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Integrated software tools supporting decision making on identification, prediction and optimization of complex technical systems operation, reliability and safety

Part 4

Integrated software tools application – Exemplary system operation and reliability optimization

Keywords

operation process optimization, optimal characteristics, reliability, availability, renewal, software tools

Abstract

There is presented the application of the integrated software tools to the operation and reliability of an exemplary complex technical system optimization. First using the computer program CP 8.9 there are determined the optimal limit transient probabilities of the exemplary system operation process at the particular operation states maximizing the system lifetime in the reliability states not worse than the critical reliability state and its optimal sojourn times at the particular operation states. Program CP 8.9 allows also for automatic evaluation of the exemplary system optimal unconditional multistate reliability function, the optimal expected values and standard deviations of its unconditional lifetimes in the reliability state subsets and the optimal mean values of its lifetimes in the particular reliability states. Moreover, in the case when the system is repairable, its optimal renewal and availability characteristics are obtained using the computer program CP 8.11.

8. The exemplary system operation process optimization

8.1. Optimal transient probabilities of the system operation process at operation states

Considering the results given in [5], it is natural to assume that the system operation process has a significant influence on the system reliability. This influence is also clearly expressed for the mean values of the system unconditional lifetimes in the reliability state subsets that can be used for the system operation process optimization performed in the accordance with the procedure proposed in Section 9.2.1 of IS&RDSS 9 [7].

To determine the optimal characteristics of the exemplary system reliability and risk: the optimal unconditional reliability function, the optimal mean values of unconditional lifetimes in the reliability state subsets, the optimal risk function of the system and the optimal moment when the system risk exceeds a permitted level we use the computer program CP 8.9 "Optimization of system operation and reliability" [2].

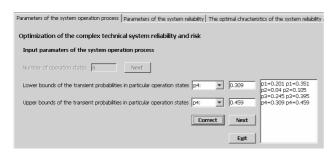
The computer program is composed of three panels. The first panel "Parameters of the system operation process" is used for reading input parameters of the system operation process [6]:

– the number of operation states of the system operation process v,

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- the lower bounds of the transient probabilities p_b , $b = 1,2,...,\nu$, in particular operation states \breve{p}_1 , \breve{p}_2 , ..., \breve{p}_{ν} ,
- the upper bounds of the transient probabilities p_b , $b = 1,2,...,\nu$, in particular operation states \hat{p}_1 , \hat{p}_2 , ..., \hat{p}_{ν} ,

fixed in [9].



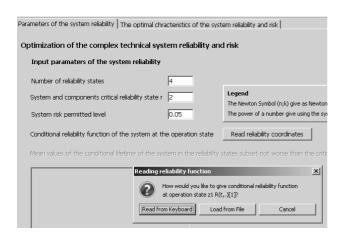
The second panel "Parameters of the system reliability" is served for reading input parameters of the system reliability model [2]:

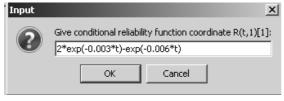
- the number of the system and components reliability states z + 1,
- the system and components critical reliability state
 r,
- the conditional reliability function of the system at the operation state z_b , b = 1,2,...,v,

$$[\mathbf{R}(t,\cdot)]^{(b)} = [1,[\mathbf{R}(t,1)]^{(b)},...,[\mathbf{R}(t,z)]^{(b)}],$$

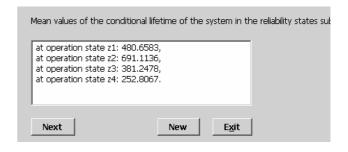
for b = 1, 2, ..., v, determined in Section 6 [5],

– the system risk permitted level δ .

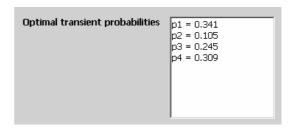




After giving the last coordinate of the conditional reliability function, the computer program determines and shows in the Text Area the mean values of the system conditional lifetimes $\mu_b(r)$, $b = 1, 2, ..., \nu$, in the reliability states subset not worse than the system critical reliability state r.



Then the computer program determines [6] the optimal transient probabilities $\dot{p}_1, \dot{p}_2, ..., \dot{p}_{\nu}$, of the complex technical system operation process.



8.2. Optimal sojourn times of the system operation process at operation states

Having the values of the optimal transient probabilities determined in Section 8.1, it is possible to find the optimal unconditional and conditional mean values of the sojourn times of the exemplary system operation process at the operation states and the optimal mean values of the total unconditional sojourn times of the exemplary system operation process at the operation states during the fixed operation time as well.

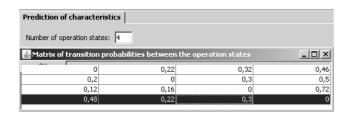
Considering, obtained from Section 8.1, the optimal transient probabilities at operation states

$$\dot{p}_1 = 0.341, \ \dot{p}_2 = 0.105, \ \dot{p}_3 = 0.245, \ \dot{p}_4 = 0.309,$$

in [9] there are determined the optimal mean values \dot{M}_b of the exemplary system unconditional sojourn times in the operation states

$$\dot{M}_1 \cong 675, \ \dot{M}_2 \cong 290, \ \dot{M}_3 \cong 490, \ \dot{M}_4 = 400.$$

Then using the probabilities [4]



and the optimal values \dot{M}_{bl} of the mean values M_{bl} of the conditional sojourn times at operation states

	Mean values of conditional sojurn times of system operation process at op 🔳 🗆 🔀						
	0	200	500	1 024			
Ì	100	0	100	480			
	900	500	0	419			
	300	500	487	0			

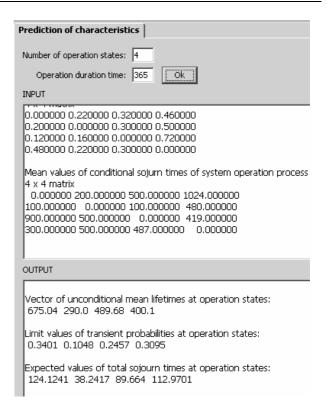
determined in [9], applying the computer program CP 8.5 we can obtain the optimal mean values of the total unconditional sojourn times of the exemplary system operation process at the operation states during the fixed operation time $\theta = 1$ year = 365 days. In the window below there are presented results of the computer porgram CP 8.5.

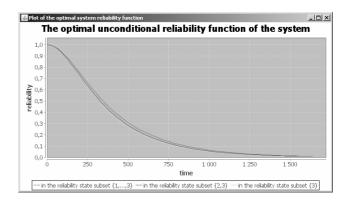
9. The exemplary system reliability optimization

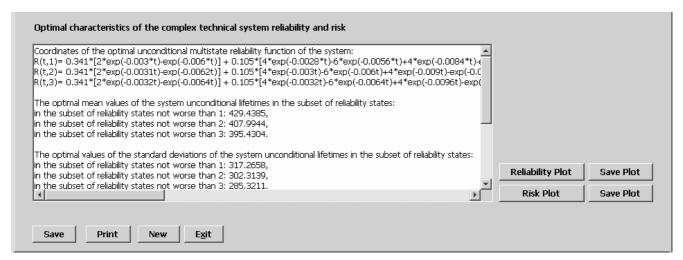
In the third panel "The optimal characteristics of the system reliability and risk" there are presented the results of the program. Namely, the computer program CP 8.9 determines the following characteristics [6]:

 the coordinates of the optimal unconditional multistate reliability function of the system (with plotting)

$$\dot{\mathbf{R}}(t,\cdot) = [1, \dot{\mathbf{R}}(t,1), \dots, \dot{\mathbf{R}}(t,z)], t \ge 0,$$

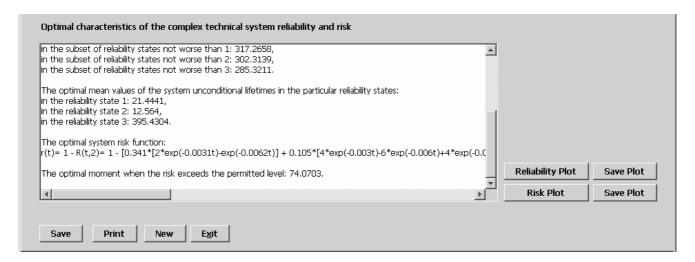




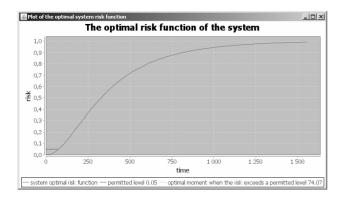


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- the optimal mean values $\dot{\mu}(u)$ of the system unconditional lifetimes in the reliability state subsets $\{u, u+1, ..., z\}, u=1, 2, ..., z$,
- the optimal values $\dot{\sigma}(u)$ of the standard deviations of the system unconditional lifetimes in the system reliability state subsets $\{u, u+1,..., z\}$, u=1,2,...,z,
- the optimal mean values $\dot{\overline{\mu}}(u)$ of the system unconditional lifetimes in the particular reliability states u = 1, 2, ..., z,
- the optimal system risk function (with plotting) $\dot{r}(t)$, $t \ge 0$,
- the optimal moment $\dot{ au}$ when the risk exceeds the permitted level δ



10. The exemplary system renewal and availability optimization

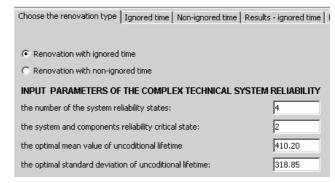
To determine the optimal renewal and availability characteristics of the exemplary system after its operation process optimization, we use the results of the system reliability characteristics optimization performed in Sections 8 and 9 and the results of the Section 11.2 of IS&RDSS 11 [7].

In the case when the exemplary system renovation time is ignored, considering the optimal values $\dot{\mu}(2)$ and $\dot{\sigma}(2)$ determined in Section 9, we predict the optimal renewal and availability characteristics of the exemplary system using the computer program CP 8.11 "Optimization of system availability" [3].

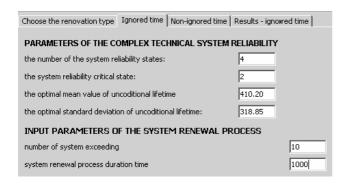
The computer program is reading:

- the number of the system reliability states,
- the system critical reliability state r,
- the optimal mean value $\dot{\mu}(r)$ of the unconditional lifetime of the system in the reliability states subset not worse than the system critical reliability state r,
- the optimal standard deviation $\dot{\sigma}(r)$ of the unconditional lifetime of the system in the reliability states subset not worse than the system critical reliability state r,

from results of Section 9 and from [9],



- the number *N* of the system exceeding the critical reliability state *r* and renovations,
- the system renewal process duration time t.



The results of the predicting the optimal renewal process characteristics of the exemplary system in case the renovation time is ignored are given in the "Results – ignored time" tab below.

Choose the renovation type Ignored time Non-ignored time Results - ignored time Results - non-ignored time
RESULTS:
the distribution of the optimal time until the Nth exceeding of reliability critical state r of this system: 7,102, 1,008.29)
the expected value: 4,102 and the variance of the optimal time: 1,016,653.23
the distribution of the optimal number of exceeding the reliability critical state r of this system:
the expected value 2.44 and the variance 1.47 of optimal number of the exceeding the reliability critic.

Each characteristic can be presented in the table of values for fixed parameter *t*. For example, the table of distribution values of the optimal time until the *Nth* exceeding the reliability critical state and the table of distribution values of the optimal number exceeding the reliability critical state are shown below.

🙆 Distribution of number of eceeding the reliability critical state				
N	Values			
0	0.095778460010645			
1	0.241075791391216			
2	0.319250684940067			
3	0.222591129838546			
4	0.081637804892566			
5	0.015713480636288			
6	0.001581987497007			
7	0.000082988446833			
8	0.000002259588423			
9	0.000000031817583			
10	0.00000000230967			
11	0.00000000000862			
12	0.000000000000002			
13	0			

The computer program is predicted the following characteristics of the complex technical system renewal and availability [6]:

- the distribution $\dot{F}^{(N)}(t,r), t \in (-\infty,\infty)$, of the optimal time $\dot{S}_N(r), r \in \{1,2,...,z\}$ until the *Nth* exceeding of reliability critical state r of this system, for sufficiently large N,
- the expected value $E[\dot{S}_N(r)]$ and the variance $D[\dot{S}_N(r)]$ of the optimal time $\dot{S}_N(r)$,

- $r \in \{1,2,...,z\}$ until the *Nth* exceeding the reliability critical state r of this system,
- the distribution $P(\dot{N}(t,r)=N)$, N=0,1,2,..., $r \in \{1,2,...,z\}$ of the optimal number $\dot{N}(t,r)$ of exceeding the reliability critical state r of this system up to the moment $t, t \ge 0$, for sufficiently large t,
- the expected value $\dot{H}(t,r)$ and the variance $\dot{D}(t,r)$ of the optimal number $\dot{N}(t,r)$, $r \in \{1,2,...,z\}$ of exceeding the reliability critical state r of this system at the moment $t, t \ge 0$, for sufficiently large t.

🕍 Distribution of time until Nth exceeding 👤 🔲 🔀				
t	Values			
0	0.00002368224814	\blacksquare		
1	0.000023783230095			
2	0.000023884620216			
3	0.000023986420052			
4	0.00002408863116			
5	0.000024191255099			
6	0.000024294293435			
7	0.00002439774774			
8	0.000024501619592			
9	0.000024605910573			
10	0.00002471062227			
11	0.000024815756279			
12	0.000024921314197			
13	0.000025027297631			
14	0.000025133708191			
15	0.000025240547493			
16	0.000025347817159			
17	0.000025455518817			
18	0.0000255636541			

Further, to make the estimation of the renewal and availability of the exemplary system in the case when the time of renovation is non-ignored, considering the optimal values $\dot{\mu}(2)$ and $\dot{\sigma}(2)$ determined in Section 9, assuming the mean value of the system renovation time $\mu_0(2) = 10$ years and the standard deviation of the system renovation time $\sigma_0(2) = 5$ years, we use the computer program CP 8.11 in the following way [3].

The computer program is reading:

- the number of the system reliability states,
- the system critical reliability state r,
- the optimal mean value $\dot{\mu}(r)$ of the unconditional lifetime of the system in the reliability states subset not worse than the system critical reliability state r,
- the optimal standard deviation $\dot{\sigma}(r)$ of the unconditional lifetime of the system in the reliability states subset not worse than the system critical reliability state r,

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Choose the renovation type Ignored time Non-ignored time Resu	ults - ignored time I			
C Renovation with ignored time				
Renovation with non-ignored time				
INPUT PARAMETERS OF THE COMPLEX TECHNICAL SYSTEM RELIABILITY				
the number of the system reliability states:	4			
the system and components reliability critical state:	2			
the optimal mean value of uncoditional lifetime	410.20			
the optimal standard deviation of uncoditional lifetime:	318.85			

- the *r*-th coordinate $\dot{\mathbf{R}}(t,r)$, $t \ge 0$, of the system optimal unconditional reliability function $\dot{\mathbf{R}}(t,\cdot)$ determined in Section 6 [5],

Choose the renovation type Ignored time				nored time	Results - r
PARAMETERS OF THE COMPLEX TEC	HNICAL S	YSTEM RELI	IABILITY	,	
the number of the system reliability state	es:		4		
the system and components reliability critical state:			2		
the optimal mean value of uncoditional life	etime		410.20		
the optimal standard deviation of uncodi	tional lifetin	ne:	318.85		
Input reliability function	Input		-	-	×Ι
	p.u.c	_	_	_	
INPUT PARAMETERS OF THE SYSTE		Give R(t,2)[1]			
the mean value of system renovation til		2*exp(-0.0	031t)-exp	(-0.0062t)	
the standard deviation of system renov		ОК		ancel	
number of system exceeding the critical					
renewal process duration time					
length of system availability interval					

- the mean value $\mu_0(r)$ of the system renovation time.
- the standard deviation $\sigma_0(r)$ of the system renovation time,
- the number *N* of the system exceeding the critical reliability state *r* and renovations,
- the system renewal process duration time t,
- the length of the system availability interval τ .

Choose the renovation type Ignored time	Non-ignored time	Results - ignored time			
PARAMETERS OF THE COMPLEX TECHNICAL SYSTEM RELIABILITY					
the number of the system reliability state	4				
the system and components reliability crit	2				
the optimal mean value of uncoditional lif	410.20				
the optimal standard deviation of uncodit	318.85				
Input reliability function					
INPUT PARAMETERS OF THE SYSTEM RENEWAL PROCESS					
the mean value of system renovation tim	e:	10			
the standard deviation of system renova	tion time	5			
number of system exceeding the critical r	eliability state	10			
renewal process duration time		1000			
length of system availability interval		365			

The computer program is predicted the following characteristics of the complex technical system renewal and availability [6]:

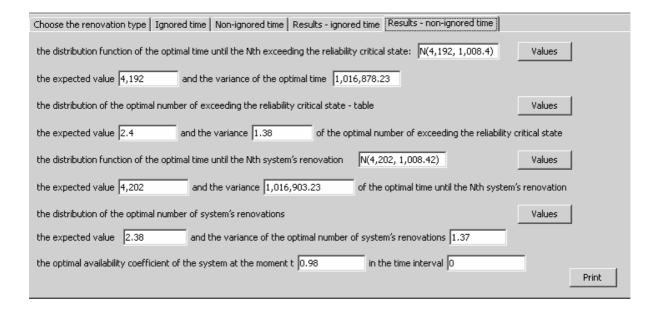
- the distribution function $\dot{\overline{F}}^{(N)}(t,r)$ = $P(\dot{\overline{S}}_N(r) < t)$, $t \in (-\infty, \infty)$ of the optimal time $\dot{\overline{S}}_N(r)$, $r \in \{1, 2, ..., z\}$, until the *Nth* exceeding the reliability critical state r of this system N = 1, 2, ..., z
- the expected value $E[\overline{S}_N(r)]$ and the variance $D[\dot{\overline{S}}_N(r)]$ of the optimal time $\dot{\overline{S}}_N(r)$, $r \in \{1,2,...,z\}$, until the *Nth* exceeding the reliability critical state r of this system,
- the distribution $P(\overline{N}(t,r)=N)$, N=1,2,... of the optimal number $\overline{N}(t,r)$, $r \in \{1,2,...,z\}$ of exceeding the reliability critical state r of this system up to the moment $t, t \ge 0$,
- the expected value $\overline{H}(t,r)$ and the variance $\dot{\overline{D}}(t,r)$ of the optimal number $\dot{\overline{N}}(t,r)$, $r \in \{1,2,...,z\}$ of exceeding the reliability critical state r of this system up to the moment $t, t \ge 0$, for sufficiently large t,
- the distribution function $\overline{\overline{F}}^{(N)}(t,r)$ = $P(\overline{\overline{S}}_N(r) < t)$, $t \in (-\infty, \infty)$ of the optimal time $\overline{\overline{S}}_N(r)$, $r \in \{1, 2, ..., z\}$, until the *Nth* system's renovation, for sufficiently large N, N = 1, 2, ...,
- the expected value $E[\overline{\overline{S}}_N(r)]$ and the variance $D[\dot{\overline{S}}_N(r)]$ of the optimal time $\dot{\overline{S}}_N(r)$, $r \in \{1, 2, ..., z\}$, until the *Nth* system's renovation,
- the distribution $P(\overline{\overline{N}}(t,r) = N)$, N = 1,2,..., of the optimal number $\overline{\overline{N}}(t,r)$, $r \in \{1,2,...,z\}$ of system's renovations up to the moment $t, t \ge 0$,
- the expected value $\overline{\overline{H}}(t,r)$ and the variance $\overline{\overline{D}}(t,r)$ of the optimal number $\overline{\overline{N}}(t,r)$, $r \in \{1,2,...,z\}$ of system's renovations up to the moment $t, t \ge 0$,
- the optimal steady availability coefficient $\dot{A}(t,r)$, $t \ge 0$, $r \in \{1,2,...,z\}$ of the system at the moment t,

- the optimal steady availability coefficient $\dot{A}(t,\tau,r), t \ge 0, \tau > 0, r \in \{1,2,...,z\}$ of the

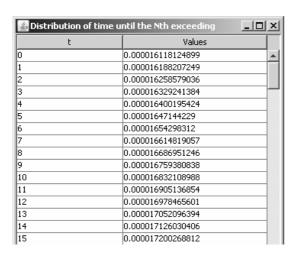
The optimal renewal and availability characteristics of the exemplary system in the case when it is repairable and its time of renovation is non-ignored are presented in the "Results – non-ignored time" tab shown below.

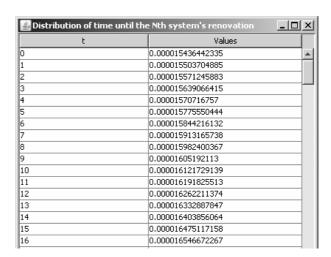
system in the time interval $\langle t, t + \tau \rangle$, $\tau > 0$.

🖺 Distribution of number of exceeding		
N	Values	
0	0.095908318587048	\blacksquare
1	0.249342555383982	
2	0.328100270939511	
3	0.218698074211274	
4	0.07375411090405	
5	0.012546889098876	
6	0.001072228036685	
7	0.000045815848068	
8	0.000000974380799	
9	0.000000010271193	
10	0.000000000053474	
11	0.00000000000137	
12	0	



Values of distribution of the optimal time until the *Nth* exceeding reliability critical state and until the *Nth* system's renovation are presented in first two tables. In the next two tables there are given values of distribution of the optimal number of system's renovation and the optimal number of exceeding the reliability critical state for fixed parameter *t*.





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🖺 Distribution of number of system's renovation		
N	Values	
0	0.098240863389695	<u> </u>
1	0.253527475649781	
2	0.329047604779527	
3	0.214953115678213	
4	0.070585118459535	
5	0.011614702978496	
6	0.000953564740319	
7	0.000038873308073	
8	0.000000783193852	
9	0.00000007765402	
10	0.00000000037754	
11	0.0000000000009	

Acknowledgements

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