



Formulating delamination-fretting wear failure predictive equation in HAp coated hip arthroplasty using multiple linear regression model

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ABSTRACT

Purpose: Present paper addresses the formulation of delamination-fretting wear failure predictive equation in HAp-Ti-6Al-4V interface of hip arthroplasty femoral stem component using multiple linear regression model.

Design/methodology/approach: A finite element computational model utilising adaptive meshing algorithm via ABAQUS/Standard user subroutine UMESHMOTION is developed. The developed FE model is employed to examine effect of different HAp-Ti-6Al-4V interface mechanical and tribological properties on delamination-fretting wear behaviour. The FE result is utilised to formulate predictive equations for different stress ratio conditions using multiple linear regression analysis.

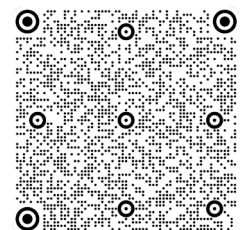
Findings: Delamination-fretting wear predictive equations are successfully formulated with significant goodness of fit and reliability as a fast failure prediction tool in HAp coated hip arthroplasty. The robustness of predictive equations is validated as good agreement is noted with actual delamination-fretting wear results.

Research limitations/implications: The influence of different mechanical and tribological properties such as delamination length, normal loading, fatigue loading, bone elastic modulus and cycle number under different stress ratio on delamination-fretting wear failure is analysed to formulate failure predictive equations.

Practical implications: The formulated predictive equation can serve as a fast delamination-fretting wear failure prediction tool in hip arthroplasty femoral stem component.

Originality/value: Limited attempt is done to explore the potential of utilizing multiple linear regression model to predict failures in hip arthroplasty. Thus, present study attempt to formulate delamination-fretting wear failure predictive equation in HAp -Ti-6Al-4V interface of hip arthroplasty femoral stem component using multiple linear regression model.

Keywords: Hip arthroplasty, Delamination, Fretting wear, HAp, Regression



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BIOMEDICAL AND DENTAL MATERIALS AND ENGINEERING**1. Introduction**

Over the past century, there has been a dramatic increase in hip arthroplasty application due to increased osteoarthritis condition [1]. Osteoarthritis is one of the major hip disorders which can lead to a number of complications such as immobility, chronic joint pain and permanent disability. Hip arthroplasty is required to replace the worn hip joint due to osteoarthritis condition. Recent evidence suggests that 88.8% of hip arthroplasty is attributable to osteoarthritis condition [2,3]. High strength, low weight and corrosion resistance are among the interesting characteristics of Ti-6Al-4V alloy to be utilized as common material in hip arthroplasty [4,5]. However, bond between human bone and Ti-6Al-4V hip arthroplasty is required to overcome biocompatibility issue [6,7].

Hydroxyapatite (HAp) is a suitable bio-ceramic material to promote bond between human bone and Ti-6Al-4V hip arthroplasty. However, the effectiveness of HAp coating is greatly challenged in long term usage more than 10 years [8,9]. HAp coated hip arthroplasty femoral stem component is susceptible to delamination-fretting wear failure which can lead to subsequent life-threatening risks such as surrounding organ inflammations and revision surgery [10]. Many researchers attempted to investigate the delamination and fretting wear condition in hip arthroplasty using experimental and numerical approaches. It has been conclusively been shown that hip arthroplasty fretting wear behavior at head-neck junction can be predicted using computational wear modelling method [11,12]. Otsuka et al. [1] and Nagentrau et al. [10] have examined delamination and fretting wear failure behavior at hip arthroplasty femoral stem component using wear modelling approach. It should be noted that costly and high computational time experimental and numerical research are often required to evaluate the fretting wear behavior in hip arthroplasty. This motivates the formulation of maximum delamination-fretting wear depth prediction tool using regression model to assist in reducing the amount of testing required and better design process of HAp coated hip implants.

Regression analysis is one of the statistical tools that can be incorporated in predicting engineering failure [13]. The main objective of regression analysis is to serve as

prediction tool by examining the relationship between criterion/dependent and predictor/independent variables [14]. Regression analysis with single and multiple predictor/independent variables are known as simple linear regression and multiple linear regression respectively [13]. In fact, regression model rarely predicts dependent variable in perfect manner. Thus, determination coefficient or known as R square values is often used as an indicator to evaluate regression model goodness of fit. Pradhan et al [15] adopted multiple linear regression analysis to predict landslides and slope failures and he concluded that the predicted outcome shows good agreement with actual data. Multiple linear regression model can assist as fast failure prediction tool in many engineering applications which can minimize costly and time consuming experimental or numerical approaches.

However, limited attempt is done to explore the potential of utilizing multiple linear regression model to predict failures in hip arthroplasty. Thus, present research seeks to formulate delamination-fretting wear failure predictive equation in HAp-Ti-6Al-4V interface of hip arthroplasty femoral stem component subjected to different mechanical and tribological properties using multiple linear regression model. The outcome of this research can serve as novel and fast failure prediction tool.

2. Methodology**2.1. Finite element (FE) model**

A finite element (FE) computational model is developed based on modified Archard wear equation to predict delamination-fretting wear. The two-dimensional plane strain case FE model consisting contact pad (bone), HAp (coating) and Ti-6Al-4V (substrate) is modelled to mimic loading condition in HAp coated hip stem arthroplasty. The assigned Young's modulus for contact pad, HAp and Ti-6Al-4V are 1 GPa, 70 GPa and 110 GPa respectively. The loading and boundary condition of FE model is presented in Figure 1a. The FE model is fixed at bottom and side to constrain translational and rotational relative motion. The FE model is subjected to normal and cyclic fatigue stress. The FE mesh module is shown in Figure 1b where

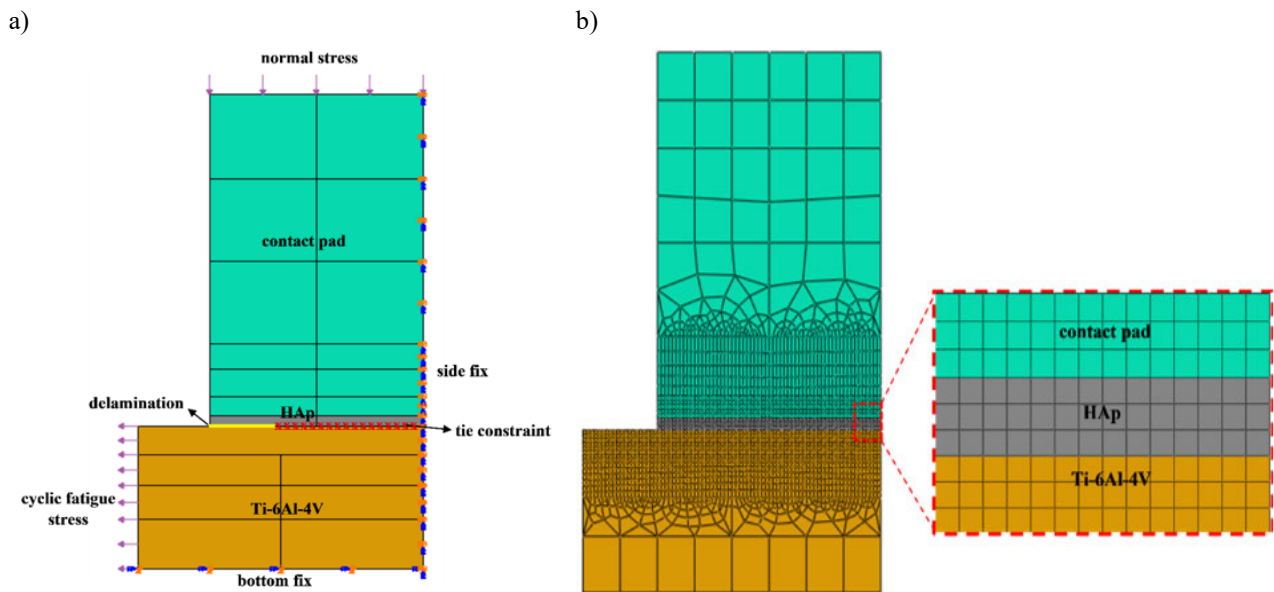


Fig. 1. FE model (a) loading and boundary condition and (b) mesh module

CPE4-A4-node bilinear plane strain quadrilateral elements with 50 μm mesh size assigned at the contact region. The mesh transition from fine to coarse is achieved via edge seeding technique.

Surface to surface contact with Lagrange Multiplier contact algorithm is assigned between HAp coating and Ti-6Al-4V with friction coefficient of 0.7. The delamination length of FE model is controlled using tie constraint approach. The delamination-fretting wear computation is performed using adaptive meshing algorithm via ABAQUS/Standard user subroutine UMESHMOTION. The FE simulation is performed with individual static general steps for 1 second time period (0.02 second increment). 1 million cycle is simulated with appropriate cycle jump of 10,000. Among the focussed mechanical and tribological variables are delamination length (0.25-1.0 mm), normal loading (20-30 MPa), fatigue loading (250-350 MPa), bone elastic modulus (0.1-20.0 GPa) and cycle number (10,000-1000,000) under different stress ratio ($R = 0.1$, $R = 10$ and $R = -1$). The predicted maximum delamination-fretting wear results are recorded in Excel software to formulate predictive equations using multiple regression model to serve as fast failure predictive tool.

2.2. Multiple linear regression model

A multiple regression model is formulated for fast prediction of maximum delamination-fretting wear depth at HAp-Ti-6Al-4V interface in artificial femoral stem

component. Regression model is adopted to formulate predictive equation to establish relationship between two or more variables [14-16]. Maximum delamination-fretting wear depth is assigned as dependent variable to indicate severity of failure at HAp-Ti-6Al-4V interface. Meanwhile, independent variables such as delamination length, normal loading, fatigue loading range, bone elastic modulus, number of cycle and stress ratio are assigned as factors that influence dependent variable. Excel multiple regression analysis is most common statistical tool to describe variation of independent variable on dependent variable [17-20].

A multiple linear regression model is employed as independent variables such as delamination length, normal loading, fatigue loading range, bone elastic modulus, number of cycle and stress ratio displaying a linear relationship trend with maximum delamination-fretting wear depth. The multiple linear regression model equation is given as Eq. 1 below:

$$y = a + b_1x_1 + b_2x_2 + b_3x_3 + \dots + b_nx_n \quad (1)$$

where, y is dependent variable (maximum delamination-fretting wear depth), x 's are independent variable (delamination length, normal loading, fatigue loading range, bone elastic modulus, number of cycle and stress ratio) and b 's are coefficient of independent variables. The goal of the multiple linear regression model using Excel software is to formulate an appropriate predictive model as a failure prediction tool in terms of maximum delamination-fretting wear depth in order to determine best fitting coefficients from finite element analysis results. The multiple linear

regression analysis is performed for four condition, i.e., stress ratio, $R = 0.1$, $R = 10$, $R = -1$ and combined stress ratio respectively.

3. Results and discussion

Figure 2 shows the maximum delamination-fretting wear finite element outcome in term of number of cycle effect under different stress ratio. The increasing trend in maximum delamination-fretting wear is noted when number of cycle increases. Similarly, the outcome of the maximum delamination-fretting wear results subjected to different mechanical and tribological properties of HAp-Ti-6Al-4V interface from FE analysis is captured as data points to formulate fast and novel failure prediction tool using multiple linear regression analysis. Multiple linear regression model is chosen to be sufficient to formulate failure predictive equation as a linear relationship between the dependent variable (maximum delamination-fretting wear depth) and the independent variables (delamination length, normal loading, fatigue loading, bone elastic modulus, stress ratio and cycle number) is registered based on FE results.

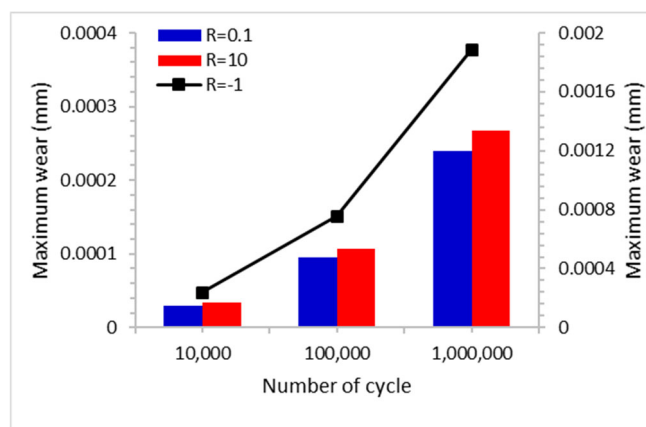


Fig. 2. Effect of cycle number on maximum wear depth under different stress ratio

3.1. Multiple linear regression model of stress ratio, $R = 0.1$

Table 1 presents multiple regression analysis output for stress ratio, $R = 0.1$ condition. Seventeen (17) sets of data are utilised to formulate maximum delamination-fretting wear depth prediction model for stress ratio, $R = 0.1$ condition. The resulting multiple linear regression equation for tensile-tensile ($R = 0.1$) condition is shown in Eq. 2 below:

$$Y = (-3.53005 \times 10^{-4}) + (6.90156 \times 10^{-5})x_1 + (-3.47320 \times 10^{-6})x_2 + (1.48643 \times 10^{-6})x_3 + (3.77302 \times 10^{-6})x_4 + (1.84889 \times 10^{-10})x_5 \quad (2)$$

where, Y is maximum delamination-fretting wear depth, x_1 is delamination length, x_2 is normal loading, x_3 is fatigue loading range, x_4 is bone elastic modulus and x_5 is cycle number. It is apparent from data that the formulated maximum delamination-fretting wear depth predictive model for stress ratio, $R = 0.1$ condition displays a strong correlation between dependent and independent variables. This is reflected by Multiple R (correlation coefficient), R Square (coefficient of determination) and Adjusted R square values which near to value 1 indicating a strong positive relationship. In fact, R Square value 0.97 demonstrating goodness of fit with lower variation proportion of dependent variable that predicted from set of independent variables in multiple linear regression. In addition, the smaller value of standard error which is equivalent to 1.51×10^{-5} represents great certainty of formulated predictive equation.

The Significance F value of 9.82×10^{-8} (less than (0.05)) indicates higher reliability (statistically significant) of predicted results using formulated regression equation for present condition. Besides that, P -value lesser than 0.05 specifies the significance of an independent variable on maximum delamination-fretting wear depth prediction. The most significant variable that dictating maximum delamination-fretting wear depth is cycle number followed by bone elastic modulus, fatigue loading range and delamination length, meanwhile normal loading (higher than 0.05) is considered as least significant independent variable.

3.2. Multiple linear regression model of stress ratio, $R = 10$

Table 2 shows multiple regression analysis output for stress ratio, $R = 10$ condition. The multiple linear regression equation is formulated from seventeen (17) sets of data. The resulting multiple linear regression equation for compressive-compressive ($R = 10$) condition is given as Eq. 3 below:

$$Y = (-3.36745 \times 10^{-4}) + (7.02241 \times 10^{-5})x_1 + (-4.16800 \times 10^{-6})x_2 + (1.49356 \times 10^{-6})x_3 + (3.93090 \times 10^{-6})x_4 + (2.08678 \times 10^{-10})x_5 \quad (3)$$

where, Y , x_1 , x_2 , x_3 , x_4 and x_5 are maximum delamination-fretting wear depth, delamination length, normal loading, fatigue loading range, bone elastic modulus and cycle number respectively.

Table 1.
Multiple regression analysis output for stress ratio, R = 0.1
SUMMARY OUTPUT (R = 0.1)

<i>Regression Statistics</i>					
Multiple R		0.983083381			
R Square		0.966452934			
Adjusted R Square		0.951204268			
Standard Error		1.51164E-05			
Observations		17			

ANOVA					
	<i>df</i>	<i>SS</i>	<i>MS</i>	<i>F</i>	<i>Significance F</i>
Regression	5	7.24133E-08	1.44827E-08	63.37950571	9.81565E-08
Residual	11	2.51358E-09	2.28507E-10		
Total	16	7.49269E-08			

	<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>
Intercept	-3.53005E-04	0.000131844	-2.677434472	0.021506526
Delamination	6.90156E-05	1.84712E-05	3.736390588	0.003286738
Normal loading	-3.47320E-06	2.13779E-06	-1.624669583	0.132515245
Fatigue loading range	1.48643E-06	3.54048E-07	4.198381978	0.001489642
Bone elastic modulus	3.77302E-06	7.80512E-07	4.834024851	0.000523979
Cycle number	1.84889E-10	1.24853E-11	14.80856041	1.30456E-08

Table 2.
Multiple regression analysis output for stress ratio, R = 10
SUMMARY OUTPUT (R=10)

<i>Regression Statistics</i>					
Multiple R		0.98275152			
R Square		0.96580055			
Adjusted R Square		0.950255345			
Standard Error		1.68765E-05			
Observations		17			

ANOVA					
	<i>df</i>	<i>SS</i>	<i>MS</i>	<i>F</i>	<i>Significance F</i>
Regression	5	8.84759E-08	1.76952E-08	62.12851915	1.09032E-07
Residual	11	3.13297E-09	2.84816E-10		
Total	16	9.16089E-08			

	<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>
Intercept	-3.36745E-04	0.000147195	-2.2877438	0.042947689
Delamination	7.02241E-05	2.06218E-05	3.405331572	0.005873498
Normal loading	-4.16800E-06	2.3867E-06	-1.746347276	0.108577029
Fatigue loading range	1.49356E-06	3.95271E-07	3.778580506	0.003054586
Bone elastic modulus	3.93090E-06	8.71389E-07	4.511067928	0.000884944
Cycle number	2.08678E-10	1.3939E-11	14.97076663	1.1633E-08

The outcome quite revealing that a strong correlation between dependent (maximum delamination-fretting wear depth) variable and independent variables (delamination length, normal loading, fatigue loading range, bone elastic modulus and cycle number) as strong positive relation (near to 1) shown by Multiple R (correlation coefficient), R Square (coefficient of determination) and Adjusted R square values.

The multiple regression output provide evidence that goodness of fit is achieved due to R Square value is equivalent to 0.97 and lower standard error of 1.68×10^{-5} . Besides that, Significance F value of 1.09×10^{-7} proves the formulated predictive equation is statistically significant with higher reliability as less than 0.05. The most significant independent variable dominating maximum delamination-fretting wear depth for stress ratio, R = 10 (compressive-compressive) condition is number of cycles followed by bone elastic modulus, fatigue loading range and delamination length. Whereas, normal loading is least significant independent variable as P-value is higher than 0.05.

3.3. Multiple linear regression model of stress ratio, R = -1

Table 3 exhibits multiple regression analysis output for stress ratio, R = -1 condition. Seventeen (17) data sets are

employed to formulate multiple linear regression equation to predict maximum delamination-fretting wear depth. The formulated multiple linear regression equation for tensile-compressive R = -1 condition is represented as in equation Eq. 4 below:

$$Y = (4.82782 \times 10^{-4}) + (-1.60705 \times 10^{-4})x_1 + (-2.19460 \times 10^{-5})x_2 + (8.56655 \times 10^{-7})x_3 + (2.75312 \times 10^{-5})x_4 + (1.10067 \times 10^{-9})x_5 \quad (4)$$

where, Y is maximum delamination-fretting wear depth, x_1 is delamination length, x_2 is normal loading, x_3 is fatigue loading range, x_4 is bone elastic modulus and x_5 is cycle number. Multiple R (correlation coefficient), R Square (coefficient of determination) and Adjusted R square values indicating a good agreement between dependent and independent variables. The minimal variation between predicted and observed outcome is registered due to R Square value of 0.72 and lower standard error of 2.98×10^{-4} indicating acceptable goodness of fit.

In addition, formulated predictive equation for tensile-compressive (R = -1) condition is statistically significant with acceptable reliability with Significance F value of 0.0078 which is lower than 0.05. The most significant single variable influencing maximum delamination-fretting wear depth is cycle number with P-value lower than 0.05.

Table 3. Multiple regression analysis output for stress ratio, R = -1
SUMMARY OUTPUT (R=-1)

Regression Statistics					
Multiple R	0.849237888				
R Square	0.72120499				
Adjusted R Square	0.594479985				
Standard Error	0.000297608				
Observations	17				
ANOVA					
	df	SS	MS	F	Significance F
Regression	5	2.52031E-06	5.04063E-07	5.691102497	0.00782956
Residual	11	9.74274E-07	8.85703E-08		
Total	16	3.49459E-06			
	Coefficients	Standard Error	t Stat	P-value	
Intercept	4.82782E-04	0.002595708	0.18599244	0.855836162	
Delamination	-1.60705E-04	0.000363655	-0.441917721	0.667110858	
Normal loading	-2.19460E-05	4.20881E-05	-0.521430282	0.612403806	
Fatigue loading range	8.56655E-07	3.13667E-06	0.273109443	0.789828505	
Bone elastic modulus	2.75312E-05	1.53665E-05	1.791639425	0.100710237	
Cycle number	1.10067E-09	2.45807E-10	4.477806047	0.000934778	

Meanwhile, other additional independent variables are less significant which can be arranged by bone elastic modulus, normal loading, delamination length and fatigue loading in ascending order (towards least significant).

3.4. Multiple linear regression model of combined stress ratio

Additional multiple linear regression analysis is performed with the goal to cater all stress ratio condition in one formulated single predictive equation. Table 4 presents multiple regression analysis output for combined stress ratio, $R = 0.1, 10$ and -1 conditions respectively. The number of data sets are increased to fifty-one (51) to guarantee the robustness of formulated multiple linear regression equation to predict maximum delamination-fretting wear depth. An additional independent variable which is stress ratio is added with other variables as discussed previously in formulating single stress ratio predictive equations. The resulting multiple linear regression equation for combined stress ratio condition is presented in Eq. 5 below:

$$Y = (-1.39348 \times 10^{-3}) + (1.83023 \times 10^{-5})x_1 + (5.06717 \times 10^{-6})x_2 + (3.77523 \times 10^{-6})x_3 +$$

$$(1.83526 \times 10^{-6})x_4 + (1.06388 \times 10^{-5})x_5 + (5.15551 \times 10^{-10})x_6 \quad (5)$$

where, $Y, x_1, x_2, x_3, x_4, x_5$ and x_6 are maximum delamination-fretting wear depth, delamination length, normal loading, fatigue loading range, stress ratio, bone elastic modulus and cycle number respectively. The data highlights that formulated predictive equation using multiple linear regression model for combined stress ratio cases suggesting a strong correlation between dependent variable (maximum delamination-fretting wear depth) and independent variables (delamination length, normal loading, fatigue loading range, stress ratio, bone elastic modulus and cycle number).

The result is in line with Multiple R (correlation coefficient), R Square (coefficient of determination) and Adjusted R square values which near to value 1 demonstrating a strong positive relationship. In addition, R Square value of 0.89 and standard error equivalent to 2.26×10^{-4} indicating strong goodness of fit and certainty of predictive equation.

The outcome also revealed that formulated multivariable linear regression model is highly reliable and statistically significant as Significance F value of 1.57×10^{-19} which corresponding to less than 0.05. Furthermore, the most

Table 4.
Multiple regression analysis output for combined stress ratio, $R = 0.1, 10$ and -1
SUMMARY OUTPUT (combined R)

Regression Statistics						
Multiple R					0.943758392	
R Square					0.890679903	
Adjusted R Square					0.875772617	
Standard Error					0.000225968	
Observations					51	
ANOVA						
		<i>df</i>	<i>SS</i>	<i>MS</i>	<i>F</i>	<i>Significance F</i>
Regression		6	1.8305E-05	3.05084E-06	59.74795832	1.57176E-19
Residual		44	2.24672E-06	5.10618E-08		
Total		50	2.05517E-05			
	<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>		
Intercept	-1.39348E-03	0.000344994	-4.039141721	0.000211695		
Delamination	1.83023E-05	0.000158032	0.115813986	0.90832693		
Normal loading	5.06717E-06	1.37567E-05	0.368341936	0.714384576		
Fatigue loading range	3.77523E-06	2.51647E-07	15.00208705	6.51447E-19		
Stress ratio	1.83526E-06	7.80569E-06	0.235118254	0.815207782		
Bone elastic modulus	1.06388E-05	6.67434E-06	1.593977955	0.118100081		
Cycle number	5.15551E-10	1.0679E-10	4.827712661	1.69962E-05		

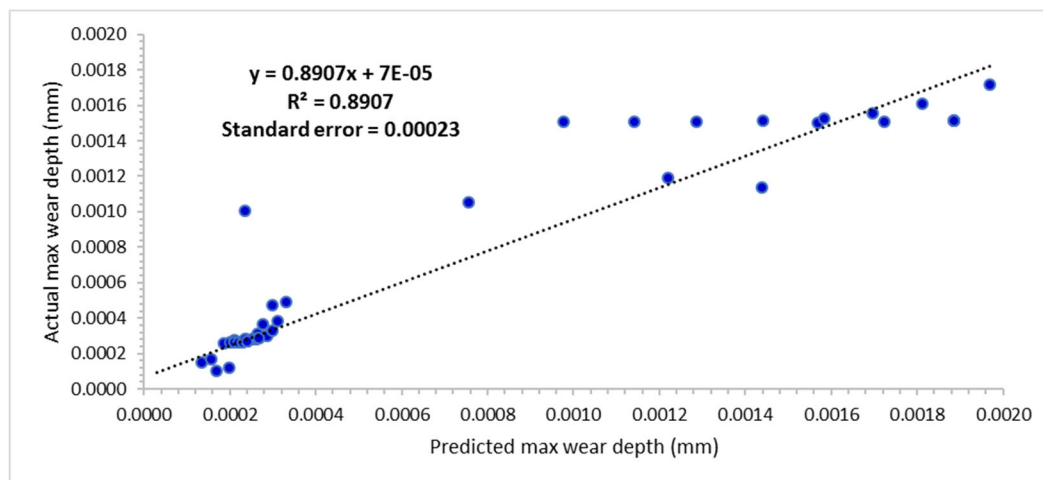


Fig. 3. Actual versus predicted max wear depth scattered plot

striking result emerge from data is that fatigue loading range followed by cycle number independent variables significantly dictating maximum delamination-fretting wear depth prediction with P-value lesser than 0.05.

Meanwhile, bone elastic modulus, normal loading, stress ratio and delamination length are least significant independent variables (P-value lesser than 0.05) in ascending order. It is apparent that formulated predictive equation using multivariable linear regression model can be adopted as a failure prediction tool for fast prediction of maximum delamination-fretting wear depth at HAp-Ti-6Al-4V interface of artificial femoral stem component in total hip replacement.

3.5. Formulated predictive equation validation

The validation of formulated predictive Eq. 5 is performed by comparing actual maximum wear depth with predicted maximum wear depth. Figure 3 presents actual versus predicted max wear depth scattered plot. A trendline is created based on the scattered plot to establish the relationship between actual and predicted values. The scattered plot is quite revealing that good agreement is achieved between actual and predicted values as R Square value of 0.8907 is registered. R Square value closer to 1 indicates strong correlation and goodness of fit with less foggy or dispersed points from trendline [21-24]. In addition, it is apparent from the data that registered standard is 0.00023. The minimal standard error defines the robustness of the formulated predictive equation. Thus, the validation of formulated predictive equation as a fast and novel failure prediction tool is successfully achieved.

4. Conclusions

This study is set to formulate delamination-fretting wear failure predictive equation in HAp-Ti-6Al-4V interface of hip arthroplasty femoral stem component using multiple linear regression analysis. The following conclusion can be drawn from the attempted research:

Maximum delamination-fretting wear predictive equations are successfully formulated using multiple linear regression analysis subjected to four condition, i.e., $R = 0.1$, $R = 10$, $R = -1$ and combined stress ratio.

The formulated predictive equations displaying a strong correlation between dependent and independent variables with R Square (coefficient of determination) near to 1 which guarantees goodness of fit.

Highly reliable and statistically significant predictive equations is adopted as fast maximum delamination-fretting wear failure prediction tool at HAp-Ti-6Al-4V interface of hip arthroplasty.

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