An Improved Method of Permutation Correction in Convolutive Blind Source Separation

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This paper proposes an improved method of solving the permutation problem inherent in frequency-domain of convolutive blind source separation (BSS). It combines a novel inter-frequency dependence measure: the power ratio of separated signals, and a simple but effective bin-wise permutation alignment scheme. The proposed method is easy to implement and surpasses the conventional ones. Simulations have shown that it can provide an almost ideal solution of the permutation problem for a case where two or three sources were mixed in a room with a reverberation time of 130 ms.

Keywords: blind source separation, cocktail party, convolutive mixing, frequency domain, permutation problem.

1. Introduction

A typical problem in array processing and data analysis is to recover the source signals from their mixtures. Blind source separation (BSS) deals with this problem (Hyvärinen et al., 2001). In recent years, BSS has received considerable attention and became a hotspot of modern signal processing. It has many potential applications, ranging from wireless communication, speech processing, image processing, biomedicine and radar technology, even to financial data analysis. An interesting application is the separation of audio sources that have been mixed and recorded by multiple microphones in a room, i.e. the so-called cocktail party...
problem. A major challenge is that the mixing process is convolutive, i.e. the observations are combinations of filtered versions of the sources. This requires many channel parameters to be estimated.

Many approaches have been proposed to do convolutive BSS (Pedersen et al., 2007). Among them, frequency-domain approaches are considered to be promising with faster convergence and lower complexity (Smaragdis, 1998; Sawada et al., 2007a). In frequency-domain BSS, the observed time-domain signals are converted into the frequency-domain, e.g. using the short-time Fourier transform (STFT), and then instantaneous BSS is applied to each frequency bin, after which the separated signals of all frequency bins are combined and re-transformed to the time-domain. An issue with frequency-domain BSS is that the permutation ambiguity may become serious. Even if satisfactory separation in each frequency bin is achieved, combining of the separated frequency bins to recover the original sources is difficult because of the unknown permutations associated with individual frequency bins.

Considerable work has been done to tackle the permutation problem. A popular strategy is to exploit mutual dependence of bin-wise separated signals across the frequencies, which tends to be high if the components originate from the same source (Murata et al. 2001; Sawada, 2007b). Another strategy is based on the direction-of-arrival estimations. By estimating the arriving delays of sources or analyzing the directivity pattern formed by a separation matrix, source direction can be estimated and permutations aligned (Sawada et al., 2004; Ikram, Morgan, 2005). The advantage of the first strategy over the second one is that it is less affected by adverse mixing conditions such as reverberation and sources being closely located. Thus, this paper focuses on solving the permutation problem based on inter-frequency dependence. We will consider two issues: a metric to measure the inter-frequency dependence, and a scheme to align the permutation across the frequencies.

A classical method, proposed by Murata (2001), aligns permutation based on an inter-frequency dependence measure: separated signal envelopes. The bin-wise permutation alignment scheme in (Murata et al., 2001) is straightforward. However, since the envelope dependence can only be clearly observed in a small percentage of all frequencies, the method in (Murata et al., 2001) is limited when dealing with many sources. Recently, a method proposed by Sawada (2007b) tries to solve the permutation problem based on another measure: separated signal power ratio, with which the inter-frequency dependence is more clearly exhibited. However, the alignment scheme in (Sawada et al., 2007b) involves a K-mean clustering step, which is unsupervised and it is difficult to control it. In addition, the performance of (Sawada et al., 2007b) also degrades with increasing number of sources.

Considering the advantages of both methods mentioned above, we propose an improved solution which combines the inter-frequency dependence of power ratio in (Sawada et al., 2007b) and the permutation alignment scheme in (Murata
et al., 2001). Comparing with them, the proposed method is more effective and easier to implement.

The rest of the paper is organized as follows. The principle of frequency-domain blind source separation is introduced in Sec. 2. The proposed permutation method is described in detail in Sec. 3. Experimental results are presented in Sec. 4. Finally, Sec. 5 concludes the paper.

2. Frequency-domain blind source separation

Suppose that $N$ source signals $s(n) = [s_1(n), \ldots, s_N(n)]^T$ are mixed and recorded by $M$ sensors, the observed signals $x(n) = [x_1(n), \ldots, x_M(n)]^T$ are given by

$$x_j(n) = \sum_{i=1}^{N} \sum_{p=1}^{P} h_{ji}(p)s_i(n-p+1), \quad (j = 1, \ldots, M), \quad (1)$$

where $h_{ji}$ is a $P$-point impulse response from source $i$ to microphone $j$. With blind source separation, the estimated source signals $y(n) = [y_1(n), \ldots, y_N(n)]^T$ are obtained:

$$y_j(n) = \sum_{i=1}^{M} \sum_{q=1}^{Q} w_{ji}(q)x_i(n-q+1), \quad (j = 1, \ldots, N), \quad (2)$$

where $w_{ji}$ is a $Q$-point unmixing filter.

The unmixing filters can be calculated using the frequency-domain method. Figure 1 gives the system structure of frequency-domain BSS. First, $x(n)$ is converted into a time-frequency series $X(m, f)$ by a blockwise $L$-point short-time Fourier transform (STFT). Thus, the convolution in (1) becomes a multiplication:

$$X(m, f) = H(f)S(m, f), \quad (3)$$

where $m$ is the frame index, $f \in [f_0, \ldots, f_{L/2}]$ is the frequency.

$$X(m, f) = [X_1(m, f), \ldots, X_M(m, f)]^T$$

and

$$S(m, f) = [S_1(m, f), \ldots, S_N(m, f)]^T$$

are the STFT of $x(n)$ and $s(n)$, respectively; $H(f)$ is the $M \times N$ mixing matrix at frequency $f$.

Moreover, separation is performed in each frequency bin $f$:

$$Y(m, f) = W(f)X(m, f), \quad (4)$$

where $Y(m, f) = [Y_1(m, f), \ldots, Y_N(m, f)]^T$ is the STFT of $y(n)$, $W(f)$ is the $N \times M$ unmixing matrix at $f$. Complex-valued instantaneous BSS algorithms, such as FastICA (Bingham, Hyvärinen, 2000) and Informax (Bell, Sejnowski, ...
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**Permutation alignment**

In this section, we describe the proposed permutation alignment method from two aspects: inter-frequency dependence measure and permutation alignment scheme.

### 3.1. Inter-frequency dependence measure

The inter-frequency dependence of speech sources can be exploited to align the permutations across all frequency bins. An inter-frequency dependence measure 1995), can be used for the calculation of $W$. However, even if satisfactory separation may be obtained in each frequency bin, there are inherent scaling and permutation ambiguities. This is expressed as

$$Y(m, f) = W(f)X(m, f) \approx D(f)\Pi(f)S(m, f), \quad (5)$$

where $\Pi(f)$ is a permutation matrix and $D(f)$ is a scaling matrix, all at frequency $f$. These ambiguities should be corrected before transformation of the frequency-domain signals back into the time domain.

In the third step, the permutation matrix $\Pi(f)$ is determined at each frequency $f$ so that separated frequency components $Y_i(m, f)$ are grouped together for the same source. This issue will be addressed later in Sec. 3.

Next, the scaling ambiguity is corrected by using the Minimal Distortion Principle (Matsuoka, Nakashima, 2001):

$$W_s(f) = \text{diag}(W_p^{-1}(f)) \cdot W_p(f), \quad (6)$$

where $W_p(f)$ is $W(f)$ after permutation alignment and $W_s(f)$ is the one after scaling correction; $\cdot^{-1}$ denotes inversion of a square matrix or pseudo inversion of a rectangular matrix, and $\text{diag}(\cdot)$ retains only the main diagonal components of a matrix.

At the end of the flow, inverse STFT is applied to $W_s(f)$ to get the time-domain unmixing filters $w(n)$, and the estimated source signals $y(n)$ is obtained by the unmixing filtering in (2). The whole procedure described above is depicted in Fig. 1.

**Fig. 1. Workflow of frequency-domain blind source separation.**
proposed in (SAWADA et al., 2007b), the separated signal power ratio, can exhibit inter-frequency dependence among all frequencies effectively. Here we give the definition of this measure.

The $M \times N$ mixing network at frequency $f$ can be estimated from the separation network by

$$A(f) = W^{-1}(f) = [a_{1}(f), \ldots, a_{N}(f)],$$

(7)

where $a_{i}(f)$ is the $i$-th column vector of $A(f)$. The observed signal can be decomposed by

$$X(m, f) = \sum_{i=1}^{N} a_{i}(f)Y_{i}(m, f),$$

(8)

where $Y_{i}(m, f)$ is the $i$-th component of $Y(m, f)$, i.e.

$$Y(m, f) = [Y_{1}(m, f), \ldots, Y_{N}(m, f)]^{T}.$$

A power ratio measure is calculated to represent the activity of the $i$-th separated signal at frequency $f$. It is defined as

$$v_{i}^{f}(m) = \frac{\|a_{i}(f)Y_{i}(m, f)\|^{2}}{\sum_{k=1}^{N} \|a_{k}(f)Y_{k}(m, f)\|^{2}},$$

(9)

where the denominator is the total power of the observed signals $X(m, f)$, and the numerator is the power of the $i$-th separated signal. Being in the range $[0, 1]$, (9) is close to 1 when the $i$-th separated signal is dominant, and close to 0 when other signals are dominant. Due to the sparseness of speech signals, power ratio can exhibit the signal activity clearly.

The correlation coefficient of signal power ratios can be used for measuring the inter-frequency dependence and aligning of the permutation. The normalized bin-wise correlation coefficient between two power ratio sequences $v_{i}^{f_{1}}(m)$ and $v_{j}^{f_{2}}(m)$ is defined as

$$\rho(v_{i}^{f_{1}}, v_{j}^{f_{2}}) = \frac{r_{ij}(f_{1}, f_{2}) - \mu_{i}(f_{1})\mu_{j}(f_{2})}{\sigma_{i}(f_{1})\sigma_{j}(f_{2})},$$

(10)

where $i$ and $j$ denote two separated channels, $f_{1}$ and $f_{2}$ are two frequencies, $r_{ij}(f_{1}, f_{2}) = E\{v_{i}^{f_{1}}v_{j}^{f_{2}}\}$, $\mu_{i}(f) = E\{v_{i}^{f}\}$, $\sigma_{i}(f) = \sqrt{E\{(v_{i}^{f})^{2}\} - \mu_{i}^{2}(f)}$ are, respectively, the correlation, mean, and standard deviation at $m$. Note that $E\{\cdot\}$ denotes expectation, where the time index $m$ is omitted for clarity.

We expect the correlation coefficient $\rho(v_{i}^{f_{1}}, v_{j}^{f_{2}})$ of two sequences $v_{i}^{f_{1}}(m)$ and $v_{j}^{f_{2}}(m)$ to be high if they originate from the same source. The principle behind this is that the active time of bin-wise separated signals are likely to coincide among frequencies for the same source. This property will be used for aligning the permutation.
3.2. Proposed permutation alignment scheme

The permutation alignment scheme employed in (Murata et al., 2001) was developed especially for the dependence measure of signal envelope. We made some modifications to it to come up with a permutation alignment scheme based on the signal power ratio measure. It is described in the 5 steps presented below.

Step 1. Calculate the power ratio $v_i^f(m)$ for all $L/2 + 1$ frequency bins and all $N$ separated signals by (9).

Step 2. Re-arrange the frequencies: \( \{ f_0, \ldots, f_{L/2} \} \rightarrow \{ g_0, \ldots, g_{L/2} \} \), in ascending order of similarity between individual components, which is defined by

$$\text{sim}(g) = \sum_{i,j \neq j} \rho(v_i^g, v_j^g);$$

therefore,

$$\text{sim}(g_0) \leq \text{sim}(g_1) \leq \cdots \leq \text{sim}(g_{L/2}).$$

It is noticed that $\text{sim}(g) = \rho(v_1^g, v_2^g) = 0$ holds for all frequencies when there are only two sources. In this case, we use the envelope measure $v_i^g = |Y_i(g)|$ instead of (9) to calculate the similarity.

Step 3. For $g_0$, keep the permutation as it is, and set $k=1$.

Step 4. For $g_k$, find a permutation $\Pi_g$ that maximizes the correlation between the power ratio of $g_k$ and the aggregated power ratio sequence from $g_0$ through $g_{k-1}$. This is achieved by maximizing the sum of correlation coefficients

$$\Pi_g \leftarrow \arg \max_{\Pi} \sum_{l=1}^{N} \rho(v_i^g, c_l) |_{i=\Pi_g(l), c=\Pi_c(l)}$$

and $c$ is the centroid of the power ratio sequence from $g_0$ through $g_{k-1}$

$$c_l(m) = \frac{1}{k} \sum_{g=g_0}^{g_{k-1}} v_i^g(m) |_{i=\Pi_g(l)}, \quad l = 1, \ldots, N.$$  

Step 5. Set $k = k+1$ and go to step 4 until $k = L/2$. It is believed that the more different are the independent components at one frequency, the easier it is to get a correct permutation result. First, the method in (Murata et al., 2001) sorts frequency bins in increasing order of similarity among independent components; then align the permutation of the sorted frequency bins one by one. However, the method assumes high correlations even between frequencies that are far apart; this assumption is not always correct in all frequencies, especially with an envelope measure. With the power ratio measure, the inter-frequency becomes clearer and the dependence assumption may be satisfied in most frequencies. Thus the proposed method performs better than the one in (Murata et al., 2001). Furthermore, as it can be seen from the steps above, the permutation alignment scheme is rather straightforward and easy to implement.
4. Experiment results

The performance of the proposed method has been evaluated under light and medium reverberant conditions. Generally, the number of microphones should be larger than or equal to that of the sources, to ensure a complete solution (JOHO et al., 2000). Here we only consider identical number of sources and microphones for convenience and simplicity. Data were obtained by simulated impulse responses of a rectangular room, based on the image model method (ALLEN, BERKLEY, 1979). The simulated environment is shown in Fig. 2. All sources and microphones are placed 1.5 m high. The reverberation time was controlled by varying the absorption coefficient of the wall. To generate the microphone signals, we used 8-seconds long speech signals sampled at 8kHz, and they were convolved with the impulse responses. The proposed method was compared with the methods in (MURATA et al., 2001) and (SAWADA et al., 2007b). (For clarity, we call them the Murata method and the Sawada method, respectively). In addition, results of a “Benchmark” method are also included, which corrects permutation ambiguities by using the known mixing filters; therefore, it represents an ideal method (IKRAM, MORGAN, 2000).

![Fig. 2. Simulated room environment.](image)

The performance is measured by signal-to-interference (SIR) ratios in dB. The input and output SIRs for the J-th channel are defined as, respectively,

\[
SIR_{INJ} = 10 \log_{10} \frac{\sum_n |\sum_l h_{JJ}(l)s_J(n-l)|^2}{\sum_{k \neq J} \sum_n |\sum_l h_{JK}(l)s_k(n-l)|^2}, \tag{15}
\]

\[
SIR_{OUTJ} = 10 \log_{10} \frac{\sum_n |\sum_l g_{JP,J}(l)s_{p,J}(n-l)|^2}{\sum_{k \neq p,J} \sum_n |\sum_l g_{JK}(l)s_k(n-l)|^2}, \tag{16}
\]
where \( n \) is the time index, \( J = 1, \ldots, N \), and \( p(J) \) is the index of the output where the \( J \)-th source appears, \( h_{Jk}(n) \) is an element of \( H(n) \) (see (1)), and \( g_{Jk}(n) \) is an element of the overall impulse response matrix \( G(n) = W(n) * H(n) \).

The Tukey window is used in short time Fourier transform, with the STFT frame size of 2048 and a shift size of 512. The instantaneous BSS is implemented by means of the Scaled Informax (DOUGLAS, GUPTA, 2007), which can converge to the optimal solution within 100 iterations. In this paper, we set the iteration number as 100. The scaling ambiguity is solved by using Minimum Distortion Principle (6). The smoothing method proposed in (SAWADA et al., 2003) is applied in order to reduce spikes due to the circularity effect of the FFT. The processing bandwidth is between 100 and 3750 Hz (sampling rate being 8 kHz).

4.1. Performance evaluation in light reverberation

The proposed method is applied in a number of conditions. The reverberation time \( RT_{60} = 130 \) ms. Various \( 2 \times 2 \) (2 sources (1F, 1M)\(^{(1)}\) and 2 microphones (B, C)), \( 3 \times 3 \) (3 sources (1F, 2M) and 3 microphones (A, B, C)) and \( 4 \times 4 \) (4 sources (2F, 2M) and 4 microphones) simulation cases are carried out. Different combinations of source locations are tested for each case. The average input SIR is about 0 dB for \( 2 \times 2 \), \(-2 \) dB for \( 3 \times 3 \), and \(-5 \) dB for \( 4 \times 4 \) cases. The separation results with the four methods for the three cases are presented in Figs. 3, 4, and 5, respectively, where the horizontal axis is the source location and the vertical axis is the average output SIR.

![Figure 3](image_url)

Fig. 3. Separation results for 2 speakers and 2 microphones (\( RT_{60} = 130 \) ms).

\(^{(1)}\) Here ‘F’ means female and ‘M’ means male.
Compared to the benchmark, all the three “non-ideal” methods show nearly ideal separation in $2 \times 2$ cases. In $3 \times 3$ cases, the Sawada method performs better than the Murata method, and the proposed method performs even better – with an almost ideal separation. In $4 \times 4$ cases, the performance of the three methods all degrades evidently; however, the proposed one is the closest to the benchmark. In a word, combining the power ratio measure and the Murata permutation alignment scheme, the proposed method is superior to the other two under various simulation conditions.
The separation result depends mainly on two factors: instantaneous BSS and permutation alignment. It is easier to separate two sources when they are far apart and hence have different transfer functions to sensors. For example, better separation is observed for the $2 \times 2$ cases '1, 9', '2, 7' than for other ones. Similarly, although sources '3, 4' are placed on one straight line, they have different transfer functions to the sensors B and C, thus it is possible to get better separation results than for closely spaced sources '5, 7'.

4.2. Performance evaluation in medium reverberation

The proposed method is evaluated in medium reverberation with $RT_{60} = 300$ ms. The room layout is identical to the one in the previous experiment. We separate $3 \times 3$ mixtures with the four methods respectively: the proposed method, the Murata method, the Sawada method, and the Benchmark method. The separation results are depicted in Fig. 6. Comparing Fig. 6 with Fig. 4, it can be seen that the performance of the four methods all degrade evidently due to the longer mixing filters in medium reverberation. Again, the proposed method shows better performance than the Sawada method and the Murata method. In most cases, its performance is close to the ideal result.

![Graph showing separation results](image)

Fig. 6. Separation results for 3 speakers and 3 microphones ($RT_{60} = 300$ ms).

5. Conclusion

Studying the frequency-domain convolutive blind source separation, this paper proposes a new permutation alignment method which employs an inter-frequency measure: the power ratio of separated signals, and the Murata align-
ment scheme. The power ratio measure can exploit the inter-frequency dependence more clearly than the conventional metrics; the permutation alignment scheme is simple but effective. Thus, the proposed method performs better than other ones evaluated. Besides, it is easy to implement. Experimental results showed the effectiveness of the proposed method.

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