1. Introduction

Present global isostatic adjustment produced horizontal and vertical secular motion of the earth surface (Paulson et al., 2007). This process is frequently monitored by GNSS (Häkli and Koivula, 2010) and repeated absolute gravity measurements (Timmen et al., 2011). Determination of the small rates of the earth surface changes in some areas is still problematic. The accuracy of position determination from non-permanent GNSS measurement is 4-7 mm/5 days and permanent GNSS measurement is 2-3 mm/7 days. The accuracy of Absolute Gravity measurements are 1 μGal/16 hours. Integration of GNSS permanent and repeated gravity measurements is one of the ways for detection of vertical movement of the earth surface. This philosophy was applied for detection of movements in the Tatra Mountains.

2. GNSS measurements – basic information

The non-permanent GPS/GNSS measurements have been performed every year at 12 points (Fig. 1.) with special monument for repeated setup of GPS/GNSS antenna module with 0.5 mm accuracy. The GPS/GNSS campaigns have been organized annually with 4-5 days observation time using only Trimble dual frequency receivers. The non-permanent GPS/GNSS measurements have been connected to the reference permanent GNSS stations: BOR1, JOZE, GOPE, GRAZ, PENC.
Reprocessing of GNSS measurements were performed by standard scheme with Bernese software, version 5.0 in according with recommendation of European Permanent Network (EPN) and CEGRN consortium (Stangl, 2007). Input parameters (e.g. EOP, ephemerides, antenna PCV) were used from IGS service. The troposphere was eliminated using Niell mapping functions. All campaigns were processed as a free network with minimum constrain condition on reference points (BOR1, JOZE, GOPE, GRAZ, PENC) in global coordinate system ITRS, realization ITRF2005 (Altamimi et al., 2007). Components of relative velocity were estimated with special software and model APKIM2005D were used for reduction of global reference velocity. The relative horizontal and vertical velocities determined from observation time interval 1998-2010 are presented on Fig. 2. and Fig. 3.
Fig. 2. The relative horizontal velocities determined from GPS/GNSS observations, time interval 1998-2010

Fig. 3. The vertical velocities determined from GPS/GNSS observations, time interval 1998-2010
For better determination of horizontal and vertical movements near the three no permanent GPS/GNSS stations (GANO, LOMS and LIES) the permanent GPS/GNSS stations (GANP, LOMS and LIE1) have been established. The measurements of permanent stations started at GANO in 2003, at LOMS in 2004 and at LIES in 2007 and have been processed in the local analytical centre Slovak University of Technology in Bratislava (SUT) (points GANP, LOMS) and Institute of Geodesy and Cartography in Bratislava (point LIE1) in frame of the EPN and CEGRN. The EPN stations BOR1, BUCU, GOPE, GRAZ, MATE, PENC, SOFI and WTZR have been used as reference permanent GPS/GNSS station in processing of points GANP and LOMS (Hefty et al., 2010) and stations BOR1, GOPE, GRAZ, JOZE, PENC, UZHL in processing of point LIE1 (Droscak, 2012). The comparison between results of no permanent and permanent observations is presented on Fig. 4.

**Fig. 4.** Comparison of no permanent and permanent GPS/GNSS measurements

### 4. Processing of the absolute gravity measurements

The repeated absolute gravity measurements performed with FG5 at three gravity sites (GANO, SKPL and LIES) have been used for determination of the vertical land uplift/subsidence trend. The one day of absolute gravity measurements (from 12 to 24 hours) have been performed at GANO in 2003, 2005, 2006, 2007 and 2008, at SKPL in 2005, 2006, 2007 and 2008 and at LIES in 2004, 2006, 2007 and 2008. The absolute gravity data have been processed by Micro-g software assuming polar motion, atmospheric and tide corrections. Correction for the fringe value, difference
in reference heights and hydrological effects were added for each measurement separately.

4.1. Modeling the Hydrological Effect

Signal of the vertical movements observed with GPS/GNSS and especially absolute gravimeter can be contaminated with hydrological signal. The aim of the hydrological correction is to eliminate the hydrology from the observed signal of absolute gravimeter. Global hydrological model and local measurements of precipitation and evaporation were used for this purpose. Effect of the hydrological masses for the spherical distance (θ) greater than 0.045° (~5 km) from the point of observation were computed using Green's functions (Farrell, 1972), equation (1), with Love’s coefficients given by (Guo et al., 2004). In this case the hydrological masses were acquired using The Global Land Data Assimilation System NOAH (GLDAS) (Rodell et al., 2004).

\[
g(\theta) = \frac{g}{m_n} \sum_{n=2}^{\infty} [n + 2h_n - (n + 1)k_n] \frac{\mu}{n\rho} (\cos \theta).
\] (1)

Local hydrological correction for points up to 4900 m from the point of observation were computed using simple hydrological model based on precipitation (P) and evaporation (E) measured at meteorological sites near to the point of observation. The surface water height (Z) is defined by \(Z = P - E\). This information combined with digital elevation model DMR3 (0.25 m x 0.25 m) served as the input in to the equation for the gravitational effect of prism given by (Sorokin, 1951), equation (2).

\[
g = -G\rho \left[ X \ln(Y + R) + Y \ln(X + R) + \frac{Z_{\text{array}}}{XY} \right].
\] (2)

5. Velocity trends comparison

The time series of ellipsoidal heights determined by GPS/GNSS measurements and absolute gravity values on the points GANO, SKPL and LIES are presented on Fig 5. The trends of ellipsoidal changes and the absolute gravity changes, presented in Table 1 and Fig. 5, are very similar at the points GANO and SKPL but they differ slightly at the point LIES.

Table 1. Velocity trends

<table>
<thead>
<tr>
<th>Point</th>
<th>(\dot{g}) ((\mu\text{Gal/yr}))</th>
<th>(\dot{h}) ((\text{mm/yr}))</th>
<th>(\dot{g}/\dot{h}) ((\mu\text{Gal/mm}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>GANO</td>
<td>0.48</td>
<td>-3.36</td>
<td>-0.14</td>
</tr>
<tr>
<td>SKPL</td>
<td>-0.09</td>
<td>-1.38</td>
<td>0.07</td>
</tr>
<tr>
<td>LIES</td>
<td>-0.18</td>
<td>-1.05</td>
<td>0.17</td>
</tr>
<tr>
<td></td>
<td><strong>permanent station</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>GANP</td>
<td>0.48</td>
<td>-0.26</td>
<td>-1.85</td>
</tr>
<tr>
<td>LOMS</td>
<td>-0.09</td>
<td>-0.10</td>
<td>0.90</td>
</tr>
<tr>
<td>LIE1</td>
<td>-0.18</td>
<td>1.85</td>
<td>-0.10</td>
</tr>
</tbody>
</table>
6. Conclusions

- Horizontal motions of the Tatra Mountains are significant but vertical motions are not significant.
- The no permanent GPS/GNSS observations are less reliable for determinations of vertical movements, than permanent GPS/GNSS observations.
- The permanent GPS/GNSS and absolute gravity measurements have the same trend. The vertical movements determined from GPS/GNSS measurements are small on the point GANO and SKPL, except the site LIES.
- For investigation of vertical movements the repeated absolute gravity measurements are needed for the determination of the trends.
- The global, regional and local hydrological calibrated models are needed for processing of absolute gravity measurements.
Better understanding of the Tatra Mountains movements requires denser network of the permanent GNSS and absolute gravity sites.

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