

## A method of determining influencing parameters and predicting random, critical events in complex technical objects

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### Abstract

A method of predicting the influence random events on the critical functionality of an object is discussed. Research is performed regarding the possibility of extending a prediction model to a prediction system by functionally uniting this model with additional models or recognizing the type of influence of a random event on a complex technical object. The proposed solution is important because executing a prediction system instead of a prediction model allows one to detect critical situations that, when influencing technical objects, can result in the catastrophic loss of functionality of the corresponding objects.

### Introduction

Critical random events  $Vp_i^K$ , that occur, alongside non-critical random events, that influence complex technical objects (CTO) and can result in catastrophic events or system failures ( $\mathcal{K}a_i$ ). ( $\mathcal{K}a_i$ ). Predicting the occurrence of various random events  $Vp_i$  instead of only  $Vp_i^K$  could fail to ensure the necessary accuracy in all cases. This inaccuracy results from calculation uncertainties that are intrinsic to the data used, the choice of the prediction model, and other considered and unconsidered random event inputs.

Assume that critical random events (CRE) that can lead to catastrophic situations occur quite rarely. To distinguish from the concept of rare events defined along with introducing the Poisson distribution function, critical random events will be called super-rare random events.

Occurrence of rare and super-rare events is typical for slow or super-slow processes. Examples of such processes are economic processes, processes that represent changes in social environments, processes of ecologic changes caused by natural factors and others. The concepts of rare and super-rare

events will be related to the time parameter and the measurement scale for this parameter. In order to predict events that can occur during these processes, non-linear prediction models are used, examples of which can be logistic models, equipotential models and so on (Anderson, 1982).

The occurrence of critical random events relating to technological processes ( $TP_i$ ) will be considered a super-rare event because they result in catastrophic situations in these  $TP_i$ . It would be incorrect not to consider events that cause catastrophic situations during the super-rare events, because in this case CTO with the corresponding  $TP_i$  could not function according to the specified requirements. We will assume the equivalence of concepts regarding a critical super-rare event  $Vp_i^K$  and a catastrophic situation  $\mathcal{K}a_i$  that occurs in  $CTO_i$ . A prediction in most cases is implemented in time, so time as a variable of the function used in the prediction model  $M(PG_i)$ .

For the purposes of this article the following terms are defined:

*Definition 1.* A time interval  $\Delta t_i$  between the moment of occurrence of a predicted event  $t_i$  and the

moment of finishing the prediction process  $\tau_i$  will be called a prediction interval:  $\Delta t_i = t_i - \tau_i$ .

Let us consider the possibility of using non-linear models for predicting events of  $Vp_i^K$  type.

Occurrence of  $Vp_i^K$  is influenced on by a series of factors that are identified by single symbol  $\mathcal{X}_i$ . A set of these factors sums up to a danger  $Nb_i$  that causes the occurrence of  $Vp_i^K$ . Because, in many cases, it is difficult to build a model  $Nb_i$  that could describe correlations between single factors  $\{\mathcal{X}_1, \dots, \mathcal{X}_n\}$  and, if it is known that these factors influence the occurrence of  $Vp_i^K$ , then, with some approximation, we can assume that the corresponding factors are independent from each other. Each single factor  $\mathcal{X}_i$  will be considered a time function  $\mathcal{X}_i(t)$ . Each factor that leads to the occurrence of a random event, causes the occurrence of  $Vp_i^K$  to a degree defined by a proportionality coefficient  $\beta_i$ . Any object of  $CTO_i$  has its basic degree of a safety level  $\mu_0$ .

Given conditions correspond to requirements relating to the use of non-linear prediction models that use exponential dependences. Due to random events of  $Vp_i^K$  type that lead to  $\mathcal{K}a_i(CTO)$  catastrophic situations that are super-rare, using an exponential dependence of a dependent variable from an argument, which in this case is time  $t$ , allows to approximate the time scale of an extra large interval. This makes it possible to speak about the occurrence of a CRE of type  $Vp_i^K$ . An example of this type of model, widely used in various branches of science, are the Cox prediction models (Korolyov, 1998).

Interpretation of the corresponding random events  $Vp_i$  lies in considering each random event  $Vp_i$  that influences  $CTO_i$  a corresponding attack  $At_i$  on  $CTO_i$  (Korostil, 2016). This interpretation of  $Vp_i$  random events is reasonable because random events  $Vp_i$  influence on  $CTO_i$  by activating some attack process  $Pr_i(At_i)$ , implemented in  $CTO_i$ , and is a process of influence of an attack  $At_i$ . Because the attack event  $At_i$  is activates in the  $CTO_i$ ,  $Pr_i(At_i)$  the attack process can be described on the basis of using components and corresponding parameters of the  $CTO_i$  object. This description can be considered an attack model, written as follows:

$$M(At_i) = [M(Pr_i(At_i)) \& M_i^\varphi(CTO_i)] \quad (1)$$

where  $M_i^\varphi(CTO_i)$  is a model of a single  $CTO_i$  fragment that takes part in the attack process  $Pr_i(At_i)$ . This allows for the follow transformation to occur when the random event occurs:

$$Vp_i \rightarrow [At_i(CTO_i) \rightarrow M(At_i)] \quad (2)$$

## Features of tasks of predicting critical events

According to classification of  $Vp_i$ , just among  $Vp_i^N$  it is possible for  $Vp_i^K$  and, respectively,  $At_i^K$  attack to occur, which leads to occurrence of system failure defined as  $\mathcal{K}a_i(CTO_i)$ . Corresponding to the relation (2) we can assume that  $Vp_i^N$  and  $Vp_i^K$  are equivalent to attacks  $At_i^N$  and  $At_i^K$ . Because attacks can be described by a large number of parameters comparing to the number of parameters usable for describing random events, formulations that regard random events will be correct regarding attacks and vice versa. Thus it is relatively easy to perform analysis of attacks instead of random events. The number of parameters that can be used to describe attacks is larger than the number of parameters that describe the corresponding random events because any attack implemented in  $CTO_i$  uses a threat ( $Zg_i$ ), placed in  $CTO_i$  and during its development an attack can extend the range of  $CTO_i$  parameters that  $At_i$  can use.

An occurrence of a single  $Vp_i^K$  is only possible when a single  $Vp_i^N$  appears with intensity not less than a given value and the corresponding events are different from each other. This condition can also be related to attacks  $At_i^N$ . If it turns out in practice that the same event  $Vp_i^K$  can use different threats, thus generating attacks different from each other, let us assume that this  $Vp_i^K$  has hidden parameters that cause the possibility to use different  $Zg_i \in CTO_i$ . For the purposes of this article the following terms are defined:

*Definition 2.* A critical number  $q_i(At_i^N)$  of various attacks  $At_i^N$  is defined as the number of attacks of type  $At_i^K$  that occurs, resulting in  $\mathcal{K}a_i(CTO_i)$ .

*Definition 3.* A critical number  $q_i(At_i^N)$  of various attacks  $At_i^N$  is a random number, and its possible values are given by a certain number interval that is defined as  $Q_i = \{q_{i1}(At_i^N), \dots, q_{im}(At_i^N)\}$ .

Despite the fact there is no sufficient information regarding the danger  $Nb_i$  that generates random events  $Vp_i$ , the number of random unexpected events  $Vp_i^N$  is limited. This is demonstrated in the following proof.

*Statement 1.* In case of unlimited number of  $Vp_i$  that  $Nb_i$  can generate, or  $Nb_i \rightarrow Vp_i \rightarrow N(Vp_i) \rightarrow \infty$ , the number of events  $Vp_i^K$ , or attacks  $At_i^K$  is limited, which means the following relation is true:

$$\left[ \sum_{i=1}^m Sg[At_i^K(CTO_i)] = m \right] \& [m \ll N]$$

where:

$$\left\{ \left\{ [At_i^K(CTO_i)] \neq 0 \right\} \rightarrow \left\{ Sg[At_i^K(CTO_i)] = 1 \right\} \right. \\ \left. \& \left\{ \left\{ [At_i^K(CTO_i)] = 0 \right\} \rightarrow \left\{ Sg[At_i^K(CTO_i)] = 0 \right\} \right\} \right\}$$

Let us assume this statement is not true. Then the number of  $At_i^K$  can increase up to infinity, or  $m(At_i^K) \rightarrow \infty$ . Each attack  $At_i^K$  is described by a model  $M(At_i^K)$ , that is a synthesis  $M(Pr_i(At_i)) \& M_i^p(CTO_i)$ , where  $M_i^p(CTO_i)$  is  $Pr_i^p[Pr_i(CTO_i)]$ . Since the number of fragments  $\varphi_i(CTO_i)$  of  $CTO_i$  structure is limited, for an arbitrary object of  $CTO_i$  type has finite structure, then the number  $Pr_i^p[Pr_i(CTO_i)]$  is limited as well. This leads to the fact that the number of  $At_i^K(CTO_i)$  is limited too, because  $M(At_i^K) = \{M(At_i^K) \& M_i^p(CTO_i)\}$ , and  $M_i^p(CTO_i) = Pr_i^p[Pr_i(CTO_i)]$ . This means that in the case where  $Nb_i \rightarrow Vp_i \rightarrow N(Vp_i) \rightarrow \infty$ , and the number  $Sg[At_i^K(CTO_i)] = m$  and  $m \ll N(Vp_i)$ ,  $N(Vp_i) - m = H$ , where  $H$  is a number of random events  $Vp_i$ , that either cannot influence  $CTO_i$  or are related to  $Vp_j$  that can be withstood by a safety system  $SB(CTO_i)$ . Correctness of the relation  $Nb_i \rightarrow Vp_i \rightarrow N(Vp_i) \rightarrow \infty$  is based on the fact that  $Nb_i$  can extend its possibilities of generating various  $Vp_i$  by extending or modifying its functional possibilities regardless of single  $CTO_i$ .

A model, oriented towards solving the task of predicting the occurrence of a certain event  $Vp_i$  that activates an attack  $At_i$ , is related to a certain threat  $Zg_i(CTO_i)$  of the corresponding  $CTO_i$  object. A threat  $Zg_i(CTO_i)$  is an important object parameter and, in general, is independent from  $Nb_i$  and attacks  $At_i$ , and can be used for activating attacks. This leads to the conclusion that the number of attacks that can be activated in  $CTO_i$  by events  $Vp_i$  depends on the number of threats existing in  $CTO_i$ . Due to the number of attacks of type  $At_i^K$  and, respectively, events of  $\mathcal{K}_i(CTO_i)$  depend on the number of attacks of  $At_i^N$  type, their number depends on the number of attacks of type  $At_i$ . The number of threats of a corresponding type that would correlate to all possible attacks  $At_i^N$  is absent in the corresponding  $CTO_i$  so the number of attacks of type  $At_i^K$  that can lead to  $\mathcal{K}_i(CTO_i)$  is lower. In this case, in the task of building such a prediction model that belongs to a certain model class and can consider the decrease of the general number of events among which one would have to be predicted during a given time interval  $\Delta t_i$ .

According to the theory of time series, concepts of trends of probable events are introduced and are described by certain functions with time variable  $t$  as an argument (Andersen, 1976). Using these concepts leads to certain prediction models, which can lead to additional modifications of general prediction models, including those involving exponentials.

An important factor that affect prediction adequacy is input data, on the basis of which calculations performed by the corresponding model are

implemented. The input data allows for the detection of the possibility of occurrence of a certain event in a time interval  $\Delta t_i$ . A source of data is a certain dangerous event that generated the corresponding data. Interpretation of the corresponding random event  $Vp_i$  has to be closely related to the interpretation of the corresponding data. So, functional possibilities  $M(PG_i)$  have to approximate processes that generate data  $\mathcal{X}_i(t)$ . This means that, in a perfect case, functional possibilities  $M(PG_i)$  have to be close to the model of  $\mathcal{X}_i(t)$  data source, which in this case is  $Nb_i$ . If we assume that  $Nb_i$  generates some factors characterized by data  $\mathcal{X}_i(t)$  in order to affect  $CTO_i$ , the model  $M(PG_i)$  can be interpreted as a certain approximation to an unknown functioning model  $Nb_i$ , or  $M(Nb_i)$ . This means that a model  $M(PG_i)$  can be built so that on the basis of immediate data  $\mathcal{X}_{i+k}(t)$ , a random event  $Vp_i$  and a given interval  $\Delta t_i$  would make it possible to modify  $M(PG_i)$  so that it is closer to the functioning model of  $Nb_i$ , or to  $M[Pr_i(Nb_i)]$ . Where  $Pr_i(Nb_i)$  are functioning processes of  $Nb_i$ . In general, the following relation can be written:

$$\Phi[\mathcal{X}_i(\delta t_i) \& Vp_i(\mathcal{X}_i(\delta t_i + \Delta t_i))] \rightarrow [M(PG_i) \rightarrow M[F(Nb_i)]]$$

In this case, the task of building a model  $M(PG_i)$  so that, if possible,  $M(PG_i)$  would approximate  $M(Nb_i)$  with the highest accuracy possible (Vazirani, 2004).

The process of building a certain  $M(PG_i)$ , within this approach, is not finished at the stage of forming the initial version of a model  $M(PG_i)$ . During the process of operation of a safety system  $SB_i(CTO_i)$ , within which a model  $M(PG_i)$  is used and analysis of data  $\mathcal{X}_i(t)$  and  $Vp_i$  is performed, the task of modifying  $M(PG_i)$  so that at single steps of using prediction data it would be possible to implement such a modification  $M(PG_i)$ . When the following relation is true:  $M(PG_i) \rightarrow M[F(Nb_i)]$ , would leads to the following relation:  $M(PG_i) = M[F(Nb_i)]$ .

### Analysis of processes of occurrence of critical random events

Random processes  $\mathcal{X}_i(t)$  relating the analysis performed are assumed to be independent and values of their influence on the occurrence of a certain random event  $Vp_i$  are assumed proportional to a certain constant value  $\beta_i$ . Actually, the value of their influence on the process of  $Vp_i$  occurrences can change during the prediction interval  $\Delta t_i$ , which can increase up to the  $\Delta T_i$  value depending on the type of prediction model and on the nature of the random processes  $\mathcal{X}_i(t)$ .

To take into account this feature of random processes, approximating these processes on  $\Delta t_i$  interval must be accomplished.

In order for a random event  $Vp_i$  to occur as a result of certain set of random processes  $\{X_1(t), \dots, X_k(t)\}$  interacting with each other, it is necessary that during  $\Delta t_i$  functions  $\{[Y_1 = f(X_1)], \dots, [Y_k = f(X_k)]\}$  possess certain values. In case of events  $Vp_i$ , affecting technical objects of  $CTO_i$  type, functions  $Y_1 = f(X_1)$  can be related to various sources of their occurrence, which are dangers  $Nb = \{Nb_1, \dots, Nb_m\}$ . The corresponding  $Nb_i$  from  $Nb$  differ from each other, which leads to the possibility to distinguish single  $Y_i = f(X_i)$ . When single  $Y_i$  reach certain values  $y_i^*$  and a certain event  $Vp_i$  occurs, it does not always mean the possibility for the corresponding  $Vp_i$  to affect  $CTO_i$ . In order for  $Vp_i$  to be able to activate the corresponding attack  $At_i$  at  $CTO_i$ , it is necessary for  $CTO_i$  to be characterized by a certain threat  $Zg_i(CTO_i)$ , that can be used by  $Nb_i$  and, respectively,  $Vp_i$ . Activating an attack  $At_i$  can be written as the following relation:

$$Nb_i(CTO_i) \rightarrow Y_i(X_i) \rightarrow Vp_i \rightarrow At_i \rightarrow [Ne_i(CTO_i) \vee Ka_i(CTO_i)] \quad (3)$$

where  $Ne_i(CTO_i)$  is a malfunction that occurs because of the influence of  $At_i$ ,  $Ka_i(CTO_i)$  is a catastrophic event that can occur in cases when  $Ne_i(CTO_i)$  is an unexpected malfunction  $Ne_i^N(CTO_i)$ . In the given relation  $Nb_i(CTO_i)$  is used. This means that  $Nb_i$  has some information regarding  $CTO_i$  and can use it to organize a certain influence on  $CTO_i$ . This situation is possible regarding  $CTO_i$  and, in this case,  $Nb_i(CTO_i)$  is called not a danger, but an enemy of  $CTO_i$ . The given relation can be written in an extended form:

$$Nb_i \rightarrow \{[Y_i(X_i)] \& [Y_i \geq b_i(Y_i)]\} \rightarrow [Vp_i \& Zg_i(CTO_i)] \rightarrow At_i(CTO_i) \rightarrow [Ne_i(CTO_i) \vee Ka_i(CTO_i)] \quad (4)$$

In accordance with this relation, to implement an influence of  $Vp_i$  on  $CTO_i$  the two conjunctions  $[Y_i(X_i)] \& [Y_i \geq b_i(Y_i)]$  and  $Vp_i \& Zg_i(CTO_i)$  have to possess the value "1", or to be true. In this case, the occurrence of an event  $Vp_i$  and the arise of a catastrophic a situation at  $CTO_i$  is caused by the following factors:

1.  $Nb_i$  generates functions  $[Y_1 = f(X_1)], \dots, [Y_k = f(X_k)]$ .
2. Values  $[[Y_1 = f(X_1)] \geq b_1(y_1)], \dots, [[Y_k = f(X_k)] \geq b_k(y_k)]$ .
3.  $(Vp_i \& Zg_i) \rightarrow At_i(CTO_i) \rightarrow Ka_i(CTO_i)$ .

When building prediction models, an increase in prediction efficiency for a chosen model in most cases is based on using the most representative samples that ensure a certain degree of efficiency of a prediction process (Bidyuk, Romanenko & Timoshchuk, 2003).

Within the scope of this paper, the possibility of increasing the degree of prediction efficiency  $\mu[M(PG_i)]$  at the expense of extending the model  $M(PG_i)$  with components functionally related to it is researched. To ensure unambiguousness in the interpretation of this approach to increasing  $\mu[M(PG_i)]$ , let us consider the following initial condition.

*Condition 1.* A random event  $Vp_i$ , that activates an attack  $At_i$  in  $CTO_i$ , can lead to appearance of new threats  $Zg_i$ . Since the process of implementing the attack  $Pr(AT_i)$  is related not only to one initial component that is characterized by a threat  $Zg_i$ , but also to other components related to each other, including the initial component, which can be described as:

$$\{[Vp_i \& Zg_i(k_i)] \& (k_i \rightarrow k_j)\} \rightarrow \{[Vp_i \rightarrow Pr_{i,r}(At_i(k_i)) \rightarrow [Pr_{i,(r+1)}(At_i(k_j))]\} \quad (5)$$

If  $Pr_i(At_i)$  has finished successfully, the components  $\{k_{ij}, \dots, k_{im}\}$  can be characterized by threats  $\{Zg_{ij}, \dots, Zg_{im}\}$  because  $At_i$  uses these components in  $Pr_i(At_i)$ . In  $Nb_i$ , information is transferred via independent, separate channels regarding the success of  $At_i$  activated by an event  $Vp_i$ , which appeared because of  $Nb_i$ . A random event  $Vp_i$ , generated by a danger  $Nb_i$ , is characterized by a set of parameters  $\{h_{i1}, \dots, h_{ik}\}$  that describe the type of  $Vp_i$  and, when activating  $At_i$ , define certain features of the corresponding attack. Examples of these parameters depend on the type of  $Nb_i$  and types of  $CTO_i$  components toward which the corresponding  $Vp_i$  and  $At_i$  are oriented. In cases when  $k_{ij}$  is an information system that is used in  $CTO_i$  and written as  $IS(CTO_i)$ , then  $Nb_i$  is also an information system that generates streams of packages directed into  $IS(CTO_i)$ . An example of information that is transferred in this stream can be viruses, intrusion programs that are activated in  $IS(CTO_i)$ . and so on (Rash et. al., 2005). When a danger  $Nb_i$  is a system of a physical influence on  $CTO_i$ , an example of  $Nb_i$  can be a tool system that can use the corresponding tools to physically affect  $CTO_i$ . A similar situation takes place when  $Nb_i$  is an object of a natural type.

*Condition 2.* When activating  $Pr_i(At_i)$ , fragments are used in  $CTO_i$  from  $Pr_i(CTO_i) = \{pr_{i1}(k_{i1}) \rightarrow \dots \rightarrow pr_{im}(k_{im})\}$  which lead to an increasing number of threats.

When predicting  $Vp_i^N$  and, respectively,  $At_i^N$  the following additional information should be considered:

- Information regarding an  $CTO_i$  object that a danger  $Nb_i$  possesses;
- Information regarding the attack goal  $C_i(At_i^N)$ , which is defined more accurately at each implementation step  $C_i(At_i^N)$ ;
- Each random event  $Vp_i^N$  is characterized by a set of parameters  $H(Vp_i) = \{h_{i1}, \dots, h_{ik}\}$ , that are used at various implementation steps of  $Pr_i(At_i)$ .

### Prediction systems and implementation of affecting the prediction parameters

One or more attacks on  $CTO_i$  are dangerous when  $CTO_i$  is vulnerable to an influence of  $Vp_i^N$ . This vulnerability means that in  $CTO_i$  there are certain threats  $Zg_i(CTO_i)$  that allow an event  $Vp_i^N$  to activate the corresponding processes of attack implementation  $Pr_i(At_i)$  in  $CTO_i$ . Threats  $Zg_i$  in  $CTO_i$  can exist since the building an object functional operation of an object. In the last case, threats as a result of incomplete and unsuccessful attacks and a decrease in the object's resource value.

It is only reasonable to perform an analysis on events that can have a negative influence on the  $CTO_i$ . Thus, it is natural to extend the prediction process by defining a degree of negativity of a possible  $Vp_i$ . The  $Vp_i$  and its respective  $At_i$  of this type belong to the class of unexpected  $Vp_i^N$  and  $At_i^N$ .

Since an attack,  $At_i^N$ , represents the last stage of activating the processes of a negative influence on  $CTO_i$ , we will discuss  $At_i^N$ . The first stage of a negative influence is an activation stage  $Vp_i^N$  that occurs in  $Nb_i$ . Information in  $Nb_i$  is formed as a result of implementing the procedures of data analysis regarding an  $CTO_i$  object. The data in most cases is outside of the object but can be obtained from the object itself. A danger  $Nb_i$  regarding  $CTO_i$  is an autonomous object. Thus, data about  $CTO_i$  stored in  $Nb_i$  can only be defined on the basis of analyzing parameters that characterize  $Vp_i^N$ . Considering this, besides identifying the moment of occurrence of the  $Vp_i^N$ , that is defined by a model  $M(PG_i)$ , it is reasonable to recognize an information image  $Im_i$ , that is implemented by a model  $M(RIm_i)$ . Implementation of a model  $M(RIm_i)$  depends on  $Vp_i^N$  type. For example, if  $Vp_i^N$  is an information package that is transferred via Internet, then  $H_i(Vp_i^N)$  is text and numeric information in single packages. In this case,  $M(RIm_i)$  implements recognition of texts and numbers. If  $Vp_i^N$  is a weather change,

the parameters  $h_{ij} \in H_i$  can be changes in pressure, wind force, environment temperature and so on. The model  $M(RIm_i)$ , in this case, is a system of tools used to analyze the given parameters. For example, to determine the estimation of a storm weather value (Wiszniewski, 1989). So, the first extension of  $M(PG_i)$  is a model  $M(RIm_i)$ . The next stage of implementing the influence of  $Nb_i$  on  $CTO_i$  is an activation of an attack  $At_i^N$  by the event  $Vp_i^N$  incorporating a threat  $Zg_i$ . This activation leads to the development of the process  $Pr_i(At_i^N)$ . This process is called an intrusion in information systems (Dudek, 2005). So, the next extension of the prediction model is a model of detecting intrusions  $M(VIn_i)$  in the corresponding environment.

In this case, prediction lies not only in detecting a certain event  $Vp_i^N$ , but, also in detecting a possible negative influence on  $CTO_i$  performed by an attack  $At_i^N$ . Based on the given extensions of the prediction model  $M(PG_i)$  by models  $M(RIm_i)$  and  $M(VIn_i)$ , some general prediction system is created:

$$SPG = F[M(PG_i), M(RIm_i), M(VIn_i)] \quad (6)$$

There can be situations when  $SPG$  will consist of a larger number of components or other extensions that can be used in  $SPG$ . This means that the system  $SPG$  is different from a single prediction model  $M(PG_i)$  because in  $SPG$ , besides the direct prediction, a set of processes is implemented that are related to the attacks  $At_i^N$  occurring and influencing the object. The prediction model by its very nature functions as an informer regarding the events  $Vp_i^N$ . The prediction system  $SPG$ , in addition to the functions of  $M(PG_i)$ , implement processes oriented towards determining the possibilities of a specific  $Vp_i^N$  on their influence on  $CTO_i$  and determining the possible counter-actions to the influence of attacks  $At_i^N$ , activated by events  $Vp_i^N$ . These factors extend the interpretation of determining the possibility of a negative influence of random events  $Vp_i^N$  and a danger  $Nb_i$ , as a whole, on the  $CTO_i$  object. Another aspect of interpretation of the given extensions regarding prediction concepts lies in the fact that, thanks to using the given extensions, the time interval of predicting  $\Delta t_i$  on the occurrence of a negative influence on  $CTO_i$  shortens. This change of the key prediction parameter occurs due to the fact that events of  $Vp_i^N$  type lose the status of a dangerous event that could become critical for  $CTO_i$  if  $SB(CTO_i)$  neutralized the corresponding influence. Because of this, the following definition is introduced:

*Definition 4.* A functional prediction is a prediction within which a prediction model  $M(PG_i)$  is

linked to other models that solve tasks closely related to predicting random events.

In the given case, the model used to detect threats  $Zg_i$  allows for the decrease in the number of events, including  $Vp_i^K$ , that are critical for the given  $CTO_i$ . The result of using  $M(PG_i)$ , that is the value  $\Delta t_i$ , is used to determine the period of monitoring the vulnerable elements of  $CTO_i$ . The model of recognizing an information image  $M(RIm_i)$  that is formed on the basis of data about predicted events  $Vp_i^N$  and, respectively, about  $At_i^N$  that are described by parameters  $H_i(Vp_i^N \vee At_i^N)$ . This allows the model to make decisions regarding the need to check a single vulnerable component or a threat  $Zg_i$  during the process of  $CTO_i$  monitoring.

Additionally, in the *SPG* system a model of calculating the value of the current object resource  $M(VR)$  is included. This can be considered a model of determining the functioning time of an object that still exists in  $CTO_i$  (Kolowrocki, 2004). This model is aimed at detecting new occurring vulnerable elements in  $CTO_i$ , that is caused by natural decrease of the value of an object resource and is caused by influence of attacks on  $CTO_i$  that occur during the operation process of  $CTO_i$  and influence of other factors that can lead to decrease of the resource value. Vulnerable elements of  $CTO_i$  that are detected can be turned into threats  $Zg_i$ . So, the model  $M(VR)$  detects vulnerable elements that have to be modified in order to avoid turning this element into a new threat. It is known that extending the resource of  $CTO_i$  is ensured by the corresponding repair service. Thus, the results of the model  $M(VR)$  are used to determine the extent of maintenance and system down time. Thanks to this, it is possible to avoid initializing the work that is performed when the corresponding  $CTO_i$  components fail.

## Conclusions

A processes of predicting random events that are critical towards the  $CTO_i$  objects is researched.

Analysis of critical events is performed and a set of features that define the corresponding events as critical status is reviewed.

To extend the possibilities of process of predicting critical events, research of a method of extending the prediction with processes that interact with the prediction is discussed. The recognition processes or the identification of a random event that is predicted, the process of detecting the possible implementation of a random event influencing  $CTO_i$ , and, a process of detecting changes of values of  $CTO_i$  resource is also reviewed. These processes, together with the prediction process, make up a prediction system that not only defines a random event related to  $CTO_i$ , but detects among them a critical event for  $CTO_i$ . This, in general, allows an interpretation of possibilities of a prediction system as a tool for predicting random critical events.

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