**Jan Radosław KAMIŃSKI** Department of Agricultural and Forest Machinery, Warsaw University of Life Sciences, Poland **Maciej KUBOŃ** Institute of Agricultural Engineering and Informatics, University of Agriculture in Kraków, Poland **Aleksandr Nikolaevich ORDA** Belorussian State Agrarian Technical University, Minsk, Belarus **Cheslav Iosifovich ZHDANOVICH** Belorussian National Technical University, Republic of Belarus e-mail: [jan\\_kaminski@sggw.pl,](mailto:jan_kaminski@sggw.pl) [maciej.kubon@ur.krakow.pl](mailto:maciej.kubon@ur.krakow.pl)

## **TRACTION PROPERTIES OF SUSPENSION SYSTEMS OF FARM TRACTORS**

*Summary*

*Presently, great attention is paid to development of new types of suspension systems of farm tractors and mobile machines which have a decreased unit pressure on soil. Their traction properties must be taken into consideration when values of suspension systems parameters are determined. The coefficient of operation performance was assumed as a criterion defining this property. The article presents an analysis of component relations of the coefficient of operation performance with the suspension system parameters. Relations between resistance and soil deformation, used by many authors were applied for calculation of the rolling resistance. It was proved that the rolling resistance of the driving source decreases when the number of support wheels increases. In order to reduce deformation of soil under the towing power it is recommended to use a tyre tread, which ensures sufficient adhesion to soil, not as a result of shearing soil with a tread, but as a result of tread friction on soil.*

**Key words***: system, traction, tractor, resistance, rolling*

# **WŁAŚCIWOŚCI TRAKCYJNE UKŁADÓW JEZDNYCH CIĄGNIKÓW ROLNICZYCH**

#### *Streszczenie*

*Obecnie dużo uwagi poświęca się opracowaniu nowych typów układów jezdnych ciągników rolniczych oraz maszyn samojezdnych charakteryzujących się obniżonym naciskiem jednostkowym na glebę. Przy ustalaniu wartości parametrów układów jezdnych konieczne jest uwzględnienie ich właściwości trakcyjnych. Jako kryterium, charakteryzujące tę właściwość przyjęto współczynnik efektywności działania. W artykule zamieszczono analizę zależności składowych współczynnika efektywności działania od parametrów układu jezdnego. Przy obliczeniach siły oporu przetaczania wykorzystano stosowane przez wielu autorów zależności między oporem a deformacją gleby. Wykazano, że opory przetaczania źródła napędu zmniejszają się przy zwiększaniu liczby kół podporowych. W celu obniżenia deformacji gleby podczas działania siły uciągu zaleca się stosowanie bieżnika ogumienia, zapewniającego dostateczne sczepienie z glebą nie w efekcie ścinania gleby bieżnikiem, a w efekcie tarcia bieżnika o glebę.*

**Słowa kluczowe***: układ, trakcja, ciągnik, opór, przetaczanie*

#### **1. Introduction**

In multi-suspension systems traction properties manifest in various ways in relation to the structure of a suspension system [11, 14]. In tractors and machines which are connected, suspension systems with the structure of wheels which move one after another in the same track are the most popular [2, 4, 6, 12].

The coefficient of operation performance is a basic criterion which defines mobile machine modernity. The value of this coefficient is defined with the following relation:

$$
\eta = \eta_{mp} \cdot \eta_f \cdot \eta_{\delta},
$$

where:  $\eta_{mp}$  – coefficient which includes mechanical resistance of the driving gear;  $\eta_f$  - coefficient which includes rolling resistance;  $\eta_{\delta}$  – coefficient which includes driving wheels slips.

Elements of COP  $\eta_f$  and  $\eta_\delta$  include energy losses related to vertical and horizontal soil deformation which increases along with the decrease of those elements. Values  $\eta_f$  and  $\eta_\delta$ define the coefficient of operation performance of the suspension system as follows:

$$
\eta_{xc} = \eta_f \cdot \eta_{\delta} = \left(1 - \frac{P_f}{P_k}\right) (1 - \delta),
$$

where:  $P_f$  – rolling resistance of the wheel system, N;

 $P_k$  – horizontal towing power of the suspension system, N;

*δ* – driving wheels slip.

Thus, the COP is affected by the rolling resistance, horizontal towing power and wheel slips. We will discuss their changes in relation to the number of axles of the suspension system.

#### **2. Theoretical discussion**

*H*

We assume that during the movement of the suspension system on soil, rolling resistance depends mainly on the energy losses related to soil deformation *Aσ*. Work of the vertical soil deformation at the i-crossing of a wheel is:

$$
A_{\sigma i} = S \int_{H_{i-1}}^{H_i} \sigma_i(h) dh \tag{1}
$$

The total value of operation after the n-loading is:

$$
A_{\sigma n} = S \sum_{i=1}^{n} \int_{H_{i-1}}^{H_i} \sigma_i(h) dh.
$$
 (2)

The value of work at the i-crossing of a wheel per one rotation and after n-crossings will be:

$$
A_{oi} = 2\pi \cdot r \cdot B \int_{H_{i-1}}^{H_i} \sigma_i(h) dh , \qquad (3)
$$

$$
A_{\sigma n} = 2\pi \cdot r \cdot B \sum_{i=1}^{n} \int_{H_{i-1}}^{H_i} \sigma_i(h) dh.
$$
 (4)

On the other hand, the rolling resistance during one rotation of a wheel is:

$$
A = 2\pi \cdot r \cdot P_f. \tag{5}
$$

When comparing right sides of equations (3) and (5) we find the value of the rolling resistance during the i-crossing of a wheel:

$$
P_{f_i} = B \int_{H_{i-1}}^{H_i} \sigma_i(h) dh.
$$
 (6)

By analogy, from equations (4) and (5) we find the total rolling resistance of the n-axle suspension system:

$$
P_{\hat{j}_n} = B \sum_{i=1}^n \int_{H_{i-1}}^{H_i} \sigma_i(h) dh.
$$
 (7)

We find the total rolling resistance of the n-axle suspension system on strongly scarified soils from the assumption that the function  $\sigma(h)$  for these soils is a constant [1]. Therefore, the property of additivity of integration may be attributed to this equation (7),

$$
P_{f_n}=B\int\limits_0^H\sigma(h)dh.
$$

But, the relation of the resistance and bending of a is subject to the relation of the hyperbolic hyperbolic tangent described by V. V. Kacygin [7]:

$$
\sigma = p_0 th \frac{k}{p_0} h,
$$

where:  $p_0$  – soil bearing capacity,  $\Pi a$ ;  $k$  – coefficient of volumetric soil deformation,  $N \cdot m^{-3}$ .

Then, the relation between the rolling resistance and the number of axles of the multi-axle suspension system assumes the following form:

$$
P_{fn} = B \frac{p_0^2}{k} \ln \left( \frac{n^{bk/p_0}}{\sqrt{1 - q^2 / p_0^2}} \right),
$$
 (8)

where:  $b$  – coefficient determined by experiment;  $q$  – wheel pressure on soil.

For low-resistance soils, the rolling resistance relation to the number of axles takes the following form:

$$
P_{fn} = B \frac{p_0^2}{k} \ln \left( \frac{1}{\sqrt{1 - q^2 / p_0^2}} \right) (1 + k_u \lg n), \tag{9}
$$

where:  $k_u$  – coefficient of merging of subsequent deformations.

*J<sub>an</sub>* = 5.  $\sum_{n=1}^{\infty} f_n(x)h dx$ .<br>
The value is well as the constrained of a whole precise constrained of the subscription of the subscription of  $A_n = 2\pi \cdot r \cdot B \int_{\pi_n}^{\infty} f_n(x)h dx$ .<br>
The method as the constrained of Rese When analysing the relations (8) and (9) we see that the rolling resistance of each subsequent wheel, situated along the side of the tractor is lower than of the previous one. The horizontal towing power increases after the increase in the number of the suspension system axles [8]. As a result, the coefficient of operation performance of the suspension system and towing also increases. During the mutual impact of the driving wheel and soil, resisting force of soil against shearing, friction forces between the resistance surface of the tyre and soil and shearing force of soil chunks with side ridges of a tread, occur.

Transmission of the rotation moment of wheels is related to slip (towing) δ. At the same time soil deformation and shearing in the horizontal plane takes place. The highest relocation of soil  $S_{\text{max}}$  is:

$$
S_{\max} = \delta L,
$$

where:  $L$  - length of the resisting surface of a wheel.

The horizontal towing power developed with the i-axle of the multi-axle suspension system fights the soil shearing forces and friction forces of a tread on soil [8].

$$
P_{K\ i} = P_{SD\ i} + P_{TP\ i}.
$$
 (10)

A horizontal element of the towing power resulting from the shearing resistance of soil is:

$$
P_{SD} = (1 - k_H) \int_{0}^{L_i} V B \tau (x) dx,
$$
 (11)

where:  $k_H$  - coefficient of filling the shape of the tyre tread;

 $L_i$  - the length of the contact of the i-wheel with soil, m;

 $V$  - coefficient, depending on the soil condition and air pressure in a tyre;

 $\tau(x)$  - the function relation between the shearing stress and soil deformation.

V.V. Kacygin et al. [8] suggested the following relation between the shearing stresses and soil deformation:

$$
\tau = f_{ck}\sigma \left[1 + \frac{f_{np}}{ch(S/k_{\partial})}\right]th\left(\frac{S}{k_{\partial}}\right),\tag{12}
$$

where:  $f_{ck}$  - kinematic friction coefficient;

 $f_{np}$  - checked (replaceable) friction coefficient,  $=\frac{4f_n-3f_{ck}}{2a_n}$ 

$$
f_{np} = \frac{-J_n - J_{Ck}}{2f_{ck}},
$$

 $f_n$  - static friction coefficient;

 $k_{\partial}$  - deformation coefficient, m;

$$
k_{\partial} = S_0 \bigg/ \text{Arch}\bigg( \bigg(1 + \sqrt{1 + 8 f_{np}^2}\bigg) \bigg/ \bigg(2 f_{np}\bigg) \bigg),
$$

 $S_0$  – deformation size, corresponding to the maximum shearing stress m,

From the relation (11) and (12) we find:  
\n
$$
P_{SD\ i} = (1 - k_H) \int_0^{L_1} v \, B \, f_{\alpha i} \, \sigma_i \left[ 1 + \frac{f_{npi}}{ch(\delta x / k_\partial)} \right] th \left( \frac{\delta x}{k_\partial} \right) dx, \tag{13}
$$

where:  $dx$  - the length of the elementary surface.

The contact stress is placed longitudinally on the contact surface of a wheel irregularly. At the approximation of the distribution of stresses with a parabola, the following parabola between the maximum and average stresses was obtained:

$$
\sigma_{\max i} = \frac{3}{2} \sigma_{cp i} = \frac{3}{2} \frac{R_i}{V B L_i},
$$
\n(14)

where:  $R_i$  – normal reaction of soil, influence on a wheel, N.

Adding the relation (13) we obtain with the formula (14) the element of the horizontal towing power as a shearing effect of soil:

$$
P_{SDi} = \left(1 - k_H\right) \frac{f_{ck} k_{\delta} R_i}{\delta L_i} \left\{\ln ch \left(\frac{\delta L_i}{k_{\delta}}\right) - f_{np} \left[\frac{1}{ch(\delta L_i/k)} - 1\right]\right\}, (15)
$$

The element of the horizontal towing power resulting from the friction of a tyre tread on soil is [8]:

$$
P_{mpi} = k_H \sigma_{cpi} V B_k L_i \mu_{ck}, \qquad (16)
$$

where:  $\mu_{cK}$  – coefficient of a tyre tread friction on soil.

Coefficient of the slip friction depends on the slip speed and normal pressure on the place of a contact [13]:

$$
\mu_{\text{cx}} = \mu_n + \left[ \left( \mu_{\text{ycn}} - U \ \sigma \right) - \mu_n \right] \left[ 1 - 1/\theta^n \right],\tag{17}
$$

where:  $\mu_n$  – coefficient of friction of the tyre tread on soil including slipping;

 $\mu_{\text{yca}}$  – replacement coefficient of the tyre tread friction on soil at  $\theta \rightarrow \infty$  and  $\sigma \rightarrow 0$ ;

*U* - angular coefficient;

 $\theta$  - coefficient of slip,  $\theta = 1/(1-\delta)$ ;

*n* - parameter which depends on the type and condition of soil.

Relation (16) after including formulas (14) and (17) assumes the following form:

$$
P_{mp i} = k_H R_i \Biggl\{ \mu_n + \Biggl[ \Biggl( \mu_{yca} - U \frac{R_i}{V B L_i} \Biggr) - \mu_n \Biggr] \Biggl[ 1 - (1 - \delta)^n \Biggr] \Biggr\},
$$
\n(18)

Substituting the relations (15) and (18) to the formula (10) we obtain the horizontal (tangent) towing power of the iwheel,

$$
P_{ki} = (1 - k_H) \frac{f_{ck} k_o R_i}{\delta L_i} \left\{ \ln ch \left( \frac{\delta L_i}{k_o} \right) - f_{np} \left[ \frac{1}{ch(\delta L_i / k_o)} - 1 \right] \right\} +
$$
  
+  $k_H R_i \left\{ \mu_n + \left[ \left( \mu_{yca} - U \frac{R_i}{\nu B L_i} \right) - \mu_n \right] \left[ 1 - (1 - \delta)^n \right] \right\},$  (19)

The relation (19) enables determination of the impact of the soil resistance force during shearing and friction of a tyre tread on soil on the horizontal (tangent) towing power. The following relation of forces is of a considerable importance for the wheel systems when each following wheel moves on the track of the previous one.

### **3. Research results**

The impact of the tread shape was not included in the theoretical discussion. If tyres have extended treads, then the tracks after the first wheel are corrugated. After that the second wheel drives in the track of the first one, a specific work of crushing blocks of soil and then soil shearing under

the angle vertically and horizontally is performed (formation of new blocks). In the experiments, it was found out that in a given case, the rolling resistance of the back wheel is higher than the previous one [9].

Let us consider the possibilities of developing a high towing force without formation of soil blocks. Wheel adhesion to soil is obtained during the wheel slip. The size of slip depends not only on the condition of the soil surface but also on the shape of the tyre tread. At the developed tread, the shearing surface of a wheel, at the specific slip, i.e. at shearing soil blocks, a relocation of a wheel takes place, mainly at the surface of the tread blocks. In this case, the element of the horizontal towing power resulting from the friction of a wheel on soil is less significant than the component of the force, resulting from the crushing resistance of soil in longitudinal direction. In the described case, a corrugated surface in the track of wheels occurs, which is an undesired phenomenon in case of a wheel suspension system when wheels move on the same track.

If a protector (tread) ensures high adhesion to soil, not as a result of shearing with a tread, but as a result of tread friction on soil, then elevations and holes in the driving wheel track may be prevented. The research shows that at the longitudinal shearing of a body on the soil surface, soil deformation, not only on the surface, but also on the sufficiently low depths of the soil layer, takes place. This indepth deformation of soil influences the increase of the level stress at shearing. The relation of the tangent stress to the gradient of the relocation of the soil layer takes the following form:

$$
\tau = \mu_{\varphi} \, \frac{ds}{dh} f(\sigma) \, ,
$$

where: *μ<sup>φ</sup>* – coefficient, which depends on the friction of soil particles one against another;

 $\frac{ds}{dh}$  – the gradient of the soil layer relocation in vertical direction;

 $f(\sigma)$  – the function which determines the relation of the internal friction of soil on the stresses condition.

Experimental research of traction properties of soil of the multi-axle suspension system was carried out on the mechanical model in the soil channel [10]. Tyres 5.00-10 of driving wheels with an undeveloped tread were used.

Figure 1 shows that at the increase in the number of axles the rolling resistance decreases and the coefficient of operation performance of the suspension system increases. During the research, loading of the suspension system was constant and was 5.2 kN and pressures on soil were changing with an inversely proportional relation to the number of axles.

During the tests, we reported low values of the coefficient of operation performance of the suspension system  $(\eta_{xc} = 0.51)$ . It may be explained with high losses related to deformation of the scarified moist soil and wheels with a small diameter and kinematic losses. After the increase of the wheels diameter to 1.5-1.8 m, the coefficient of operation performance of the suspension system increased to the value of 0.62 only as a result of limiting slips. Calculations were made pursuant to the probability criterion  $\partial l / k_{\partial}$ .



*Source: own work / Źródło: opracowanie własne*

Fig. 1. Relation of the rolling resistance and the coefficient of performance operation of the suspension system to the number of suspensions of the multi-wheel suspension system

*Rys. 1. Zależność siły oporów przetaczania i współczynnika efektywności działania układu jezdnego od liczby podpór wielokołowego układu jezdnego*

## **4. Conclusions**

1. Increase in the number of axles of the multi-axle suspension system results in reduction in the rolling resistance of each subsequent wheel moving on the track of the previous one.

2. A chassis of multi-axle suspension systems should be equipped with tyres with a non-extended tread

#### **5. References**

- [1] Boikov V., Zhdanovich Ch., Orda A.: Agroecological concept of running systems of mobile agricultural machinery. Belt and Tire Traction in Agricultural Vehicles. SP-1291, SAE 1997, 109-113.
- [2] Brennensthul M.: Ocena właściwości trakcyjnych układu koło-podłoże w aspekcie zdolności uciągowych ciągnika jako uniwersalnego źródła energii pociągowej. Uniwersytet Przyrodniczy we Wrocławiu. Rozprawa doktorska, 2012.
- [3] Evdokimov P.D.: Ustojchivost' gidrotekhnicheskikh sooruzhenij i prochnosti ikh osnovanij. Moskva – Leningrad. Energiya, 1966, ss. 129.
- [4] Golka W., Kamiński J.R.: Potrzeba badań eksploatacyjnych ciągników i maszyn rolniczych. (The need for field tests of tractors and agricultural machines). Problemy Inżynierii Rolniczej. 2016, Zeszyt 3(93), 5-14.
- [5] Golka W. (red.): Kierunki rozwoju techniki w transporcie rolniczym, uprawie gleby, siewie, nawożeniu i ochronie roślin. (Trends of technique development in agricultural transport, soil tillage, seeding, fertilization and plant protection). Inżynieria w Rolnictwie, 2016, Monografie 23. ISSN 2083-9545.
- [6] Kamiński J.R., Kruk I.S., Szeptycki A.: Ciągnikowe agregaty maszynowe w nowoczesnym rolnictwie. (Tractor-machine sets in modern agriculture). Inżynieria w Rolnictwie, 2015, Monografie 18. ISSN 2083-954.
- [7] Katsygin V.V.: Оsnovy teorii vybora optimal'nykh parametrov mobil'nykh sel'skokhozyajstvennykh mashin i orudij. Voprosy sel'skokhozyajstvennoj mekhaniki. 1964, Тоm 13. Minsk, s. 5-147.
- [8] Katsygin V.V., Orda А. N., Kotlobaj А. Ya.: Vliyanie parametrov kolesnykh dvizhitelej na tyagovo-stsepnye svojstva traktorov. Mekhanizatsiya i elektrifikatsiya sel'skogo khozyajstva. 1982, 4, s. 28-30.
- [9] Ksenevich I. P., Skotnikov V. A.: O rabote traktornykh tandem koles. Traktory i sel'khozmashiny. 1978, 10, s. 8-9.
- [10] Orda A. N.: Vybor metoda i mekhanicheskoj modeli dlya issledovaniya koleeobrazovaniya kolesnymi khodovymi sistemami. Sbornik nauchnykh rabot aspirantov (CNIIMESKH). 1975, Minsk, s. 158-167.
- [11] Orda A. N., Šklarevič V. A., Kamiński J. R., Borusiewicz A.: Snizhenie uplotnyayushchego vozdejstviya khodovykh sistem pochvoobrabatyvayushchikh agregatov na pochvu. (Ograniczenie ugniatania gleby kołami jezdnymi agregatów uprawowych; Decrease in the condensing impact of running systems of soil-cultivating units on the soil). W: Obrabotka pochvy i proizvodstvo semyan l'na. (Uprawa gleby i produkcja nasion lnu. Soil cultivation and harvesting flax for seeds). Wyższa Szkoła Agrobiznesu w Łomży, 2016, Monografia. ISBN 978-83-87492-99-10.
- [12] Pieczarka K.: Analiza właściwości trakcyjnych ciągnika Fendt 820 w wybranych technologiach uprawy gleby. (Analysis of traction properties of Fendt 820 tractor in the selected technologies of soil cultivation). Inżynieria Rolnicza. 2011, 9(134), 193-199.
- [13] Ul'yanov N. А.: Teoriya samokhodnykh kolesnykh zemlerojno-transportnykh mashin. Moskva. Mashinostroenie, 1969, s. 520.
- [14] Zhdanovich Ch., Mamonov M., Kuboń M., Kamiński J.R.: Effect of steering gear parameters of crawler tractor cornering ability. (Wpływ parametrów mechanizmu nawracania na zwrotność ciągnika gąsienicowego). Agricultural Engineering, 2016, Vol. 20, 2, 159-169.