Porosity and gas saturation – depth correlation for Pliocene

It was noticed a poor gas saturation-depth correlation and the correlation coefficient is between 0 (Sarmatian) and 0.12 (Pliocene), on total formations. The best gas saturation-depth correlation is for Eocene, where the correlation coefficient is  $-0.45$ .

## 6. PERMEABILITY-DEPTH CORRELATION

The regression lines and the correlation coefficients for both permeabilities-depth variations were determined for each reservoir, each geological formation and total gas reservoirs and total geological formations (Fig. 2).

It was noticed a rather good permeability parallel with stratum-depth correlation for Badenian, Eocene and Cretacic and the correlation coefficient is between  $-0.2$  and  $-0.64$  a poor correlation for the other geological formations where the correlation coefficient is between  $-0.07$  and  $-0.14$ , on total formations. The best permeability parallel with stratum-depth correlation is for Cretacic, where the correlation coefficient is  $-0.64$ .

It was observed that the permeability parallel with stratum-depth variation is different from permeability perpendicular on stratum-depth variation.

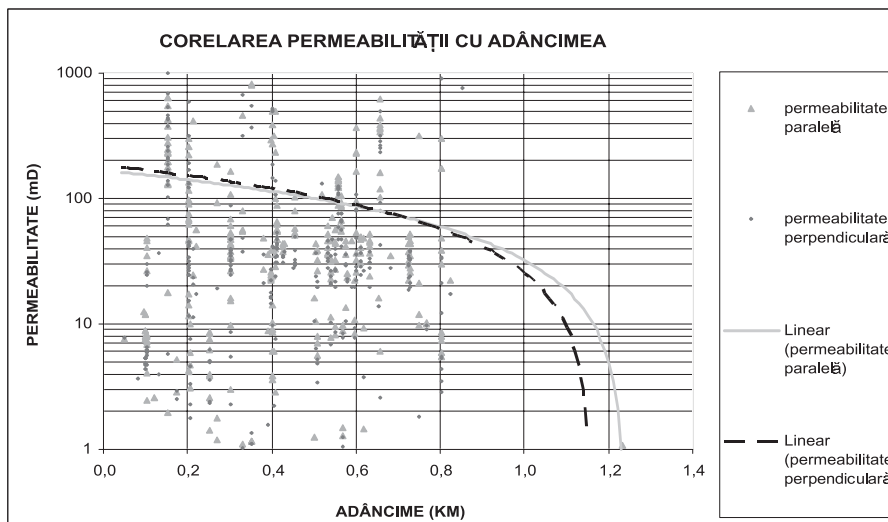


Fig. 2. Permeability-depth correlation for Pliocene

### 7. POROSITY-PERMEABILITY CORRELATION

There were determined the regression lines and the correlation coefficients for porosity-permeability parallel with stratum variation, for each reservoir, each geological formation and total gas reservoirs and total geological formations, as it is considered that the permeability parallel with stratum shows better the real situation in the gas reservoir.

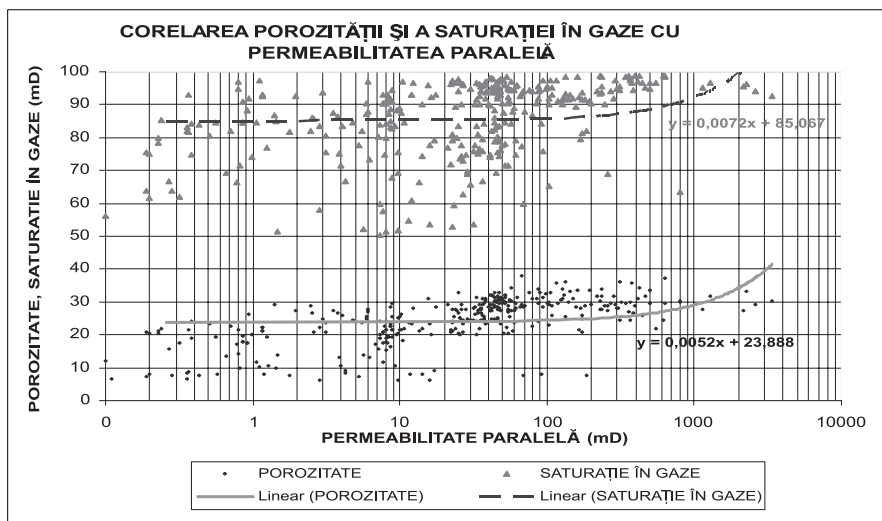


Fig. 3. Porosity and gas saturation – permeability parallel with stratum correlation for Pliocene

It was noticed a rather good porosity-permeability parallel with stratum correlation and generally permeability parallel with stratum grows when porosity grows. The correlation coefficient is between 0.24 (Pliocene, Buglovian) and 0.8 (Eocene, Cretacic), on total formations (Fig. 3).

## 8. GAS SATURATION-PERMEABILITY CORRELATION

There were determined the regression lines and the correlation coefficients for gas saturation-permeability parallel with stratum variation, for each reservoir, each geological formation and total gas reservoirs and total geological formations, as it is considered that the permeability parallel with stratum shows better the real situation in the gas reservoir.

It was noticed a rather good gas saturation-permeability parallel with stratum correlation and generally permeability parallel with stratum grows when gas saturation grows. The correlation coefficient is between 0.13 (Buglovian) and 0.84 (Jurassic), on total formations.

## 9. POROSITY-GAS SATURATION CORRELATION

The regression lines and the correlation coefficients for porosity-gas saturation variation were determined for each reservoir, each geological formation and total gas reservoirs and total geological formations (Fig. 4).

It was noticed a rather good porosity-gas saturation correlation and generally gas saturation grows when porosity grows. The correlation coefficient is between 0.23 (Cretacic) and 0.66 (Eocene), on total formations.

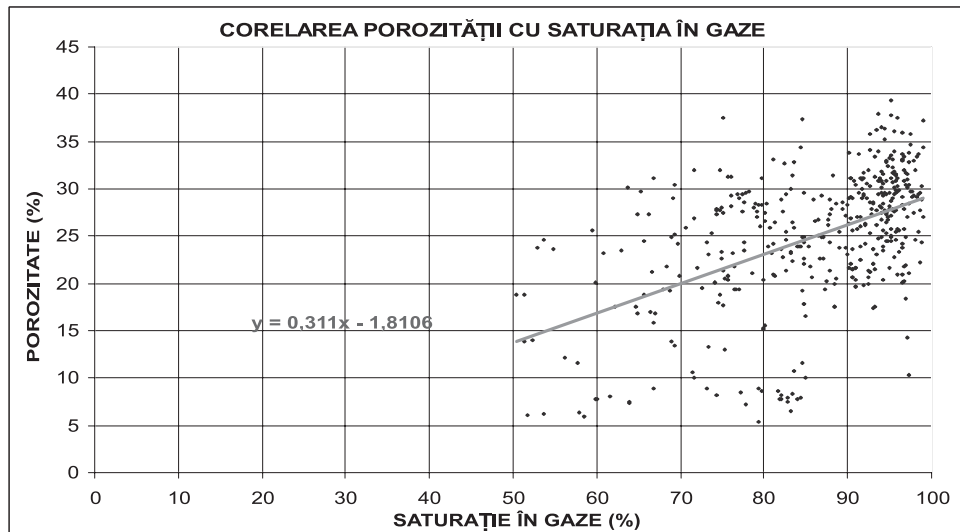


Fig. 4. Porosity – gas saturation correlation for Pliocene

## 10. ANALYSIS RESULTS AND THE CONFIDENCE OF THE ESTIMATIONS

The fact that the shape of the histograms for the main geological formations (Pliocene, Sarmatian, Buglovian, Badenian, Eocene, Cretacic and Jurassic) from porosity and gas saturation data distribution is not always normal for all the geological formations, or log-normal for permeability, respectively, although the data volume available for statistical analysis is rather high, shows that indeed the physical properties which characterize the reservoir rocks of the gas reservoirs from the Southern part of Transylvanian Depression are very heterogeneous (Figs 5–10).

It was noticed that the average values of the physical parameters obtained through statistical methods (median) are close to arithmetic average (which characterizes porosity and gas saturation) and geometrical average (which characterizes permeability), in Table 1.

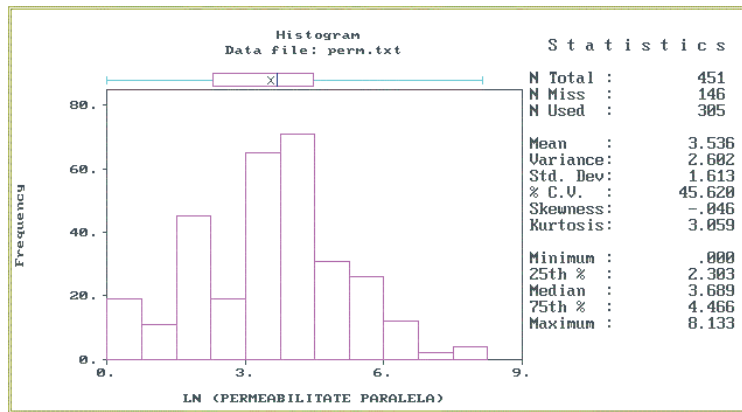


Fig. 5. Permeability parallel with stratum histogram at Pliocene

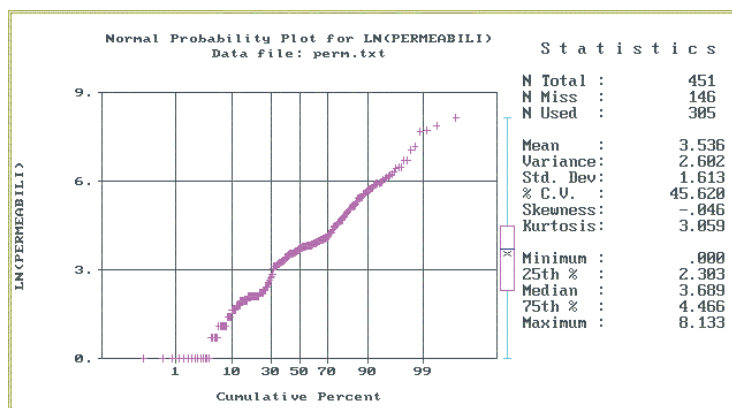


Fig. 6. Cumulative for permeability parallel with stratum at Pliocene

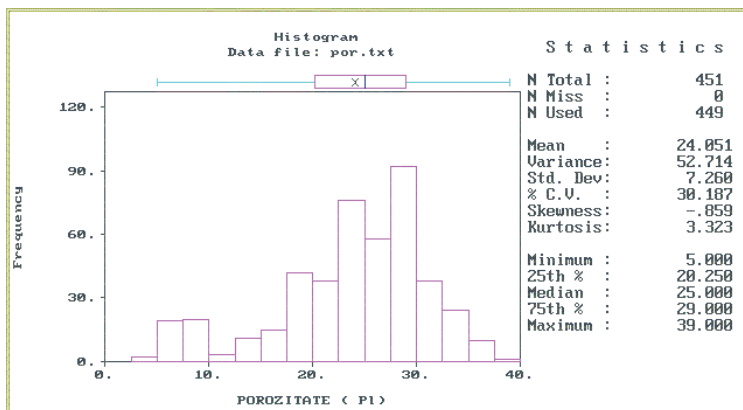


Fig. 7. Porosity histogram at Pliocene

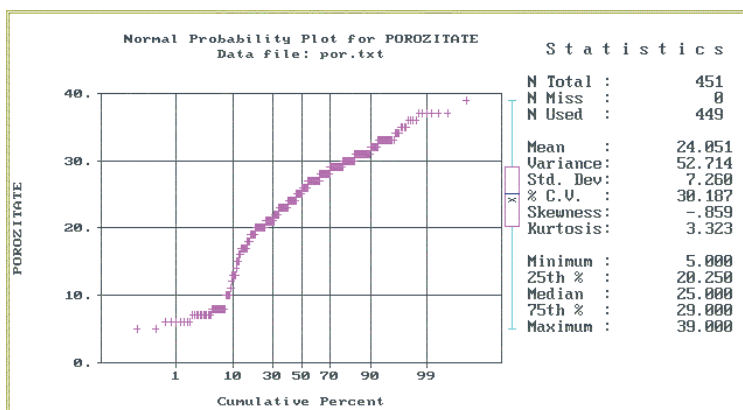


Fig. 8. Cumulative for porosity at Pliocene

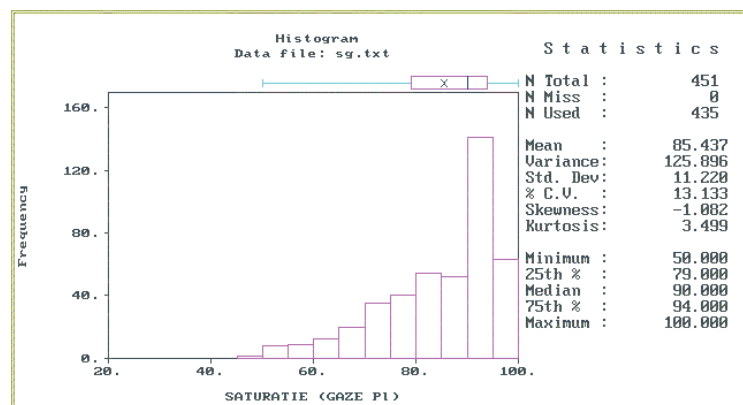
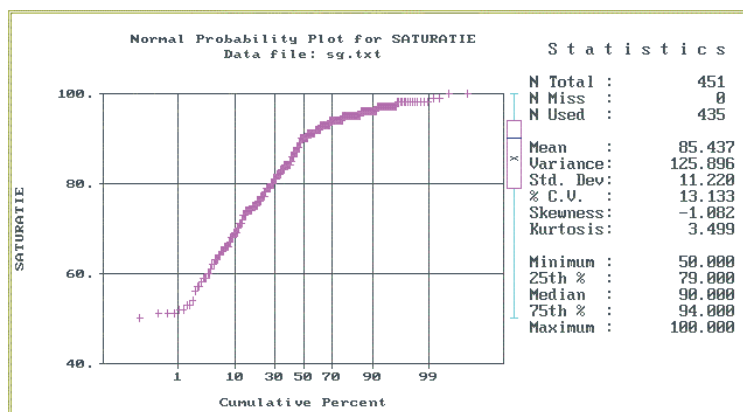


Fig. 9. Gas saturation histogram at Pliocene



**Fig. 10.** Cumulative for gas saturation at Pliocene

**Table 1**

The average values of the physical parameters: median, arithmetic mean, geometrical mean

Formation	Porosity [%]		Gas saturation [%]		Permeability [md]	
	Median	Arithmetic mean	Median	Arithmetic mean	Median	Geometric mean
Pliocene	25.9	24.6	90.4	85.9	35.02	20.24
Sarmatian	16.1	16.2	83.8	80.4	2.21	3.26
Buglovian	9.6	11.8	84.3	82.2	1.05	1.72
Badenian	9.3	11.5	82.9	81.01	0.84	1.18
Cretacic	7.6	8.2	84.11	82.25	0.28	0.35
Jurassic	6.4	7.2	75.03	74.55	0.09	0.08

From the correlations between the main parameters performed for total gas reservoirs on geological formations it was observed:

- a very good correlation between:
  - porosity and gas saturation for Pliocene and Eocene; the correlation coefficient is 0.5 for Pliocene and 0.66 for Eocene;
  - porosity and permeability parallel with stratum for Badenian, Eocene and Cretacic; the correlation coefficient is 0.47 for Badenian, 0.80 for Eocene and 0.79 for Cretacic;
  - gas saturation and permeability parallel with stratum for Jurassic; the correlation coefficient is 0.84;
- good correlations for porosity and gas saturation and for porosity and permeability, for all formations;
- rather good correlations for porosity and depth, for all formations;
- poor correlations for gas saturation and depth, for permeability and depth, for all formations.



Comparison between the resulted parameters from statistical analysis and the present parameters used in the volumetric estimation of the resources

From the statistical analysis of the cores resulted values of the physical parameters which can be used for the estimation of the natural gas resources.

It was made a comparison between the resulted parameters from statistical analysis and the present parameters used in the volumetric estimation of the resources for some gas reservoirs (see Tab. 2).

**Table 2**

Comparison between the resulted parameters from statistical analysis and the present parameters used in the volumetric estimation of the resources

Structure	Minimum-maximum values of the core parameters [%]		Parameters obtained from statistical analysis (arithmetic mean-median) [%]		Present parameters used in the estimation of the resources [%]	
	Porosity	Gas saturation	Porosity	Gas saturation	Porosity	Gas saturation
A	6–25	51–72	11–13	57–58	10–25	55–75
B	6–27	50–96	17–19	80–88	12–23	55–72
C	6–35	57–98	22	86–89	16–22	55–70
D	5–29	50–99	11	79–82	13–19	55–65
E	5–50	51–98	8–13	81–79	10–18	55–65
F	5–29	63–98	10–14	86–88	12–23	55–72
G	5–28	50–98	8–12	79–94	17–20	65–70
H	5–25	51–97	9–11	77–79	14–22	55–72

It was observed that in most cases the porosity was overestimated and the gas saturation was much underestimated, excepting structure A, where the gas saturation was overestimated.

## REFERENCES

- [1] Arps J.J.: *Estimation of Primary Oil Reserves*. J.P.T., August 1956, 182–191
- [2] Bennion D.W., Griffiths J.C.: *A Stochastic Model for Predicting Variations in Reservoir Rock Properties*. SPEJ, March 1966, 9–16
- [3] Bradley H.B.: *Petroleum Engineering Handbook*. SPE, Richardson, USA, 1987
- [4] Craft B.C., Hawkins M.F.Jr.: *Applied Petroleum Reservoir Engineering*. London, Constable Co. Ltd. 1959
- [5] Crețu I., Grigoraș I.D.: *Reserves Estimation Methodology Project*. Petroleum & Gas University of Ploiești, February 1996

- [6] Crețu I., Ionescu E.M., Stoicescu M.: *Hidraulica zăcămintelor de hidrocarburi*. Aplicații numerice în exploatarea primară. București, Editura Tehnică 1993
- [7] Crețu I.: *Hidraulica zăcămintelor de hidrocarburi*. Vol. 1, 2. București, Editura Tehnică 1987
- [8] Dake L.P.: *Fundamentals of Reservoir Engineering*. Developments in Petroleum Science, 8, Amsterdam – Oxford – New York, Elsevier Scientific Publishing Company 1978
- [9] Ding L.Y., Mehra R.K., Donnelly J.K.: *Stochastic Modeling in Reservoir Simulation*. SPE Reservoir Engineering, February 1992, 98–106
- [10] Gardner W.A.: *Introduction to Random Processes*. New York, Mc. Graw Hill Book Co. Inc. 1989
- [11] Grigoraș I.D.: *Studiul caracterului aleator al parametrilor mediului solid și evaluarea gradului de neuniformitate al zăcămintului de hidrocarburi*. Referat 1 – Doctorat, Ploiești, Universitatea Petrol-Gaze, Catedra Hidraulică, Termotehnică și Inginerie de zăcământ, 1995
- [12] Grigoraș I.D.: *Modele matematice de evaluare a performanțelor zăcămintului cu luarea în considerație a caracterului aleator al proprietăților mediului solid*. Referat 2 – Doctorat, Ploiești, Universitatea Petrol-Gaze, Catedra Hidraulică, Termotehnică și Inginerie de zăcământ, 1995
- [13] Grigoraș I.D.: *Contribuții la elaborarea de modele fizico-matematice generate din analiza datelor de exploatare a zăcămintelor de petrol*. Ministerul Educației Naționale, Universitatea Ploiești, Petrol-Gaze 1999 (Teză de Doctorat)
- [14] Grigoraș I.D.: *Contribuții la elaborarea de modele fizico-matematice generate din analiza datelor de exploatare a zăcămintelor de petrol*. Ploiești, Ministerul Educației Naționale, Universitatea Petrol-Gaze 1999 (Teză de Doctorat)
- [15] Grigoraș I.D., Aszalos T.: *Posibilități de prelucrare statistică a informațiilor existente la nivelul unui zăcământ de hidrocarburi*. Sesiunea de comunicări științifice: „Industria de Petrol și Gaze – Prezent și perspective”, Institutul de Petrol și Gaze, Ploiești 14–15 mai 1992, broșura secțiunii Inginerie de Zăcământ
- [16] Grigoraș I.D., Aszalos T., Alexandru W., Prodan D.: *Construcția hărților cu izolinii asistată de calculator prin utilizarea funcțiilor de tendințe și posibilități de generare a secțiunilor geologice*. Jubileu Științific: “Industria de Petrol și Gaze – Prezent și viitor”, Institutul de Petrol și Gaze, Ploiești 14–15 mai 1992, broșura secțiunii de Geologie–Geofizică
- [17] Grigoraș I.D., Crețu I.: *Asupra evaluării incertitudinii în unele calcule din ingineria de zăcământ*. lucrare prezentată la Simpozionul Național de Teoria Filtrării, Universitatea de Petrol și Gaze, Ploiești 23–24 iunie 1995
- [18] Grigoraș I. D., Marcaș G.: *O metodă de calcul a volumului brut pentru un zăcământ de hidrocarburi*. Revista Română de Petrol, serie nouă, vol. 1, No. 2, octombrie 1994
- [19] Grigoraș I.D., Nicolescu Ș., Ionescu M.: *Metode stochastice pentru evaluarea resurselor de hidrocarburi*. Buletinul Universității „Petrol-Gaze”, Volumul LII, Seria Geologie, Nr 4, 2000, Număr special cu lucrările Simpozionului Jubiliar 2000 „Cercetarea științifică – realizări și perspective în pragul secolului XXI”, ISSN 1221-9371, Ploiești

- [20] Grigoraș I.D., Grigoraș G.: *Studiu privind analiza statistică și realizarea unor corelări privind parametri fizici determinați pe baza carotelor mecanice din zăcămintele de gaze naturale din partea de sud a Depresiunii Transilvaniei*. Addeco S.R.L., Ploiești, S.N.G.N. ROMGAZ S.A.-Sucursala Mediaș, februarie 2005
- [21] Haldorsen H.H., Damsleth E.: *Stochastic Modeling*. J.P.T., April 1990, 404
- [22] Ioachim Gr., Popa C.: *Exploatarea zăcămintelor de țiței*. București, Editura Tehnică 1979
- [23] Jensen J.L., Lake L.W., Corbett P.W.M., Goggin, D.J.: *Statistics for Petroleum Engineers and Geoscientists*. Upper Saddle River, NJ 07458, Prentice Hall PTR 1997
- [24] Lake L.W., Carroll H.B., Jr., Wesson T.C.: *Reservoir Characterization II*. San Diego, California, Academic Press Inc. 1991
- [25] Law J.: *Statistical Approach to the Interstitial Heterogeneity of Sand Reservoirs*. Trans., AIME (1944), 155, 202–222
- [26] McCray A.W.: *Petroleum Evaluations and Economic Decisions*. Englewood Cliffs, New Jersey, Prentice Hall Inc. 1975
- [27] Megill R.E.: *An Introduction to Risk Analysis*. Tulsa, OK, Penn Well Books 1984
- [28] Rubinstein R.Y.: *Simulation and the Monte Carlo Method*. New York, NY, John Wiley and Sons 1981
- [29] Slider “Slip” H.C.: *Worldwide Practical Petroleum Reservoir Engineering Methods*. Tulsa, Oklahoma, Penn Well Publishing Company 1983
- [30] Soare A. et al.: *Ingineria zăcămintelor de hidrocarburi*. București, Editura Tehnică 1981
- [31] Șarapov I.P.: *Utilizarea statisticii matematice în geologie*. București, Editura Tehnică 1968
- [32] Vernescu A., Popa C.Gh.: *Utilizarea simulării statistice în ingineria de zăcământ*. Mine, Petrol, Gaze, vol. 26, nr 12, 1975, 578
- [33] Vernescu Al.: *Evaluarea resurselor și rezervelor de țiței, problemă tehnico-economică*. Revista Română de Petrol, serie nouă, vol. 2, No. 3, Iunie 1995
- [34] Vernescu A.: *Mecanica zăcămintelor petrolifere*. București, Editura Tehnică, 1966
- [35] Walstrom J.E., Mueller T.D., McFarlane R.C.: *Evaluating Uncertainty in Engineering Calculations*. J.P.T., December 1967, 1595–1603
- [36] Warren J.E., Price H.S.: *Flow in Heterogeneous Porous Media*. SPEJ, September 1961, 153–169
- [37] Zorilescu D.: *Metode matematice de analiză și decizie în geologie și minerit*. București, Editura Tehnică 1972
- [38] *Pachet de programe pentru industria petrolieră. Manual de utilizare*. Ploiești, AD-DECO S.R.L. 1992–1993