

FAST FCM WITH SPATIAL NEIGHBORHOOD INFORMATION FOR BRAIN MR IMAGE SEGMENTATION

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Abstract

Among different segmentation approaches Fuzzy c-Means clustering (FCM) is a well-developed algorithm for medical image segmentation. In emergency medical applications quick convergence of FCM is necessary. On the other hand spatial information is seldom exploited in standard FCM; therefore nuisance factors can simply affect it and cause misclassification. This paper aims to introduce a Fast FCM (FFCM) technique by incorporation of spatial neighborhood information which is exploited by a linear function on fuzzy membership. Applying proposed spatial Fast FCM (sFFCM), elapsed time is decreased and neighborhood spatial information is exploited in FFCM. Moreover, iteration numbers by proposed FFCM/sFFCM techniques are decreased efficiently. The FCM/FFCM techniques are examined on both simulated and real MR images. Furthermore, to considerably decrease of convergence time and iterations number, cluster centroids are initialized by an algorithm. Accuracy of the new approach is same as standard FCM. The quantitative assessments of presented FCM/FFCM techniques are evaluated by conventional validity functions. Experimental results demonstrate that sFFCM techniques efficiently handle noise interference and significantly decrease elapsed time.

1 Introduction

Medical imaging is a technique and process used to create images of the human body or parts for clinical purposes. In medical imaging, accurate detection of tissue borders is very important [1,2]. Image segmentation is a technique to label pixels/voxels and categorizes the image into separate sections; each section with uniformity in gray levels. Medical image segmentation extracts tissue borders in medical images. Magnetic resonance imaging (MRI) is a medical imaging modality and an important tool in the evaluation of brain diseases. Segmentation of MR images has many applications in medicine such as [1-4]:

- Identification of tissue anatomy
- Pre-and-post surgical Evaluation
- Detection of abnormal tissues such as tumors and pathological lesions
- Investigation of nervous system diseases such as MS and Alzheimer
- Evaluation of arteriosclerosis disease
- Detection of left and right ventricles
- Breast cancer detection
- Diagnosis of seizures
- Diagnosis of immune system weakness

MR image segmentation methods are commonly based on statistical or structural properties of images [5]:

1-Methods based on statistical characteristics: the statistical features are extracted from different models and functions such as the probability distribution function of the image intensities. Statistical methods segment an image by estimation of intensity distribution and assign the class labels to their corresponding pixels. They can either be parametric or nonparametric. Both are extensively used in segmentation of brain MR images such as Markov random models (MRFs) and Bayesian network classifiers [6, 7].

2-Methods based on structural characteristics: in these approaches the spatial characteristics of the image like edges and regions are applied. Segmentation with structural characteristics includes several groups:

- Pixel based methods segment according to the image intensity features. Thresholding, k-means, or fuzzy c-means clustering are pixel based approaches [8, 9];
- Edge based methods rely on boundary identification by tracing closed areas in the image. However they fall into the trap of false and blurred edges; also their performances are unpredictable. Edge detectors such as active contours or common edge detections (like prewitt, sobel & canny) were plentifully used in image segmentation [5, 10];
- region-based methods detect similar regions based on predefined criteria. The criteria can be image intensity level, the similar tissues, image uniformity, or sharpness. Region growing is a common region based technique [11].

Commonly combination of above methods has been used for optimal segmentation of medical images. Among existing methods, FCM is a well-developed unsupervised clustering approach. Widespread applications in image segmentation caused FCM to be considered as a favorite method. Applying fuzzy membership, each pixel can be a member of all tissues with different membership degrees. FCM because of its fuzziness, has high capability to reserve more information about the orig-

inal image compared to the other segmentation approaches [12, 13].

Conventional FCM doesn't have enough convergence speed in medical applications specifically in emergency circumstances. This paper presents a fast FCM algorithm based on neighborhood spatial information. Proposed FFCM technique utilizes novel rule to update cluster centers in each iteration step. The new rule significantly preserves quality of standard FCM and is faster than it. Furthermore, using dist-max algorithm [14] cluster centers are initialized before clustering process. Therefore, algorithm convergence speed increases more. Moreover proposed sFFCM algorithm by incorporation of spatial information [15] in FFCM avoids from tissue misclassification by noise interference.

The rest of this paper is as follows: In section 2-1, the conventional FCM algorithm is reviewed. Section 2-2 initializes cluster centers. Section 2-3 presents FFCM algorithm and Section 2-4 proposes sFCM/sFFCM by incorporation of spatial information in FCM/FFCM. To assess FCM techniques, validation functions are expressed in section 3. Then in Section 4, results and discussion are presented; and section 5 involves the conclusions of this paper.

2 Methodology

2.1 FCM algorithm

The c-means families are well developed group of batch clustering type because they are "least square" models. Each cluster consists of one or more common characteristics depending on the dimension of input data. FCM developed in 1970s, assigns fuzzy memberships to each element of dataset instead of hard membership [16]. Therefore in FCM each data point belongs to multiple clusters with different membership values. Let $X = \{x_1, x_2, \dots, x_n\}$ denote an input vector with n pixels which should be partitioned into ($2 \leq c \leq n$) and x_j is feature value. FCM is an iterative optimization procedure which minimizes the following cost function [15]:

$$J_m(U, V) = \sum_{i=1}^c \sum_{j=1}^n u_{ij}^m \|x_j - v_i\|^2. \quad (1)$$

And

$$\begin{aligned} 0 \leq u_{ij} \leq 1 \text{ for } 1 \leq i \leq c, 1 \leq j \leq n, \\ 0 \leq \sum_{k=1}^c u_{ik} < n \text{ for } 1 \leq i \leq c, \\ \sum_{i=1}^c u_{ij} = 1, \text{ for } 1 \leq j \leq n. \end{aligned}$$

Where n is number of data points, m is the fuzzy fitness grade (m equals to 1 in hard clustering and more than 1 in fuzzy clustering), u_{ij} is the membership of pixel x_j in the i -th cluster, v_i is the centroid of i -th cluster, and $\|\cdot\|$ is Euclidean norm.

Since the cost function must be minimized, pixels which are close to their clusters center should have high membership values. Vice versa low membership values are assigned to pixels with data far from cluster center. In the other hand, the maximum distance between the cluster centroids leads to the optimum clustering. Membership function and cluster centers are updated by the following equations:

$$u_{ij} = \frac{1}{\sum_{k=1}^c \left(\frac{\|x_j - v_i\|}{\|x_j - v_k\|} \right)^{2/(m-1)}}. \quad (2)$$

$$v_i = \frac{\sum_{j=1}^n u_{ij}^m x_j}{\sum_{j=1}^n u_{ij}^m}. \quad (3)$$

Starting with an initial value for each cluster center, the FCM converges to a solution for v_i representing the local minima or a saddle point of the cost function [15]. Convergence rate can be determined by comparing the differences between the membership function or cluster centers in two successive iterations. Convergence time depends on computing time of membership functions and cluster centers in the iterations.

2.2 Cluster center initialization

In order to avoid the random initialization, the dist-max algorithm for the center initialization has been offered [14]. In FCM/FFCM algorithm random initialization consumes more time to algorithm be converged. Cluster center initialization algorithm for FCM/FFCM is as follows [14]:

Step1: Sorting m_i 's in ascending order where $m_k = \frac{1}{p} \sum_{s=1}^p x_{is}$ and $i=1,2,\dots,n$ for input vector $X = \{x_1, x_2, \dots, x_n\}$ which is p -dimensional data.

Step2: Relabeling and reorganizing the dataset matrix as $X' = \{x'_1, x'_2, \dots, x'_n\}$; Partition the data in to c groups and Find $nc_k = \lfloor n/c \rfloor$, where nc_k is number of data points in k -th cluster; such that the $(j-1)$ th group contains the $(j-1)$ th nc_k data of X' , and the c -th group contains the remaining all elements; where $j=1,2,\dots,c$. The number of cluster c is specified according to the nature of the dataset ($1 < c < n$).

Step3: Making a distance tables that show the distance between the elements within each group. (ie) if group $k = \{x_1^k, x_2^k, \dots, x_n^k\}$, the distance table in this group is (table 1):

Step4: Selecting the maximum distance from each distance table of groups. If d_{ij}^k is maximum distance of k -th group, find the mean value M_k of the elements x_i and x_j then assign centroid of k -th cluster as M_k , and $k=1,2,\dots,c$.

2.3 Proposed Fast FCM

As mentioned, high speed algorithms such as clustering ones are required in medical applications. Moreover, standard FCM doesn't have enough convergence speed especially in emergency conditions. FCM assigns c membership grades to every pixel. By iteratively updating the cluster centers and membership grades for each data point, FCM moves the cluster centers to the right location within a data set. However, updating membership matrix with $c \times n$ member is a time consuming procedure. In FCM, centroids are updated by fuzzy memberships which need much time because cluster centers are selected as a fuzzy quantity. Whereas cluster centers are similar feature vectors and can be calculated by a hard membership. Hence to reduce time and amount of computations in FCM, a hard membership can be assigned to pixels for updating cluster centers in each iteration step. however, segmentation will be a fuzzy procedure. Applying hard membership, the new algorithm to update centroids is proposed as following:

Step1: For p -dimensional input data, rearrange u_{ij} to $d_1 \times d_2$ matrix; where d_1 and d_2 are input dimensions.

Step2: Set new fuzzy membership as u_{ij}^* and label matrix as $L = \{L^1, L^2, \dots, L^c\}$; where L^k is label matrix of k -th cluster in current iteration.

Step3: Set all data points which are correspond to

	x_1^k	x_2^k	...	x_n^k
x_1^k	d_{11}^k	d_{12}^k		d_{1n}^k
x_2^k	d_{21}^k	d_{22}^k		d_{2n}^k
.
x_n^k	d_{n1}^k	d_{n2}^k	...	d_{nn}^k

Table 1. distance matrix within each data group

L^k label matrix as I^k .

Step4: Define $I^k = I_1^k, I_2^k, \dots, I_{nc_k}^k$ for k -th cluster, where nc_k is number of data points in k -th cluster

Step5: Update centroid of k -th cluster by the following equation:

$$v_k^* = \frac{\sum_{j=1}^{nc_k} I_j^k}{nc_k} \quad (4)$$

2.4 Spatial FCM/FFCM

Neighborhood pixels have many similarities and analogous feature properties therefore they are members of the unique clusters with great probability. Nevertheless it has not been exploited in the FCM/FFCM algorithm successfully. To utilize neighborhood spatial information in image processing, the spatial function can impressively be represented as [15]:

$$h_{ij} = \sum_{k \in NB(x_j)} u_{ik} \quad (5)$$

The spatial function h_{ij} just like the membership function u_{ij} , indicates the possibility that pixel x_j belongs to i -th cluster. The lattice window $NB(x_j)$ represents a 5×5 square lattice with a linear spatial function and x_j is a pixel in center of lattice window.

If the majority of pixels in the local lattice belongs to the similar cluster, the spatial function h_{ij} will denote that the pixel with great possibility is a member of the cluster [17]. Therefore incorporation of the spatial function into membership function is as follows [15]:

$$u_{ij}^* = \frac{u_{ij}^p \times h_{ij}^q}{\sum_{k=1}^c u_{kj}^p \times h_{kj}^q} \quad (6)$$

Where u_{ij}^* is new membership function, and

the parameters p and q signify the comparative influence of both membership and spatial functions u_{ij} and h_{ij} respectively. The improved spatial FCM/FFCM with parameter p and q is represented as sFCM $_{p,q}$ /sFFCM $_{p,q}$.

Hence new spatial fuzzy clustering is summarized in two stage process at each iteration step. In the 1st stage FCM /FFCM technique is simulated and in each iteration step membership function is updated. In the second stage spatial information of neighboring pixels are exploited in FCM /FFCM with spatial function. Therefore the new membership function in spatial domain for all pixels is updated by mapping all pixels membership functions to the spatial domain.

The proposed sFCM/sFFCM can be summarized as follows:

Step1: Select the number of clusters (c), fuzziness value ($m=2$); initialize $V^{(0)}/V^{*(0)}$.

Step2: Update the membership matrix U/U^* by Eq.(6).

Step3: Update cluster center matrix V/V^* for sFCM/sFFCM by Eq.(3)/ Eq.(4).

Step4: Repeat steps 3–4 until $\left\|v_i^{(t+1)} - v_i^{(t)}\right\| < \epsilon$, where ϵ is a small positive constant.

3 Validation functions for fuzzy clustering

Mostly two types of validity functions are used to evaluate the performance of clustering: fuzzy partition and geometric structure. Partition coefficient V_{pc} and partition entropy V_{pe} are fuzzy partition functions and defined as following [18, 19]:

$$V_{pc} = \frac{\sum_{j=1}^n \sum_{i=1}^c u_{ij}^2}{n}. \quad (7)$$

$$V_{pe} = (-1) \times \frac{\sum_{j=1}^n \sum_{i=1}^c u_{ij} \log(u_{ij})}{n}. \quad (8)$$

In these equations less fuzziness shows better performance of the algorithm. As a result, the best clustering is achieved when V_{pc} has maximum value (close to one) or V_{pe} has minimum value (close to zero). these functions can only measure the fuzzy partition and don't have a direct access to the intensity vector. This problem can be solved using validity functions based on the geometric structure. To optimum clustering in validity functions based on the geometric structure, samples within one partition should be compacted and samples between different clusters should be separated [19]. To quantify the ratio of total variation within clusters, V_{fs} and V_{xb} are defined as following [18]:

$$V_{fs} = \sum_{j=1}^n \sum_{i=1}^c u_{ij}^m (\|x_j - v_i\|^2 - \|v_i - \bar{v}\|^2). \quad (9)$$

$$V_{xb} = \frac{\sum_{j=1}^n \sum_{i=1}^c u_{ij}^m (\|x_j - v_i\|^2)}{n * (\min_{i,k} \{ \|x_k - v_i\|^2 \})}. \quad (10)$$

Where, $v_i \neq v_k$ and minimized V_{fs} or V_{xb} lead to optimal clustering.

4 Results and discussion

To verify the effectiveness of the presented FCM techniques, they were evaluated on both synthetic and real MR images. in the simulations, images were corrupted by additive Gaussian white noise then segmented by FCM techniques. In all experiments cluster centers are initialized by dist-max algorithm.

similar results in the presence of noise show similar performances of FCM and FFCM techniques. Since T1 weighted images of the human brain use the longitudinal component of magnetic resonance imaging, they have high contrast and resolution; therefore they are proper for medical image segmentation.

Figure 1(a) is a simulated T1weighted MR image [15] which in Figure 1(b) is corrupted by additive Gaussian white noise ($\sigma = 0.002$); gray levels are 50, 100, 150, and 200. Each gray level represents a living tissue on MR image and should be specified as a separate cluster. result of clustering by FCM, FFCM, sFCM_{1,1}, sFFCM_{1,1}, sFCM_{0,2}, and sFFCM_{0,2} techniques have been represented respectively in Figure 1 (c)-(h).

Figure 2(a) shows the simulated T1 weighted MR image of human brain corrupted by additive Gaussian white noise ($\sigma = 0.001$) in (b). segmentation results, including white matter (WM), gray matter (GM), and the cerebrospinal fluid (CSF) using standard FCM techniques have been represented in Figure 2 (c)-(h).

Real MR images also used to assess performance of proposed FFCM and sFFCM techniques. Experiments show that real MR images can be segmented efficiently by sFFCM method. In Figure 3 (a) real MR image acquisitioned from 3T scanner is portrayed; this image is corrupted by additive Gaussian white noise ($\sigma = 0.001$) in Figure 3 (b). segmentation results using FCM techniques have been represented in Figure 3 (c)-(h).

To do quantitative comparison between performances of all presented FCM techniques, results of different validation functions are tabulated in continue. Table 2 and 3 represents quantitative comparison of FCM, sFCM_{p,q}, FFCM, and sFFCM_{p,q} approaches by the conventional fuzzy validity functions. In most cases, the validity functions based on the fuzzy partition show high similarity for the standard and fast FCM techniques. Moreover, differences between two approaches are insignificant. Most close to one in V_{pc} , most close to zero in V_{pe} and V_{xb} , and greatest negative value in V_{fs} demonstrate better clustering results.

In Figure 4 simulation time and iteration numbers using FCM techniques are shown. elapsed time and number of iterations are significantly decreased by the proposed FFCM and sFFCM approaches in diverse images. Moreover, in all FCM/sFFCM techniques, cluster centers were initialized by dist-max algorithm.

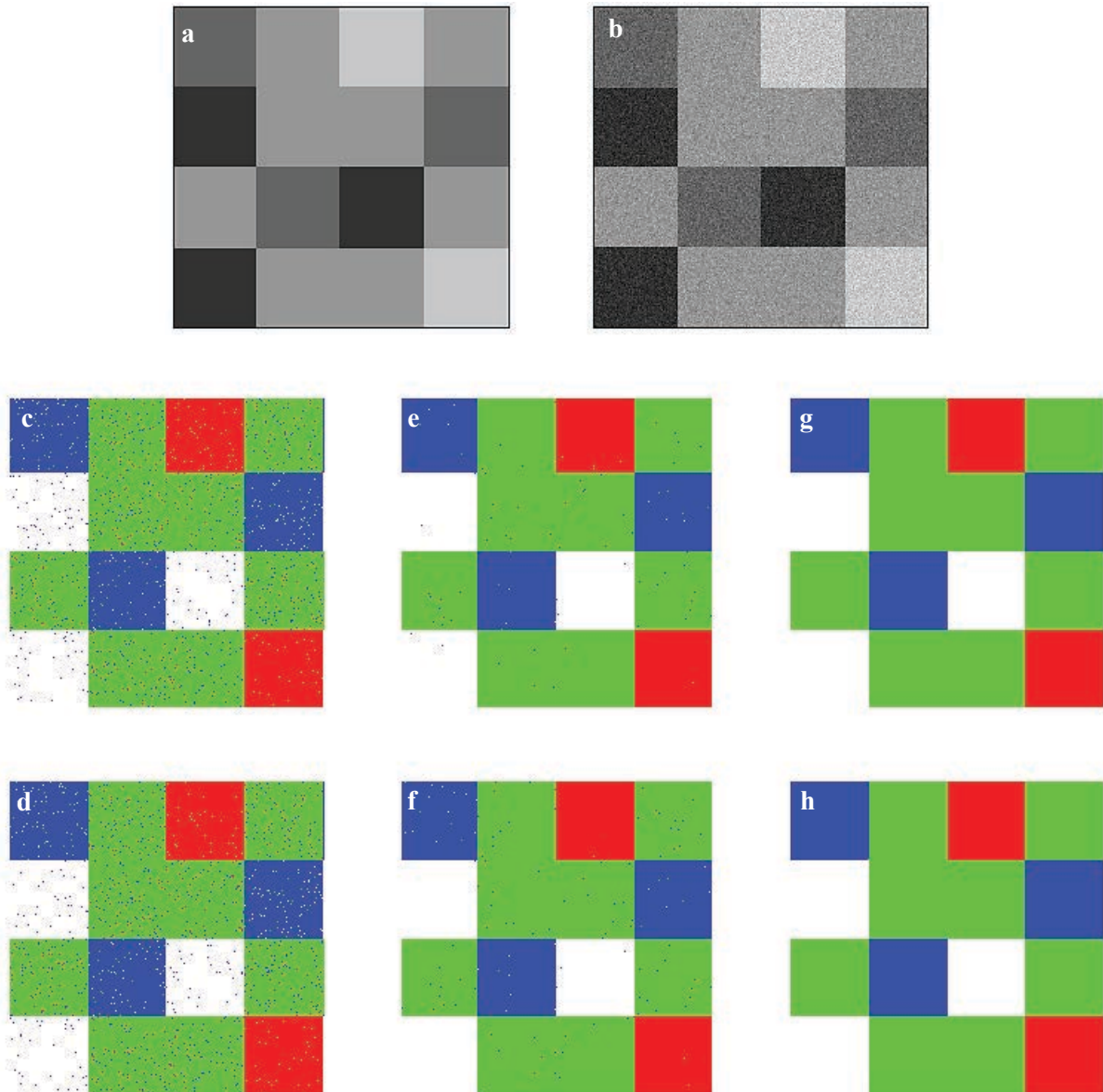


Figure 1. Segmentation results on synthetic MR image; (a) Synthetic MR image (b) corrupted by Gaussian white noise ($\sigma = 0.002$); segmented images by (c) FCM (d) FFCM, (e) $sFCM_{1,1}$, (f) $sFFCM_{1,1}$, (g) $sFCM_{0,2}$, and (h) $sFFCM_{0,2}$.

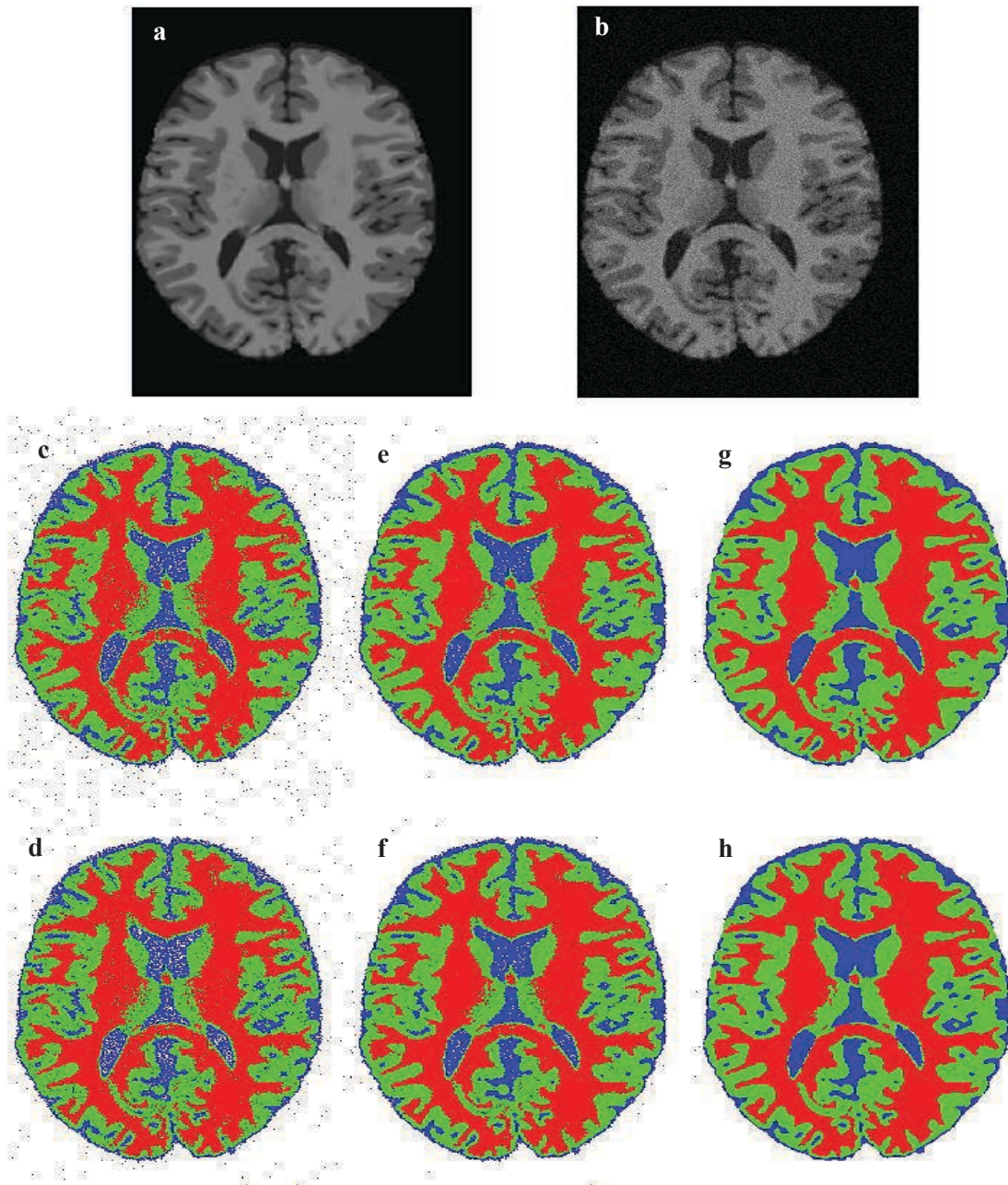


Figure 2. Segmentation results on simulated MR image; (a) simulated T1 weighted image, (b) corrupted by additive Gaussian white noise ($\sigma = 0.001$); segmented images by (c) FCM, (d) FFCM, (e) sFCM_{1,1}, (f) sFFCM_{1,1}, (g) sFCM_{0,2}, and (h) sFFCM_{0,2}.

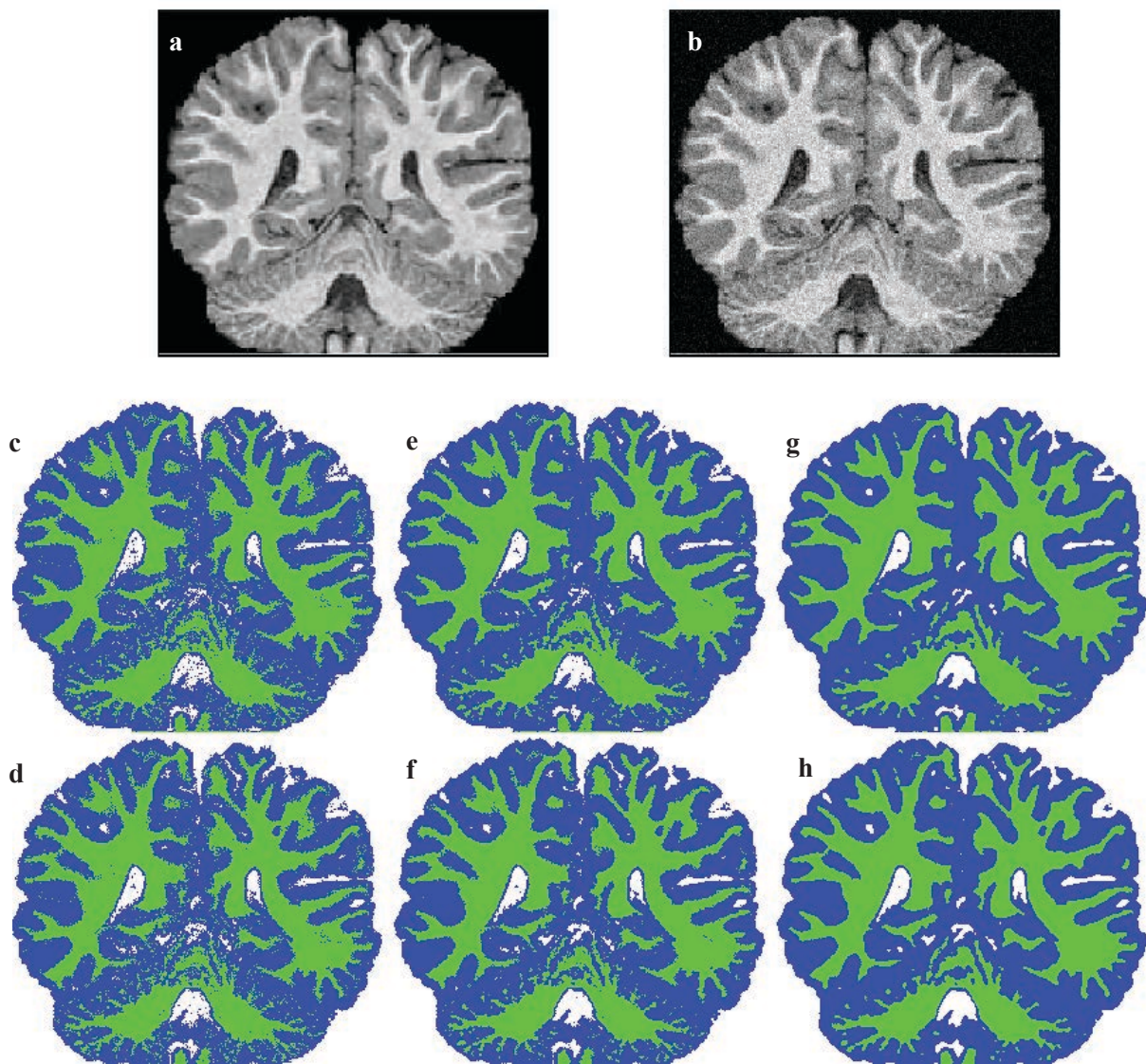


Figure 3. Segmentation results on real MR image ; (a) real T1 weighted image, (b) corrupted by additive Gaussian white noise ($\sigma = 0.001$); segmented images by (c) FCM (d) FFCM, (e) sFCM_{1,1} , (f) sFFCM_{1,1} , (g) sFCM_{0,2} , and (h) sFFCM_{0,2}.

Table 2. Fuzzy partition (V_{pc} and V_{pe}) for various images using FCM/FFCM techniques

technique	simulated 4 level MRI ($\sigma=0.002$)		simulated MRI ($\sigma=0.001$)		Real MRI (3T)	
	V_{pc}	V_{pe}	V_{pc}	V_{pe}	V_{pc}	V_{pe}
FCM	0.847	0.135	0.847	0.131	0.852	0.117
FFCM	0.847	0.135	0.848	0.132	0.842	0.129
sFCM _{1,1}	0.975	0.024	0.943	0.044	0.931	0.051
sFFCM _{1,1}	0.973	0.025	0.944	0.043	0.932	0.051
sFCM _{0,2}	0.969	0.031	0.916	0.064	0.907	0.068
sFFCM _{0,2}	0.967	0.032	0.916	0.064	0.905	0.069

Table 3. Geometric structure (V_{xb} and V_{fs}) for various images using FCM/FFCM techniques.

technique	simulated 4 level MRI ($\sigma=0.002$)		simulated MRI ($\sigma=0.001$)		Real MRI (3T)	
	V_{xb}	$V_{fs} \times (-10^6)$	V_{xb}	$V_{fs} \times (-10^6)$	V_{xb}	$V_{fs} \times (-10^6)$
FCM	0.038	145	0.047	163	0.065	306
FFCM	0.038	143	0.051	154	0.078	248
sFCM _{1,1}	0.046	160	0.053	176	0.069	320
sFFCM _{1,1}	0.048	157	0.058	167	0.087	266
sFCM _{0,2}	0.054	156	0.067	170	0.083	306
sFFCM _{0,2}	0.056	154	0.070	163	0.099	254

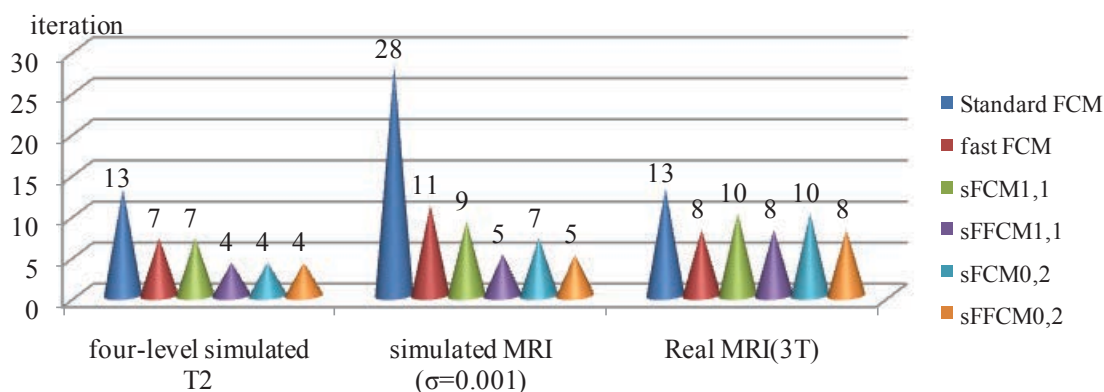
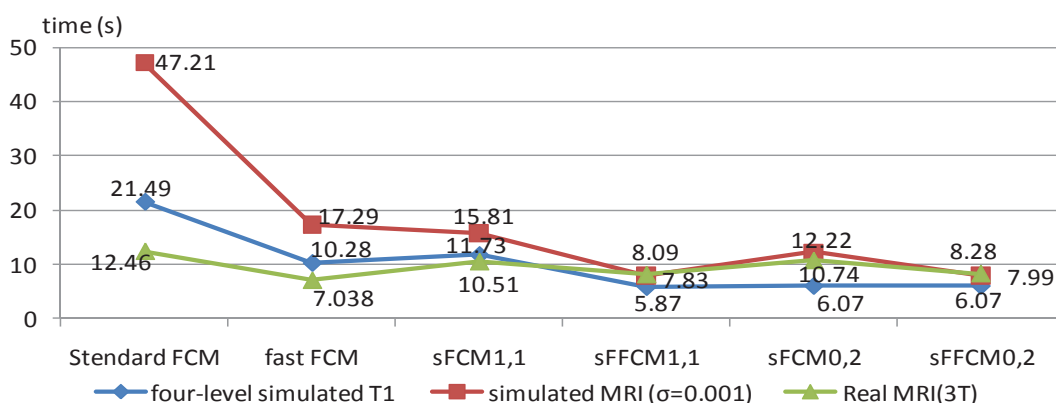


Figure 4. Figure 4: Simulation time (up) and iteration numbers (down) for FCM, FFCM, sFCM_{1,1}, sFFCM_{1,1}, sFCM_{0,2} and sFFCM_{0,2} on various images.

5 Conclusion

In medical imaging especially in emergency situations, using high speed agents such as clustering ones are very important. standard FCM may not have required convergence rate especially in emergency conditions. Hence this paper proposed a Fast FCM technique. by new approach, time and iteration numbers relatively decreased to half of traditional FCM. Synthetic and real MR images were used in the experiments. Proposed FFCM technique decreased the computational amount and time in comparison with standard FCM. Moreover a linear spatial function was used to incorporate spatial neighborhood information in FCM/FFCM algorithm. The sFFCM algorithm decreased noise interference and handled nuisance factors effectively. Proposed sFFCM technique segmented brain MR images with the same quality of the sFCM approach whereas reduced its elapsed time. Furthermore, to more increase convergence rate and more diminish iteration numbers, cluster centers were initialized by an algorithm. Quantitative assessments of FCM/FFCM techniques were evaluated by common fuzzy validation functions. Simulation results verify efficient performance of proposed techniques.

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