Atomic short-range order in mechanically synthesized iron based Fe-Zn alloys studied by $^{57}$Fe Mössbauer spectroscopy

**Abstract.** Mechanical alloying method was applied to prepare nanocrystalline iron-based Fe$_{1-x}$Zn$_x$ solid solutions with $x$ in the range $0.01 \leq x \leq 0.05$. The structural properties of the materials were investigated with the Mössbauer spectroscopy by measuring the room temperature spectra of $^{57}$Fe for as-obtained and annealed samples. The spectra were analyzed in terms of parameters of their components related to unlike surroundings of the iron probes, determined by different numbers of zinc atoms existing in the neighborhood of iron atoms. The obtained results gave clear evidence that after annealing process, the distribution of impurity atoms in the first coordination spheres of $^{57}$Fe nuclei is not random and it cannot be described by binomial distribution. The estimated, positive values of the short-range order parameters suggest clustering tendencies of Zn atoms in the Fe-Zn alloys with low zinc concentration. The results were compared with corresponding data derived from Calphad calculation and resulting from the cellular atomic model of alloys by Miedema.

**Key words:** hyperfine interactions • mechanical alloying • Mössbauer spectroscopy • nanocrystalline materials • short-range order

**Introduction**

Mechanical alloying (MA) is one of the non-equilibrium processing methods [1] that allow one to obtain such materials as nanocrystalline solid solutions, amorphous alloys, or composites with unique properties. The controlled thermal treatment of mechanically alloyed products combined with a structural investigation, allow determining the structural stability of the materials. Monitoring of MA by Mössbauer spectroscopy concerns important information about structural changes, phase transformations, magnetic and thermodynamic properties.

While the macroscopic magnetic properties of the binary iron-based alloys obtained by various methods were described in the literature quite well, the hyperfine interactions in these alloys are not well known, especially in the case of the mechanically synthesized alloys being subsequently subjected to thermal treatment. Moreover it is known that mechanical, magnetic, and thermodynamic properties of alloys depend, in general, on local fluctuations in their composition. These fluctuations can be quantitatively described in terms of the short-range order (SRO) parameter $\alpha$, introduced by Cowley [2]. Physically, this parameter measures the deviation at short range from the random state, with values
Experimental and results

The powder samples of Fe\(_{1-x}\)Zn\(_x\) alloys with \(x\) in the range \(0.01 \leq x \leq 0.05\), were prepared by milling appropriate amounts of the Aldrich 99.98% pure crystalline iron and 99.999% pure crystalline zinc; both materials in a form of particles with sizes less than 0.5 mm. The mechanical alloying processes were performed in a Fritsch Pulverisette 6 planetary ball mill with stainless-steel vial and balls. The total weight of the powders was 10 g and the ball-to-powder weight ratio was 10:1. The milling processes were carried out at room temperature under an argon atmosphere and the milling speed amounted to 500 rpm.

The room temperature \(^{57}\text{Fe}\) Mössbauer spectra were measured for the studied samples by means of a constant-acceleration POLON spectrometer of standard design. The measurements for each specimen were performed twice, just after its synthesis in the mill and after an annealing process. All samples were annealed in vacuum at 700 K for 12 h. After that they were slowly cooled to room temperature over 6 h. Under those conditions, diffusion effectively stops at a certain temperature \(T_d\), so the observed distributions of atoms in the annealed specimens should be the frozen-in state, corresponding to the temperature. According to the data given in the literature, \(T_d\) for iron is close to 700 K [12]. Spectra for the samples after the annealing process are presented in Fig. 1.

Each measured spectrum was fitted with a sum of a certain number of different six-line patterns corresponding to hyperfine fields (\(B\)) at \(^{57}\text{Fe}\) nuclei generated by different numbers of Fe and Zn atoms located in the first coordination shell of the probing nuclei. The number of fitted patterns depended on the concentration of zinc in the samples. The fitting procedure was done under assumption that the influence of Zn atoms on \(B\) as well as the corresponding isomer shift (IS) of a six-line subspectrum, are additive and independent of the atom positions in the first coordination shell of the nuclear probe [15]. In other words it was accepted that for each subspectrum the quantities \(B\) and IS are linear functions of the numbers \(n\) of Zn atoms located in the first coordination shell of \(^{57}\text{Fe}\) and the functions can be written as follows:

\[
\begin{align*}
B(n) &= B_0 + n\Delta B_1, \\
\text{IS}(n) &= \text{IS}_0 + n\Delta\text{IS}_1
\end{align*}
\]

where \(\Delta B_1\) (\(\Delta\text{IS}_1\)) stands for the change of \(B\) (IS) with one Zn atom located in the first coordination shell of the Mössbauer probe. At the same time we assume that the quadrupole splitting/shift QS for all fitted six-line patterns is equal to zero because of the cubic symmetry of the iron-based alloys. Moreover, it was assumed that the three linewidths \(\Gamma_{16}, \Gamma_{25}\), and \(\Gamma_{34}\) for all components of a spectrum which are related to the existence of impurity atoms in the first coordination shell of \(^{57}\text{Fe}\) are the same and they are different from linewidths of that component, determined by the nuclear probes having in their vicinity only Fe atoms. This division of sub spectra into two sets with different linewidths takes into account the fact observed for other systems, that the linewidths can be influenced by an existence of large/small enough impurity atoms in the nearest neighborhood of the Mössbauer probes. The example of a fit obtained under these assumptions is presented in Fig. 2 whereas the found values of the best-fit parameters are displayed in Table 1. The values essentially differ from corresponding data.
given in the literature [14–16]. In Ref. [14] one can find that for the Fe\text{0.965}Zn\text{0.035} alloy \(B_0 = 32.96(2)\) T, \(\Delta B_1 = -1.60(2)\) T, \(\Delta B_2 = -0.06(3)\) T, \(\Delta B_3 = 1.30(2)\) T, and for Fe\text{1-x}Zn\text{x} \((x < 0.2)\) [15]: \(\Delta B_1 = -1.80\) T, \(\Delta B_2 = -0.70\) T. At the same time, theoretically calculated values reported in work [16] are \(\Delta B_1 = -1.34\) T, \(\Delta B_2 = -0.28\) T, \(\Delta B_3 = 0.74\) T.

As the main result of the analysis, the values of parameters \(c(0), c(1),\) and \(c(2)\) were determined. The parameters are intensities of those components of a spectrum which are related to the existence of zero, one or two \((n)\) zinc atoms in the first coordination shell of nuclear probes \(^{57}\text{Fe},\) respectively. The \(c(n)\) values were used to find parameter \(\langle n\rangle\) being the average number of Zn atoms in the first coordination shell of \(^{57}\text{Fe}\) Mössbauer probe:

\[
\langle n\rangle = \sum_{n=0}^{8} nc(n) \tag{2}
\]

The results are presented in Figs. 3a and 3b.

In disordered iron-based alloys, the probability \(p(n)\) of occurring given configuration of impurity atoms in the first coordination spheres of \(^{57}\text{Fe}\) nucleus can be described by the binomial distribution \(p(n) = \frac{N!}{(N-n)!n!}x^n(1-x)^{N-n}\) where \(N\) denotes, for example, the coordination number of the first or first and second spheres, \(x\) is the concentration of impurity atoms, and \(n\) stands for the number of impurity atoms in the first or the first and second coordination spheres. In the case of Fe\text{1-x}Zn\text{x} alloys with the \(x\) range 0.01 \(\leq x \leq 0.05,\) atoms are distributed in the bcc lattice and the total number of atoms located in first coordination sphere of \(^{57}\text{Fe}\)

\[
\text{Table 1. Some of the best-fit parameters of the assumed model of the }^{57}\text{Fe Mössbauer spectrum measured for annealed samples of Fe}_{1-x}\text{Zn}_x\text{ alloys. The standard uncertainties for the parameters result from the variance of the fit}
\]

<table>
<thead>
<tr>
<th>(x)</th>
<th>(B_0) [T]</th>
<th>(\Delta B_1) [T]</th>
<th>(IS_0) [mm/s] (\text{relative to } \alpha\text{-Fe})</th>
<th>(\Delta IS_1) [mm/s]</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.01</td>
<td>32.819(46)</td>
<td>-0.963(16)</td>
<td>0.0087(29)</td>
<td>0.0016(11)</td>
</tr>
<tr>
<td>0.02</td>
<td>32.819(48)</td>
<td>-1.067(13)</td>
<td>0.0070(21)</td>
<td>0.0081(37)</td>
</tr>
<tr>
<td>0.03</td>
<td>32.905(71)</td>
<td>-0.884(12)</td>
<td>0.0085(26)</td>
<td>0.0080(39)</td>
</tr>
<tr>
<td>0.04</td>
<td>32.886(41)</td>
<td>-1.021(15)</td>
<td>0.0075(35)</td>
<td>0.0225(50)</td>
</tr>
<tr>
<td>0.05</td>
<td>32.916(51)</td>
<td>-1.066(17)</td>
<td>0.0075(39)</td>
<td>0.0181(52)</td>
</tr>
</tbody>
</table>

Fig. 2. The \(^{57}\text{Fe Mössbauer spectrum for the Fe}_{0.95}\text{Zn}_{0.05}\) alloy measured at room temperature after the annealing process at 700 K, fitted with three six-line subspectra.

Fig. 3. Total intensities of those components of a spectrum which are related to the existence of zero \((c(0)\) blue points\), one \((c(1)\) green points\) and two \((c(2)\) red points) Zn atoms in the first coordination shells of nuclear probes \(^{57}\text{Fe}\) in the nanocrystalline Fe\text{1-x}Zn\text{x} alloys after (a) the mechanical milling and (b) the annealing process at 700 K. The solid lines describe probabilities of finding zero \(p(0)\), one \(p(1)\) and two \(p(2)\), Zn atoms in the first coordination shell \((N_1 = 8)\) of an Fe atom in the random bcc Fe\text{1-x}Zn\text{x} alloy.

is equal to 8. In the real alloys, the distribution of impurity atoms is generally different from the statistical one. This deviation from the random state can be quantitatively described by SRO parameter. The SRO parameters for systems with bcc lattice have the following form [2]:

\[
\alpha_1 = 1 - \frac{\langle n\rangle}{8x} \tag{3}
\]

when it concerns the first coordination shell.
for all as-obtained specimens the parameter values are presented in Table 2 and Fig. 4. As one can see well as those annealed at 700 K for 12 h. The results of samples, those as-obtained in a planetary ball mill as well as those annealed at 700 K for 12 h. The results are presented in Table 2 and Fig. 4. As one can see for all as-obtained specimens the parameter values are negative and its absolute value is relatively small. This testifies that the Zn atoms were practically randomly distributed in the iron matrix during the mechanical alloying process. On the other hand in the case of the annealed samples the situation is different because one observes positive large values of the parameter. The parameter values suggest that in the first shell of the nuclear probes being in the annealed alloys there are much less Zn atoms than in corresponding random alloys. The fact can be explained by a tendency of Zn atoms to form clusters in iron-based Fe-Zn solid solutions. In terms of interactions it means that the interaction between Fe and Zn atoms is repulsive (predominance of Zn-Zn bonds). The observation can be compared with the Miedema’s model predictions [17] on the enthalpy $H_{\text{Fe-Zn}}$ of the solution of Zn in Fe as well as the results of Calphad calculations concerning enthalpy of formation $H^{\text{for}}$ for the Fe-Zn alloys [18–20]. It is possible because the enthalpy $H^{\text{for}}$ is related to the enthalpy $H_{\text{Fe-Zn}}$ in the following way:

$$H_{\text{Fe-Zn}} = \left[\frac{\partial H^{\text{for}}}{\partial x}\right]_{x = 0}$$

On the other hand, the enthalpy $H_{\text{Fe-Zn}}$ is related to the binding energy $E_b$ between two Zn atoms in the dilute Fe$_{1-x}$Zn$_x$ system with $x$ close to zero. According to Królas model [21]

$$H_{\text{Fe-Zn}} = -2E_b(0)/2,$$

where $E_b(0)$ is the extrapolated value of $E_b$ for $x = 0$ and $z$ stands for the coordination number of the crystalline lattice ($z = 8$ for $\alpha$-Fe).

Positive value of enthalpy $H_{\text{Fe-Zn}}$ of solution of zinc in iron predicted by Miedema’s model (displayed in Table 3) means that interaction between zinc atoms in iron matrix is attractive – negative value of binding energy between two Zn atoms. This model prediction coincides with our observation based on SRO values, that zinc atoms form clusters in iron-based Fe-Zn solid solutions. However, Calphad calculations are at variance with such result. Negative values of enthalpy $H_{\text{Fe-Zn}}$ of solution of zinc in iron obtained on the basis of Calphad computations (included in Table 3) indicate that the interaction between zinc atoms is repulsive – positive value of binding energy between two Zn atoms.

Conclusions

The $^{57}$Fe Mössbauer study of the short-range order parameter $\alpha_1$ for Fe$_{1-x}$Zn$_x$ nanocrystalline alloys reveals that the parameter depends on the heat treatment of the investigated specimens. For the as-obtained powder specimens, the $\alpha_1$ parameters are negative and its absolute value is relatively small. This testifies that the Zn atoms were practically randomly distributed in the iron matrix during the mechanical alloying process. On the other hand in the case of the annealed samples, the situation is different because one observes disappearance of the slight ordering-type correlations (the predominance of Fe-Zn bonds) and nanocrystalline alloy exhibits clustering tendencies. The positive $\alpha_1$ value means that in the first coordination shell of the nuclear

### Table 2. The SRO parameter $\alpha_1$ for the nanocrystalline Fe$_{1-x}$Zn$_x$ alloys deduced from the $^{57}$Fe Mössbauer spectra

<table>
<thead>
<tr>
<th>$x$</th>
<th>Powder samples before annealing process $\alpha_1$</th>
<th>Powder samples after annealing process $\alpha_1$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.01</td>
<td>$-0.0338(74)$</td>
<td>0.6573(86)</td>
</tr>
<tr>
<td>0.02</td>
<td>$-0.2070(14)$</td>
<td>0.5948(78)</td>
</tr>
<tr>
<td>0.03</td>
<td>$-0.0670(13)$</td>
<td>0.6100(10)</td>
</tr>
<tr>
<td>0.04</td>
<td>$-0.0956(91)$</td>
<td>0.6492(36)</td>
</tr>
<tr>
<td>0.05</td>
<td>$-0.0064(58)$</td>
<td>0.7497(35)</td>
</tr>
</tbody>
</table>

### Table 3. The enthalpy $H_{\text{Fe-Zn}}$ [eV/atom] of solution of zinc in iron

<table>
<thead>
<tr>
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<th></th>
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</thead>
<tbody>
<tr>
<td>1.183</td>
<td>$-0.059^<em>, -0.065^</em>, -0.088^{**}$</td>
</tr>
</tbody>
</table>
probes being in the annealed nanocrystalline alloys, there are much less Zn atoms than in corresponding random alloys. In terms of interactions it means that the interaction between two Zn atoms is attractive (predominance of Zn-Zn bonds). This conclusion agrees with the semi-empirical Miedema’s model predictions [17] and it is at variance with Calphad calculations [18–20].

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References