In the case of bucket wheel excavators, the cutting process is influenced by the forces opposing the working elements and cutting tools. These forces determine the choice of machines and their parameters as well as the operating method [1, 2]. Studies conducted on the failure causes of mechanical parts show that the cutting and loading systems cause the highest rate of failure – about 32% of all recorded mechanical failures [3].

In this paper, we will use the Finite Element Method (FEM) to analyze the deformations and stresses acting on the cutting teeth mounted on the rotor of BWEs. For this, SolidWorks® software was used, both as a CAD tool to design the teeth as well as to model and simulate the phenomena.

Key words: BWE, rotor, cutting teeth, cutting tooth support, FEM, force, strain, deformation

1. STEPS FOR A FEM APPROACH

The starting point for any project using FEM and simulation is a model that can be a part or a set of parts. First, the characteristics of the material(s) of the parts, the tasks to which they are subjected, and the restrictions are defined [4]. Subsequently, as with any FEM-based analysis tool, the geometry of the model is divided into relatively small entities called finite elements. Creating the elements is commonly called meshing [5].

The degrees of freedom (DOF) of a node in a finite element mesh define the ability of the node to perform translation and rotation. The number of degrees of freedom that a node possesses depends on the element type. In SolidWorks® simulation, the nodes of the solid elements have three degrees of freedom, while those of the shell elements have six degrees of freedom.

Creating the mesh network often requires changes in the CAD geometry:

- cancelling – the process of removing parts of the geometry that are insignificant to the analysis, such as fillets or bevels,
- idealization – a more aggressive process of changing the geometry; for example, thin walls are replaced with surfaces or beams replaced by lines,
- cleaning – necessary for the geometry to satisfy the requirements imposed by the meshing.

Creating a mathematical model consists of: modifying the CAD geometry (i.e., Fig. 1 – we removed the fillets), defining the loads and strains, imposing the restrictions, defining the properties of the material,
10 I. Kertesz Brinas, N.I. Rebedea, I.L. Oltean
and determining the type of analysis (static, dynamic, etc.) to be carried out [6]. The properties of the material, the tasks, and the restrictions imposed on the model make up the input information for a certain type of analysis.

The mathematical model based on the FEM geometry, the information and properties of the material, the requirements to which the model is subjected, and the imposed restrictions can be divided into finite elements using the meshing process (Fig. 2).

The discreet loads and restrictions are applied to the nodes of the finite element mesh [7].

Often, the most difficult step of an FEM study is the analysis of the results. The correct interpretation of the results implies the understanding of all of the simplifications and errors that they induce in the first three stages: defining the mathematical model, the meshing, and coming up with the solution.

2. VON MISES YIELD CRITERION

The von Mises stress test criterion (also known as the Huber criterion) is a stress test that represents all six components of a general 3-D state (Fig. 3).

The general stress is represented by three normal stresses \( \sigma_x, \sigma_v, \sigma_z \) and six tangential or shear stresses. Due to the symmetry of the shear stresses, the 3D general tension state is characterized by six components: \( \tau_{yx}, \tau_{yz}, \tau_{xz} = \tau_{zx} \).

Von Mises stress can be expressed by the following equation:

\[
\sigma_{vm} = \sqrt{\frac{1}{2}\left[(\sigma_x - \sigma_y)^2 + (\sigma_y - \sigma_z)^2 + (\sigma_z - \sigma_x)^2 + 3(\tau_{yx}^2 + \tau_{yz}^2 + \tau_{zx}^2)\right]}
\]

Von Mises stress is frequently used for the structural safety analysis of materials with elasto-plastic properties (such as steel or aluminum alloys). In theory, a ductile material yields when the von Mises stress equals the permissible stress limit. In most cases, the flow limit is used as a stress limit. According to the von Mises criterion in the case of failures, the factor of safety (FOS) is expressed as follows:

\[
FOS = \frac{\sigma_{\text{limit}}}{\sigma_{vm}}
\]

where \( \sigma_{\text{limit}} \) is the flow limit.

3. GEOMETRIC PARAMETERS OF TEETH OF BWES

The geometry of the cutting teeth of BWEs is influenced by:
- the functional parameters of the excavator,
- the constructive parameters of the cups (Fig. 4) and rotor (Fig. 5),
- the shape and type of cutting teeth used,
- the type of excavated material,
- cost.

There are two types of cutting teeth: 1 – chisel-shaped cutting teeth (used on BWEs); 2 – conically shaped cutting teeth (used on both single-bucket excavators and shearer-loader machines) [10].
In Figures 6 and 7, we present a chisel-shaped cutting tooth that is mounted on an ESRC – 1400-type BWE used in the Oltenia Basin open-pit lignite mines [11]. From the point of view of the geometric parameters, two types of cutting teeth are needed: one for overburden excavation, and the other for lignite excavation. We analyzed the tooth used for lignite excavation; the geometric parameters of these cutting teeth are shown in Table 1 [12].

For a realistic approach, the FEM was conducted on an assembly of a cutting tooth and its cup holder support bracket. When creating this assembly, we set up the geometrical links between the two components. Figure 8 shows the restrictions (fixation condition) imposed on the analyzed assembly.

### Table 1

<table>
<thead>
<tr>
<th>No.</th>
<th>Geometric parameters</th>
<th>Symbol</th>
<th>Dimensions of cutting tooth [°]</th>
<th>Correlation</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>angle of clearance</td>
<td>α</td>
<td>55</td>
<td>α + β + δ = 90°</td>
</tr>
<tr>
<td>2.</td>
<td>set angle</td>
<td>β</td>
<td>7</td>
<td></td>
</tr>
<tr>
<td>3.</td>
<td>angle of sharpening</td>
<td>δ</td>
<td>28</td>
<td>γ + α = 90°</td>
</tr>
<tr>
<td>4.</td>
<td>cutting angle</td>
<td>γ</td>
<td>35</td>
<td></td>
</tr>
<tr>
<td>5.</td>
<td>longitudinal lateral angle</td>
<td>ξ</td>
<td>5</td>
<td>–</td>
</tr>
<tr>
<td>6.</td>
<td>transverse lateral angle</td>
<td>θ</td>
<td>3</td>
<td>–</td>
</tr>
<tr>
<td>7.</td>
<td>rake angle</td>
<td>ϕ</td>
<td>13</td>
<td>–</td>
</tr>
<tr>
<td>8.</td>
<td>cutting edge width</td>
<td>b</td>
<td>120</td>
<td>–</td>
</tr>
</tbody>
</table>
The maximum tangential and normal cutting forces at the tooth’s trajectory were considered as well as the lateral force generated by the pivoting movement [13].

These forces have the following values:

\[ F_x = 60 \, \text{kN}; \quad F_y = 18 \, \text{kN}; \quad F_z = 10 \, \text{kN}. \]

With respect to the tooth surfaces, we will have the following component forces:

\[ F_{y1} = F_x \cos \alpha - F_y \cos \gamma = 25.857 \cdot 10^3 \, \text{N} \quad (3) \]

\[ F_{x1} = F_x \sin \alpha - F_y \sin \gamma = 36.198 \cdot 10^3 \, \text{N} \quad (4) \]

\[ F_{z1} = 10 \cdot 10^3 \, \text{N} \quad (5) \]

For these forces, the state of stresses for a cutting tooth with a sharpening angle of 28° (which has a leaner construction) were determined. These forces are the resultant forces of specific loads having a random distribution on the active faces of the cutting tooth, which (for our calculations) were considered as applied to the tip of the cutting tooth (Fig. 9).

Based on Figure 12, it can be observed that the most stress occurs on the tail part of the cutting tooth (between its holder and joint). The maximum von Mises stress is 332 N/mm².
5. CONCLUSIONS

FEM is a numerical analysis method that is used to solve problems in various engineering fields. In mechanical engineering, it is widely used for solving structural, vibrational, and thermal problems; and because of its numerical versatility and efficiency, this method imposed itself on the engineering analysis software market while other methods have become niche applications.

FEM/FEA is mainly used during the product-development phase to analyze a project. The ultimate goal of using FEM as a design tool is to change the standard repetitive cycle of design → prototype → test into a simplified process in which the prototypes are not used as design tools but rather as a validation of the final design.

The use of FEM enables design iterations to shift from the physical space of prototypes and testing into the virtual space of computer simulation.

The simulation of the behavior of cutting teeth mounted on BWEs using FEM was based on the results (obtained over the years by the Department of Mechanical, Industrial, and Transport Engineering) of research contracts aimed at improving the performance of BWEs used in open-pit mining in the Oltenia Basin.

The results obtained using this method are consistent with those determined by analytical methods in the research studies conducted within the MITE Department:

- mounting the cutting tooth into a cup holder causes the von Mises stress to be maximal in the tail area of the tooth, holder, and joint;
- the maximum deformation occurs at the tip of the cutting tooth;
- it is necessary to design a new holder that will better encase the cutting tooth and to carry out a study of the deformations and stresses in this new configuration using simulation and modeling.

References


ILDIKO KERTESZ BRINAS, M.Sc., Eng. 
NARCIS IONEL REBEDEA, M.Sc., Eng. 
ILIE LUCIAN OLTEAN, M.Sc., Eng. 
Department of Mechanical, Industrial and Transportation Engineering 
University of Petroșani 
20 Universității str. 
332006 Petroșani, HD, Romania 
kerteszildiko@gmail.com