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## NUMERICAL MODELLING OF PRESSURE AND VELOCITY RATES OF FLOWING ENGINE OILS IN REAL PIPE

### NUMERYCZNE MODELOWANIE CIŚNIENIA I PRĘDKOŚCI PRZEPŁYWU OLEJU SIL- NIKOWEGO PRZEZ PRZEWÓD RUROWY W WARUNKACH RZECZYWISTYCH

*The article deals with the numerical modelling of physical state flowing liquid in a real environment of real technical component (pipe). Specifically it is about to set the pressured and velocity rates along the pipe geometry in a certain places for temperature dependent material (three engine oil with different viscosity class) at three monitored temperatures of flowing medium. The numerical models were created by means finite element method. Observation focused mainly on places behind technical component geometry curvature which are from the point of view of flowing features most interesting.*

**Keywords:** numerical modelling, flow, engine oil, temperature, viscosity, density, FEM.

*Artykuł dotyczy modelowania numerycznego stanu fizycznego cieczy płynącej w rzeczywistym środowisku rzeczywistego elementu technicznego (przewodu rurowego). W szczególności, celem pracy było określenie ciśnienia i prędkości przepływu materiału, którego właściwości zależą od temperatury, w określonych punktach przewodu rurowego dla trzech monitorowanych temperatur przepływającego czynnika. Do badań użyto trzech typów oleju silnikowego o różnej klasie lepkości. Modele numeryczne tworzone za pomocą metody elementów skończonych. Obserwacje prowadzono głównie w miejscach tuż za zakrzywieniami elementu technicznego, które są najbardziej interesujące z punktu widzenia właściwości przepływu.*

**Słowa kluczowe:** modelowanie numeryczne, przepływ, olej silnikowy, temperatura, lepkość, gęstość, MES.

#### 1. Introduction

The great amount of plants, engineers and researches now deal with how to save production costs in the production of certain products. The situation in engineering is same. Lowering material quantity for production can save considerable amount. But there is an issue how to save the material and keep the same quality goods or else production goods safety at the same time. The experimental costs can exceed savings themselves. In this case the numerical modelling can be very well proved [1] and [15].

If the input has a good quality, [13] confirm that result can be very precise in case of using suitably chosen modelled methods. These obtained models can help to engineers to propose such parts which are not uselessly excessive but at the same time they should be safe in accordance to requested standards [14]. Ideal part shapes can be simulated as well both from the statistical view and dynamical view – elasticity, firmness, hydrodynamics, aerodynamics, thermodynamics etc. [10].

According to publication [5] the numerical modelling of many physical phenomenon is closely connected to simulation of certain form of velocity by mathematical means. The liquid velocity is related to solutions of various problems which are given by physical simulation.

Mathematical model consists in equations definition which describes processes above. In view of the fact that there are plane two-dimensional processes, axially symmetrical or three-dimensional and timely dependent, there are described by partial differential system equations which must be solved by numerical methods. Their use is subjected to broaden knowledge from field of flowing, turbulence, numerical methods, and computer technology. Commercial programme systems can be used to solve flowing. User's task is to assemble correct calculating model which includes some mathematical,

psychical and technical principles. It is necessary to find for such a model all input data in valid standards, carry out solution at terminal, and correctly interprets results for next use and also to carry out effective inspection in all phases of all input and output data. User has to categorize all information on geometrical data (two-dimensional or three-dimensional data, topology), external power data and physical data (information about flowing medium and its physical features). User's necessary task is to have knowledge of hydro-mechanics, thermos-mechanics and other science by problem intricacy[2].

In this study is described the numerical modelling of physical state flowing engine oil in a real pipe by means finite element method. Specifically it is about to set the pressured and velocity rates along the pipe geometry. The theoretical idea is that the variation in viscosity and density of liquid causes significant changes in pressure drop and flow density [6] and [7].

#### 2. Material and Methods

Engine oil feeding tube for turbo-blower was real technical component in this contribution. This pipe is used in tractor engines. Its shape, dimensions and monitored spots beyond geometry curvature are displayed in the Fig. 1.

Quality input data were necessary to obtain for numerical modelling. According to temperature dependent flowing liquid, engine oils with viscosity class 5W-30, 10W-40 and 15W-40 were chosen. At this engine oil temperature dependence of density and dynamical viscosity dependence was measured. The measured values of dynamical viscosity and density are displayed in Table 1.

Temperature dependence of dynamical viscosity was measured by rotary viscometer Anton Paar DV-3P with temperature sensor Pt100. The standardized spindle R3 was used which is most suitable for measuring liquid with similar viscosity. Temperature range of

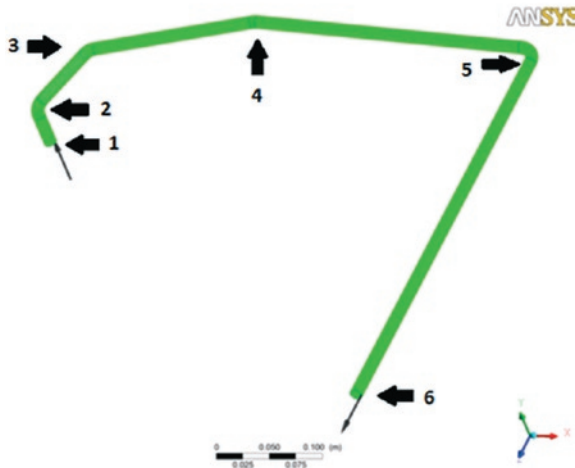


Fig.1. Real technical component (pipe)

measuring was chosen between -10°C and 100°C, similarly stated by [8] and [9].

Temperature dependence of specific weight (density) was measured by digital hydrometer Densito PX30 with API range for measuring of oil products. Temperature range was chosen between -10°C and 70°C.

The numerical modelling was done in programme FLUENT, because this program is optimal for finite element method and for Navier-Stokes differential equations solving.

Table 1. Values of dynamic viscosity and density of engine oils at various temperatures

Temperature (°C)	Density (kg.m <sup>-3</sup> )			Dynamic viscosity (mPa.s)		
	5W-30	10W-40	15W-40	5W-30	10W-40	15W-40
-10	859	867	881	1433	2415	5298
0	856	863	878	828	1108	2667
10	852	862	876	374	607	739
20	848	860	873	227	306	412
30	845	856	870	144	180	225
40	838	854	867	89	115	144
50	835	852	862	67	85	98
60	834	848	858	57	70	74
70	833	846	854	49	59	63
80				42	53	56
90				40	47	52
100				38	45	50

Continuous functions from measured data of dynamical viscosity and density were necessary to create for needs of numerical modelling [6]. Similar work process can be observed at [12].

The exponential function was most suitable function for using of results interpose by general form [11]:

$$\eta = a \exp(bt) \tag{1}$$

Where  $\eta$  is a dynamic viscosity;  $t$  is temperature;  $a, b$  are coefficients. Values of these coefficients are shown in Table 2.  $R^2$  is coefficient of determination.

Table 2. Values of coefficients for Eq. (1)

Viscosity class of engine oil	a (mPa.s)	b (1/°C)	R <sup>2</sup>
5W-30	790.6	-0.05976	0.9936
10W-40	1186	-0.06996	0.9955
15W-40	2379	-0.08122	0.9924

The linear function was chosen as the most suitable function using for results interpose of measured density values [7]:

$$\rho = ct + d \tag{2}$$

where  $\rho$  is density;  $t$  is temperature;  $c, d$  are coefficients. Values of these coefficients are shown in Table 3.  $R^2$  is coefficient of determination.

Table 3. Values of coefficients for Eq. (2)

Viscosity class of engine oil	c (1/°C)	d (mPa.s)	R <sup>2</sup>
5W-30	-0.3869	855.5	0.9841
10W-40	-0.2571	864.2	0.9866
15W-40	-0.3226	878.7	0.9848

There is a process in the Fig. 2 showing exponential functions interposed measured values of dynamical viscosity. In the Fig. 3 there is a displayed process of linear functions interposed measured density values.

### 3. Results and Discussion

Modelling of pressured profiles, mass flow and velocity of engine oil streaming with viscosity class 5W-30, 10W-40 and 15W-40 in certain places along geometry of technical component was made by Finite Element Method. There were used general continuity equation, see Eq. (3), and Navier-Stokes equations, see Eq. (4), [5]:

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0 \tag{3}$$

$$\begin{aligned} \frac{\partial u}{\partial t} + \frac{\partial(uu)}{\partial x} + \frac{\partial(uv)}{\partial y} + \frac{\partial(uw)}{\partial z} &= -\frac{1}{\rho} \frac{\partial p}{\partial x} + \nu \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right) + f_x \\ \frac{\partial v}{\partial t} + \frac{\partial(vu)}{\partial x} + \frac{\partial(vv)}{\partial y} + \frac{\partial(vw)}{\partial z} &= -\frac{1}{\rho} \frac{\partial p}{\partial y} + \nu \left( \frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} + \frac{\partial^2 v}{\partial z^2} \right) + f_y \\ \frac{\partial w}{\partial t} + \frac{\partial(wu)}{\partial x} + \frac{\partial(wv)}{\partial y} + \frac{\partial(ww)}{\partial z} &= -\frac{1}{\rho} \frac{\partial p}{\partial z} + \nu \left( \frac{\partial^2 w}{\partial x^2} + \frac{\partial^2 w}{\partial y^2} + \frac{\partial^2 w}{\partial z^2} \right) + f_z \end{aligned} \tag{4}$$

where  $u, v, w$  are velocity components;  $p$  is pressure;  $\rho$  is density;  $\nu$  is kinematic viscosity;  $f_{x,y,z}$  denotes external forces (gravity, centrifugal). Other exact equations are shown in publication [5].

Average pressure values, weight flowing and velocity of engine oil streaming at medium temperature 0°C, 20°C and 70°C are presented in Table 4, gradually for all six chosen cross-sections.

From calculated data the plummet of pressure can be observed during temperature increase of engine oil flowing as well as increasing of velocity flowing which is related to increase of liquid weight flowing. For illustration were chosen only figures of engine oil with viscosity class 15W-40.

In the Fig. 4 there are velocity streamlines in cross-sections 1-6 at liquid temperature of 0°C. In the Fig. 5 there are velocity vectors in cross-sections 1-6 at liquid temperature of 20°C. In the Fig. 6 there are pressures in cross-sections 1-6 at liquid temperature of 70°C.

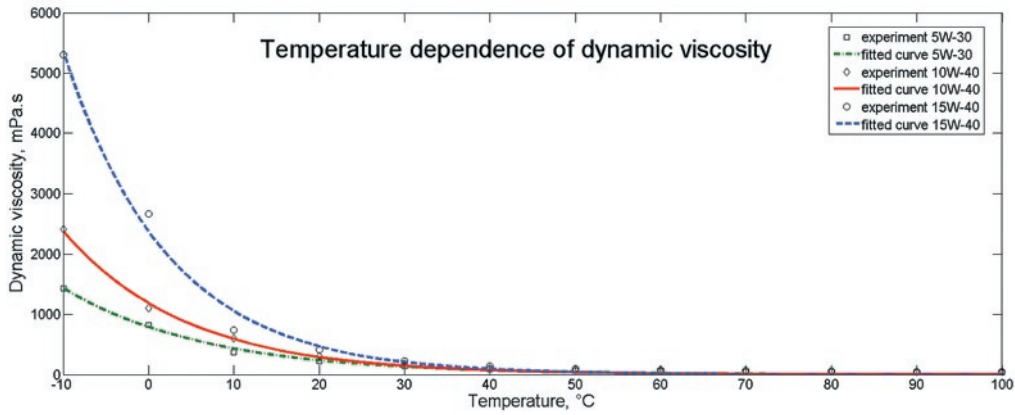


Fig. 2. Temperature dependences dynamic viscosity of engine oils and fitting by exponential function

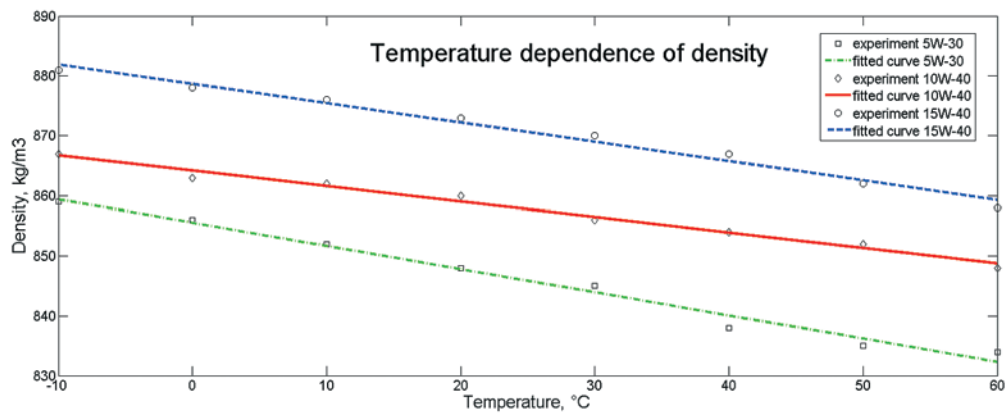


Fig. 3. Temperature dependences density of engine oils density and fitting by linear function

Table 4. Values of pressure, mass flow and velocity of engine streaming for specific temperatures

Temp. (°C)	Cross-section	Pressure (kPa)			Mass flow (g.s <sup>-1</sup> )			Velocity (m.s <sup>-1</sup> )		
		5W-30	10W-40	15W-40	5W-30	10W-40	15W-40	5W-30	10W-40	15W-40
0	1	500.0	499.8	499.8	17.62	14.61	11.30	15.81	13.12	10.02
	2	472.4	468.0	465.6	18.01	15.07	11.55	15.92	13.21	10.04
	3	431.2	419.5	418.7	17.65	14.69	11.34	15.86	13.17	10.04
	4	342.9	317.6	327.2	17.51	14.55	11.26	15.81	13.14	10.04
	5	194.1	176.6	184.8	17.49	14.58	11.22	15.82	13.14	10.04
	6	0.002	0.002	0.001	17.53	14.61	11.29	15.82	13.14	10.04
20	1	499.9	499.9	499.9	17.85	16.37	16.59	16.55	14.73	14.68
	2	421.8	471.4	470.7	17.97	16.78	16.98	16.60	14.86	14.81
	3	360.9	428.0	428.0	17.88	16.55	16.76	16.54	14.79	14.74
	4	279.9	336.7	337.8	17.84	16.41	16.62	16.52	14.74	14.69
	5	119.1	191.4	192.8	17.83	16.36	16.56	16.53	14.75	14.70
	6	0.001	0.005	0.005	17.85	16.40	16.61	16.52	14.74	14.69
70	1	499.9	499.9	499.9	19.12	18.92	18.18	17.04	16.62	16.02
	2	467.9	468.2	469.5	19.66	19.48	18.70	17.47	16.99	16.28
	3	432.6	433.2	434.4	18.81	18.78	18.34	17.16	16.74	16.12
	4	347.6	348.5	351.2	19.10	18.97	18.36	17.08	16.66	16.04
	5	202.7	203.1	204.0	18.62	18.57	18.09	17.30	16.85	16.16
	6	0.013	0.012	0.012	19.39	19.25	18.54	17.05	16.64	16.03

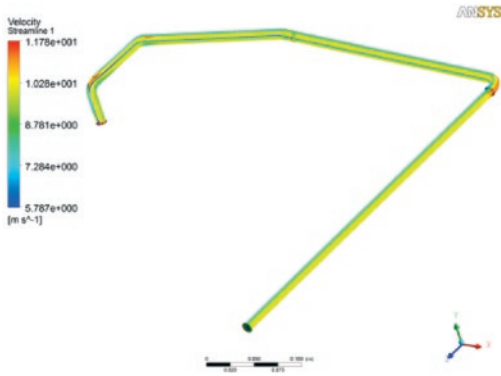


Fig. 4. Velocity streamline in chosen places at oil temperature of 0°C

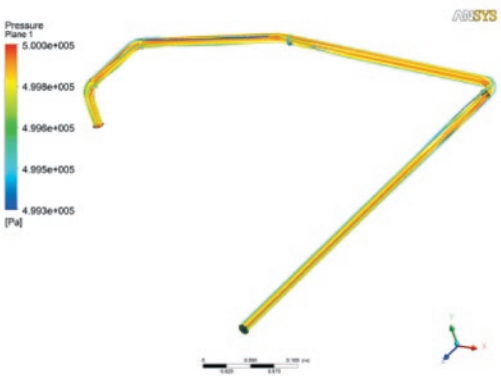


Fig. 5. Velocity vectors in chosen places at oil temperature of 20°C



Fig. 6. Pressures in chosen places at oil temperature of 70°C

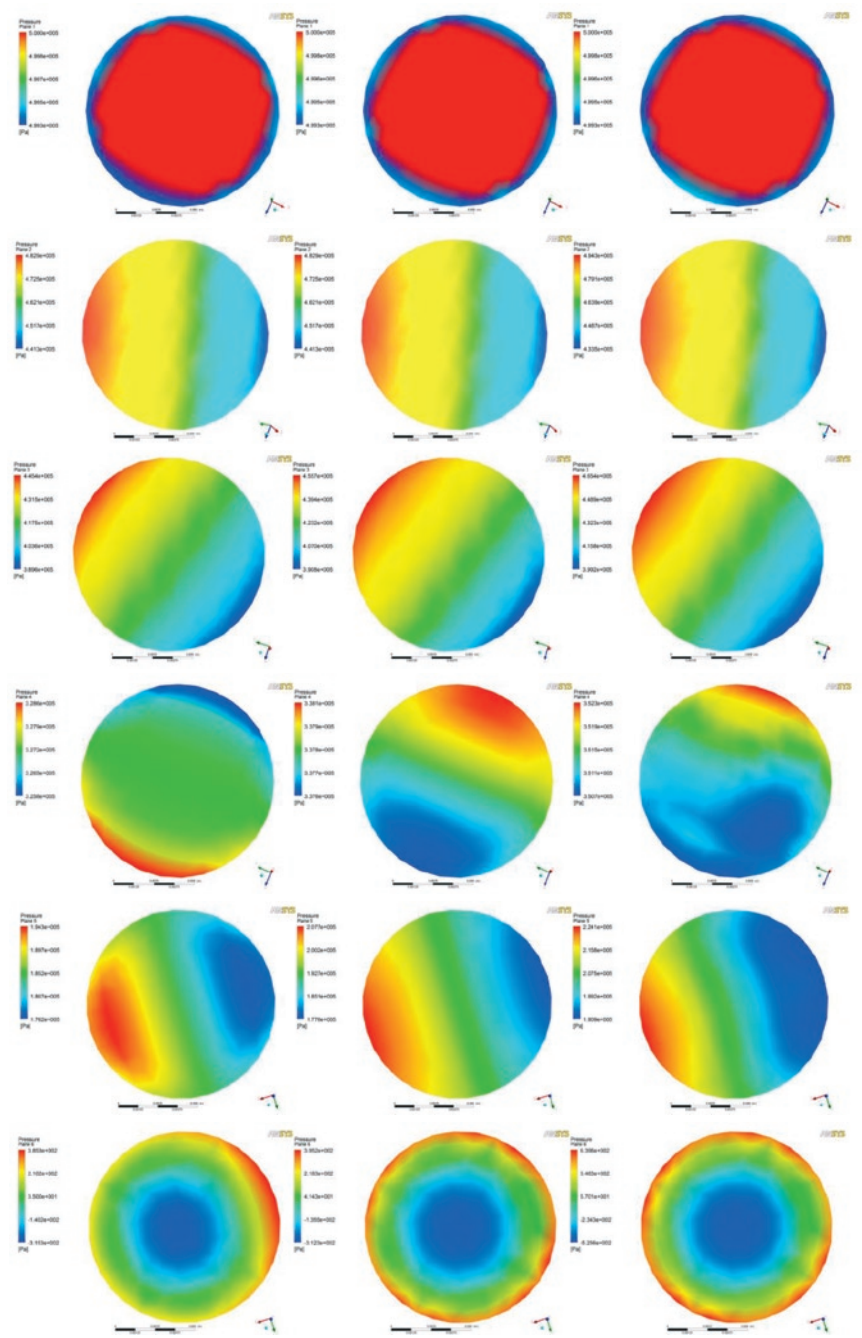


Fig. 7. Pressure decomposition in plane of sections 1–6 at oil temperature of 0°C, 20°C and 70°C

In the Fig. 7 there is a graphical representation of pressure decomposition in chosen cross-sections 1–6, at liquid temperature 0°C, 20°C and 70°C. During creation of numerical models of pressure decomposition in cross-sections was chosen the smoothest displaying system as in [3] and [4].

In several cross-sections are not any significant differences of pressure at the different temperatures. Only cross-section 4 shows some differences of pressure whole temperatures. It may be caused by high velocity of engine oil, which is lead to turbulent flow.

**4. Conclusion**

Numerical modelling of physical states of streaming liquid in real environment of technical component was made in this article. As a liquid was used engine oil and real technical component was engine oil feed pipe to turbo-blower. This feed pipe is used in tractor engines.

Firstly, the temperature dependence of dynamical viscosity and density of engine oils with viscosity class 5W-30, 10W-40 and 15W-40 was measured by using method of modern measuring devices. These data were interposed suitably chosen regression curved lines – exponential function (viscosity) and linear function (density) – to reach dependence connection which is necessary for numerical modelling.

Also, by using programme there were created numerical models of average values of weight flowing, velocity streaming and decomposition of pressure liquid in six chosen cross sections. These cross-sections were suitably chosen – input, output and geometry curving of feed pipe. Numerical modelling was made at temperatures of 0°C, 20°C, and 70 °C.

The results of average pressure values, weight flowing and velocity of engine oil streaming at three different temperatures show increasing velocity of flowing liquid with increase of temperature and



decrease of dynamical viscosity. That is why the weight flowing values of flowing liquid increased.

During numerical modelling creation of pressure decomposition in cross-sections was chosen smoothest displaying system, therefore all colour highlighted pressure values are very precise.

The theoretical idea is that the variation in viscosity and density of liquid causes significant changes in pressure drop and flow density was partially confirmed. With increasing temperature the viscosity and density of engine oil decreased, which was caused higher values of flow velocity and mass flow. This also applies vice versa. Temperature dependence, respectively viscous and density dependence on the pressure drop was not shown.

The results of these experiments can be used for design engineers to predict physical states of engine oil flowing (or similar viscous liquids) in pipe of similar diameter and geometry. The pressure and velocity results are able to predict, which material and what thickness must be used to produce real pipes.

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